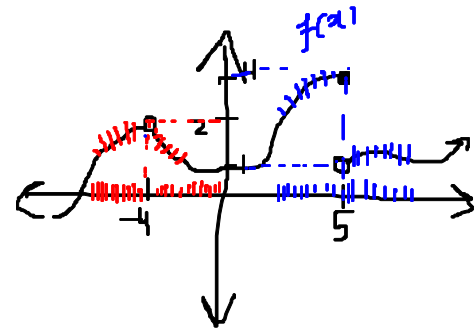


# FIND LIMIT WITH GRAPH



$$\lim_{x \rightarrow -4} f(x) = 2$$

$$\lim_{x \rightarrow -4} + f(x) = 2$$

$$\lim_{x \rightarrow -4} - f(x) = 2$$

$$f(-4) = \text{not defined}$$

$$\lim_{x \rightarrow 5} f(x) = \text{DNE}$$

$$\lim_{x \rightarrow 5} + f(x) = 4$$

$$\lim_{x \rightarrow 5} - f(x) = 4 = L$$

$$f(5) = 4$$

2. Use the graphs of  $f$  and  $g$  in the accompanying figure to find the limits that exist. If the limit does not exist, explain why.

$$\lim_{x \rightarrow 2} [f(x) + g(x)] = \lim_{x \rightarrow 2} f(x) + \lim_{x \rightarrow 2} g(x) = 0 + 0 = 0$$

(a)  $\lim_{x \rightarrow 2} [f(x) + g(x)] = 0$

(b)  $\lim_{x \rightarrow 0} [f(x) + g(x)] = \text{DNE}$

(c)  $\lim_{x \rightarrow 2} [f(x) + g(x)] = 0$

(d)  $\lim_{x \rightarrow 0^-} [f(x) + g(x)] = \text{DNE}$

(e)  $\lim_{x \rightarrow 2} \frac{f(x)}{1 + g(x)} = \frac{\lim_{x \rightarrow 2} f(x)}{1 + \lim_{x \rightarrow 2} g(x)} = \frac{0}{1 + 0} = 0$

(f)  $\lim_{x \rightarrow 2} \frac{1 + g(x)}{f(x)} = \frac{1 + 0}{0} = \infty$

(g)  $\lim_{x \rightarrow 0^+} \sqrt{f(x)} = \left( \lim_{x \rightarrow 0^+} |f(x)| \right)^{1/2} = (-2)^{1/2} = \text{ND}$

(h)  $\lim_{x \rightarrow 0^-} \sqrt{f(x)} = \left( \lim_{x \rightarrow 0^-} |f(x)| \right)^{1/2} = (-2)^{1/2} = \text{ND}$

$$\lim_{x \rightarrow 2} f(x) = 0$$

$$\lim_{x \rightarrow 2} g(x) = 0$$

$$\lim_{x \rightarrow 2} f(x) = 0$$

$$\lim_{x \rightarrow 2} g(x) = 0$$

$$\lim_{x \rightarrow 0} f(x) = -2 = L$$

$$\lim_{x \rightarrow 0} g(x) = 2 = L$$

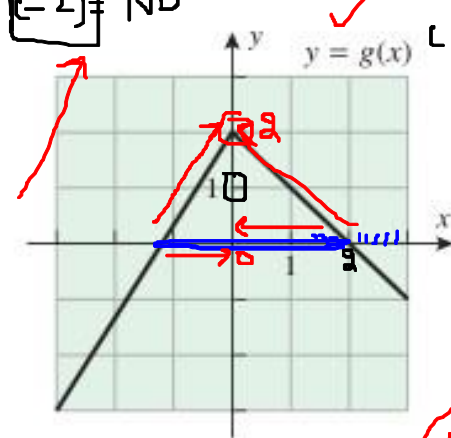
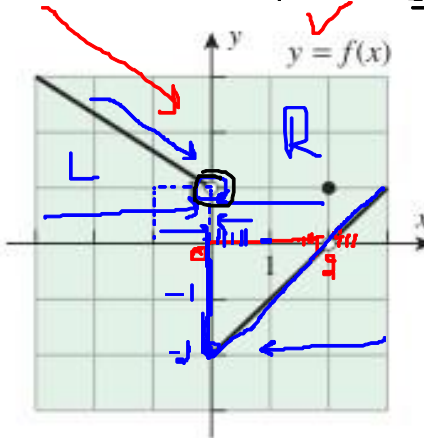
$$\lim_{x \rightarrow 0} f(x) = 2 = L$$

$$\lim_{x \rightarrow 0} g(x) = 2 = L$$

$$\lim_{x \rightarrow 0} f(x) = 2 = L$$

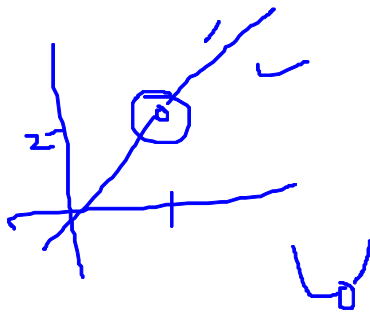
$$\lim_{x \rightarrow 0} g(x) = 2 = L$$

$$\sqrt{f(x)}$$



▲ Figure Ex-2

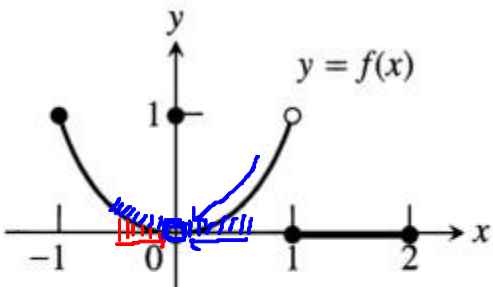
$$\infty, \text{DNE} \notin \mathbb{R}$$



$$\lim_{x \rightarrow 0} f(x) = 0$$

$$\lim_{x \rightarrow 0^+} f(x) = 0 = L$$

$$\lim_{x \rightarrow 0^-} f(x) = 0 = L$$

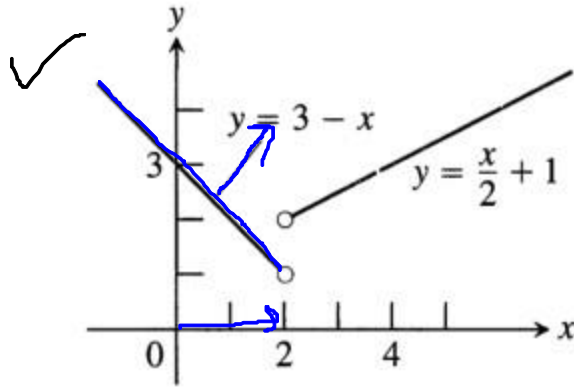


piecewise graph.

3. Let  $f(x) = \begin{cases} 3-x, & \boxed{x < 2} \\ \frac{x}{2} + 1, & \boxed{x > 2} \end{cases}$

L R

$\lim_{x \rightarrow 2^-}$   $\lim_{x \rightarrow 2^+}$

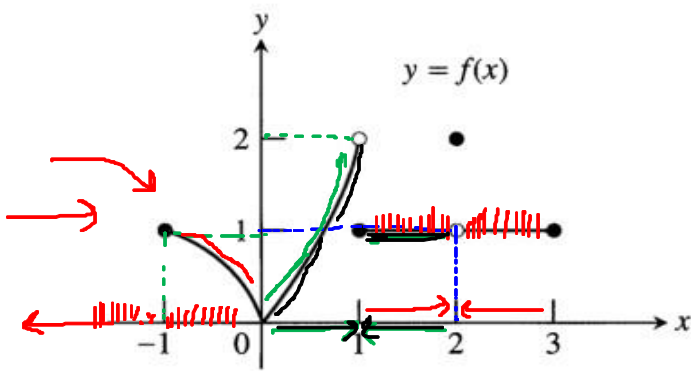


$\lim_{x \rightarrow 2} f(x) = \text{DNE}$

$\lim_{x \rightarrow 2^-} f(x) = \lim_{x \rightarrow 2^-} 3-x$   
 $= (3) - 2$   
 $= 1$  [exists]

$\lim_{x \rightarrow 2^+} f(x) = \lim_{x \rightarrow 2^+} \left(\frac{x}{2} + 1\right)$   
 $= \frac{2}{2} + 1$   
 $= 1 + 1 = 2$   
 (exists)

L  $\neq$  R



(a)  $\lim_{x \rightarrow 2} f(x) = 1$

Sol:-  
 $\lim_{x \rightarrow 2} f(x) = \lim_{x \rightarrow 2} f(x)$   
 $1 = 1$

(b)  $\lim_{x \rightarrow -1} f(x) = \text{DNE}$

Sol:-  $\lim_{x \rightarrow -1} f(x) = \lim_{x \rightarrow -1} f(x)$   
 $\text{DNE} \neq \text{DNE}$

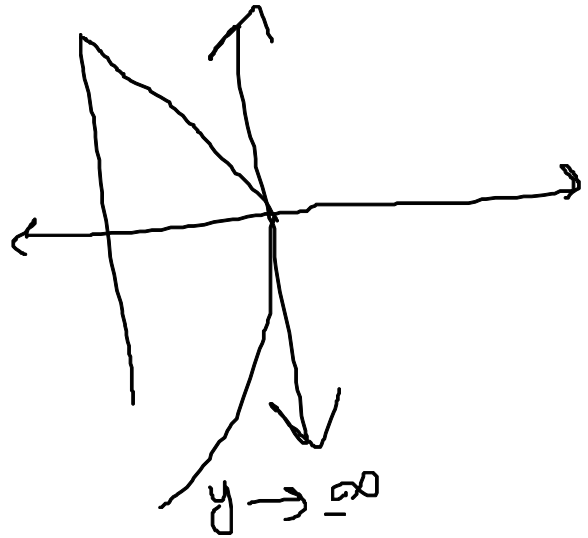
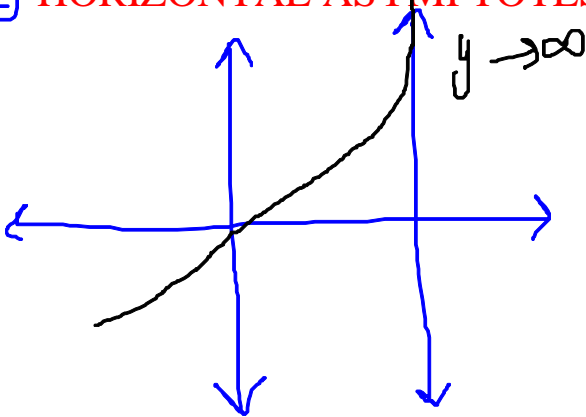
(c)  $\lim_{x \rightarrow 1} f(x) = \text{DNE}$   
 $\lim_{x \rightarrow 1^-} f(x) = \lim_{x \rightarrow 1^-} f(x)$   
 $2 \neq 1$

# INFINITE LIMITS

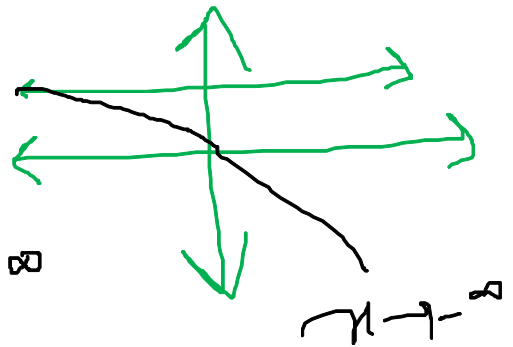
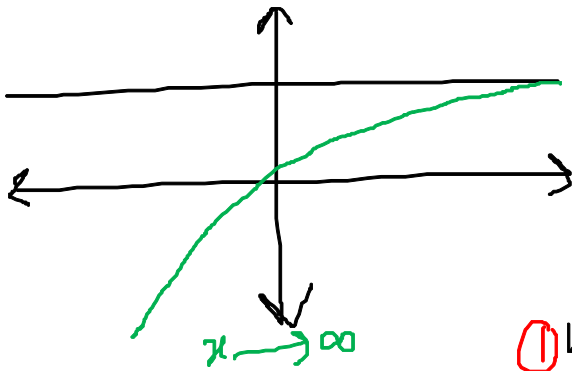
① VERTICAL ASYMPTOTES  $y =$

② HORIZONTAL ASYMPTOTES  $x =$

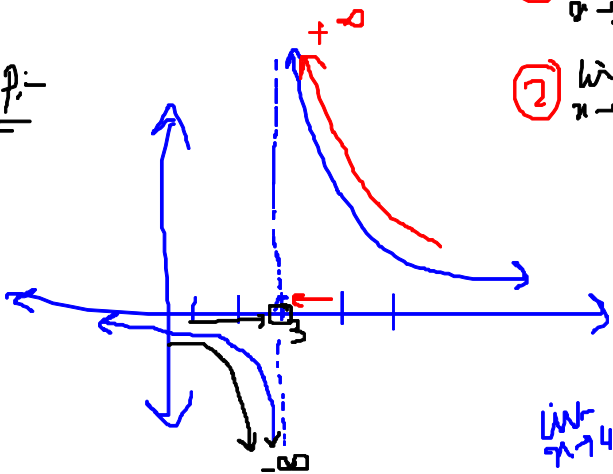
①



②



Exp:-



①  $\lim_{x \rightarrow 3^-} f(x) = -\infty$

②  $\lim_{x \rightarrow 3^+} f(x) = +\infty$

$\lim_{x \rightarrow 3} f(x) = \text{DNE}$

$\lim_{x \rightarrow 4} f(x) = \infty$  (DNE)

$\lim_{x \rightarrow 4^-} f(x) = +\infty$

$\lim_{x \rightarrow 4^+} f(x) = +\infty$

