

Lecture: 02

Inadequacies of Classical Mechanics:-

In C.M., we can find inadequacies / errors of such kinds:-

i) Stability of Matter:-

In an ionic material, ions are in motion. Electrons revolve around nucleus of an atom. Electrons constantly accelerate as they emit radiation (radiation \Rightarrow a charged particle emits light when it accelerates).

This radiation cannot be seen when electrons emit radiation, they should fall in nucleus in

The time of order of 10^{-10} m.

Such a collapse would be catastrophic

for the chemical behaviour of the atoms. So classically

stability of matter was not observed. which was later

discussed by Q.M. currently.

2) Optical Spectra:-

Simply in simple wording seven colour strip is optical spectra

Radiation emitted from elements heats up the material or an electrical discharge takes place in gaseous form, it is found to have continuous range of frequencies. If allowed frequencies are $\omega_1, \omega_2, \dots$ then formula for observed frequencies is

$$\omega = n_1\omega_1 + n_2\omega_2 + \dots$$

This is in linear combination

where n_1, n_2, \dots are integers.

But after experiments, results couldn't match, but with Ritz combination

→ Spectral lines of any element include frequency that is sum/diff of two other lines.

Now let's allowed frequencies are $\omega_1, \omega_2, \dots$ then observed freq. is

$$\omega = \omega'_n - \omega'_m$$

so optical spectra also obtained by wave mechanics not by e.m. Difference is clear by obtaining observed frequencies.

Principle of equipartition of Energy:-

\bar{E} = energy, T = Temperature
 $\bar{E} \propto T = \bar{E} = kT$, k is

Boltzmann constant.

Wave Number:-

It is defined as:-

Wave Number = $\frac{\text{No of cycles}}{\text{length}}$

Wave No = k

length = L , $k = \frac{2\pi n}{L}$
unit = cycle/m.

Rayleigh-Jeans formula:-

Black body Radiation:-

If an enclosure is in equilibrium in radiation with surroundings, called black body radiation.

Perfect Black Body:-

If a hole in enclosure observes

radiation but not escapes it, Then such body is called perfect black body.

Formula:-

Let 'L' be the length of box containing radiation, then each allowed frequency occurred in

The form of $e^{ik \cdot r}$,

where $k \cdot r = k_x x + k_y y + k_z z$

In order, that the wave remain in the box, being reflected back

4 forth from the walls, as it is necessary that it have the same value at one wall as opposite

one. so that the values of k

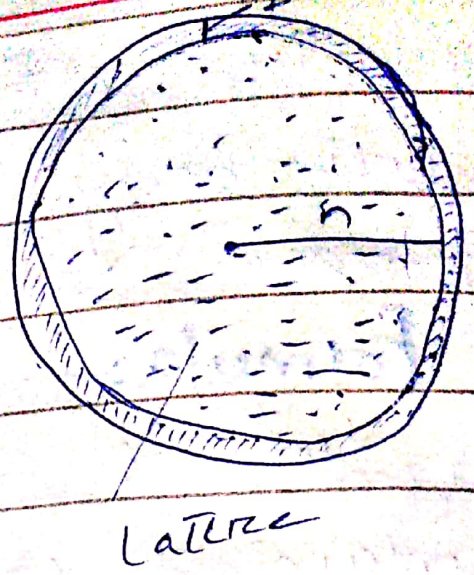
$$k_x = \frac{2\pi}{L} n_1, \quad k_y = \frac{2\pi}{L} n_2, \quad k_z = \frac{2\pi}{L} n_3$$

$$k = \frac{2\pi}{L} (n_1, n_2, n_3) \quad \text{where}$$

$$L^2 n^2 = n_1^2 + n_2^2 + n_3^2$$

We want to calculate no of allowed values of k.

we will regard n^3 pts in a lattice, we consider a shell having radius ' n ' & thickness



' Δn ', which is equal to vol of shell.

$$\text{Vol} = (4\pi n^2) \Delta n = 4\pi n^2 \Delta n$$

($n, \Delta n$ are not so small)

Simply we write formula of wave numbers, as

$$k = \frac{2\pi}{L} n \Rightarrow n = \frac{Lk}{2\pi}$$

we form our formula in wave form per unit volume when k lies b/w k & $k + dk$

$$|dn| = 2 \cdot \frac{1}{L^3} 4\pi \left(\frac{Lk}{2\pi} \right)^2 d\left(\frac{Lk}{2\pi} \right)$$

(we multiplied due to polarization by 2)

$$n = 2 \cdot \frac{1}{L^3} 4\pi \left(\frac{L}{2\pi} \right)^3 k^2 dk$$

$$\left. \begin{aligned} v &= \frac{v}{\lambda} \Rightarrow v = f \lambda \quad \text{--- (1)} \\ \omega &= \frac{c}{\lambda} \Rightarrow c = \omega \lambda \quad \text{--- (2)} \\ \lambda &= L \quad \text{if } n=1 \end{aligned} \right\}$$

$$Q(2) \quad c = \omega L \Rightarrow \omega = \frac{c}{L} = \frac{kc}{2\pi}$$

$$\Rightarrow k = \frac{2\pi\omega}{c}$$

Now we form our formula when n is dependent on ω & change in freq. changes from ω to $\omega + d\omega$

$$n(\omega) d\omega = 2 \cdot \frac{1}{L^3} 4\pi \left(\frac{L}{2\pi}\right)^3 \left(\frac{2\pi\omega}{c}\right)^2 d\left(\frac{2\pi\omega}{c}\right)$$

$$= 2 \cdot \frac{1}{L^3} 4\pi \frac{L^3}{8\pi^3} \left(\frac{2\pi}{c}\right)^3 \omega^2 d\omega$$

$$n(\omega) d\omega = \frac{8\pi}{c^3} \omega^2 d\omega$$

as formula of equipartition of energy is of one wave is kT . we can get total energy of all particles

$$E(\omega) d\omega = \frac{8\pi}{c^3} \omega^2 d\omega \cdot kT$$

\Rightarrow for low frequencies, but not for higher. But total energy of radiation per unit vol of enclosure $\Rightarrow \int_0^{\infty} E(\omega) d\omega$, which would be infinite. Indeed total energy must be finite.