

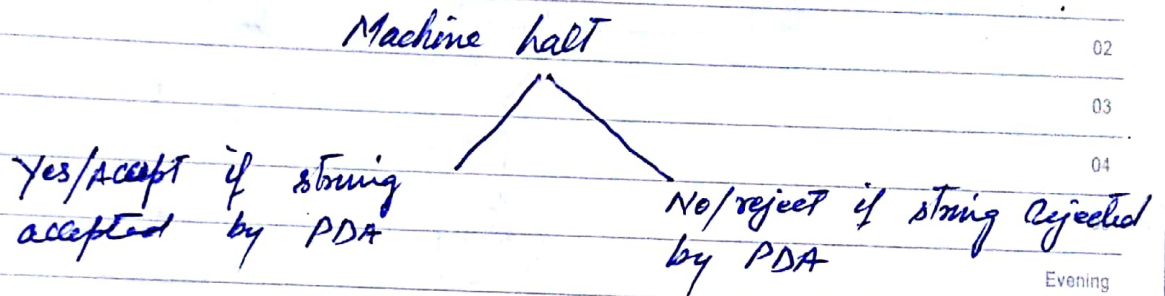
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Push Down Automata (PDA)

→ A mathematical model that corresponds analogously to CFL's that can be generated from CFG's is called PDA's.



Ex-1

$$a^+ = \{ a, aa, aaa, \dots \}$$

for string 'aa'

WEDNESDAY 23
۱۰ رجب

THURSDAY 24
۱۱ رجب

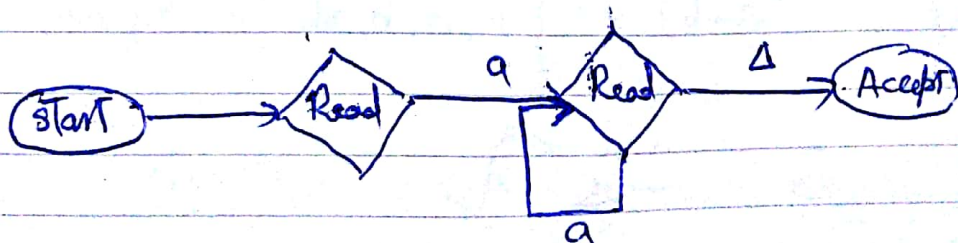


if the tape is blank, then



we read from left to right and right side is infinite and no back tracking is allowed here.

then PDA would be



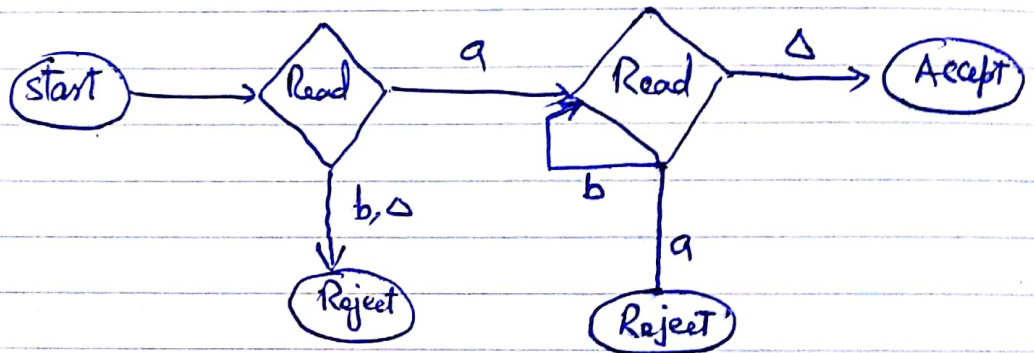
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Examples of PDA's for regular languages

(i) $ab^* = \{a, ab, abb, abbb, \dots\}$

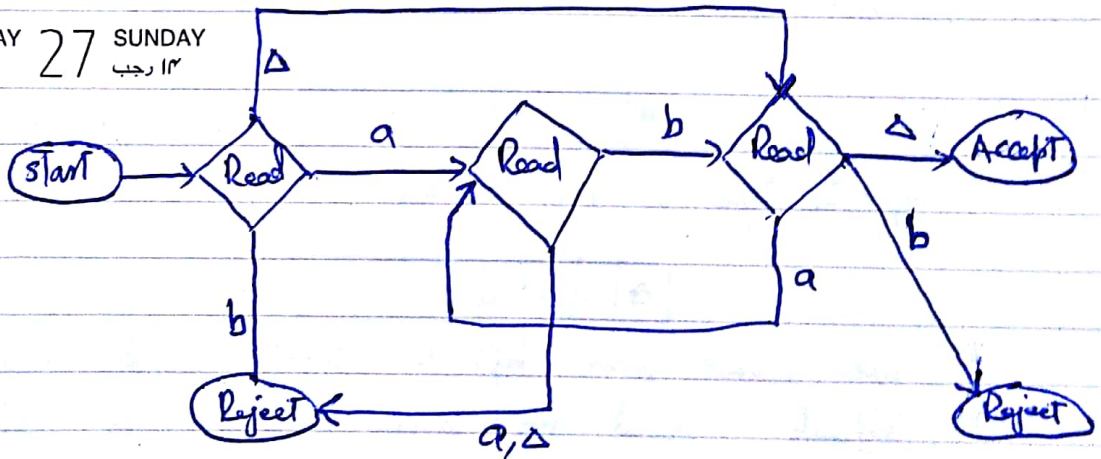


(ii) $(ab)^* = \{\Lambda, ab, abab, ababab, \dots\}$

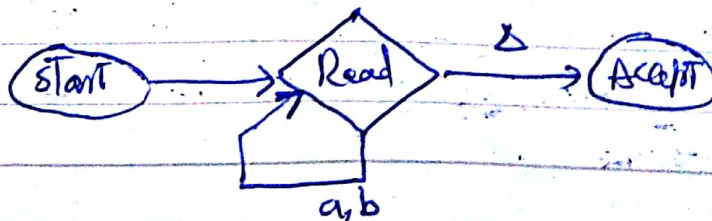
25 FRIDAY رجب ۱۳

26 SATURDAY رجب ۱۳

27 SUNDAY رجب ۱۳



(iii) $(a+b)^* = \{\Lambda, a, b, ab, ba, bb, aa, \dots\}$

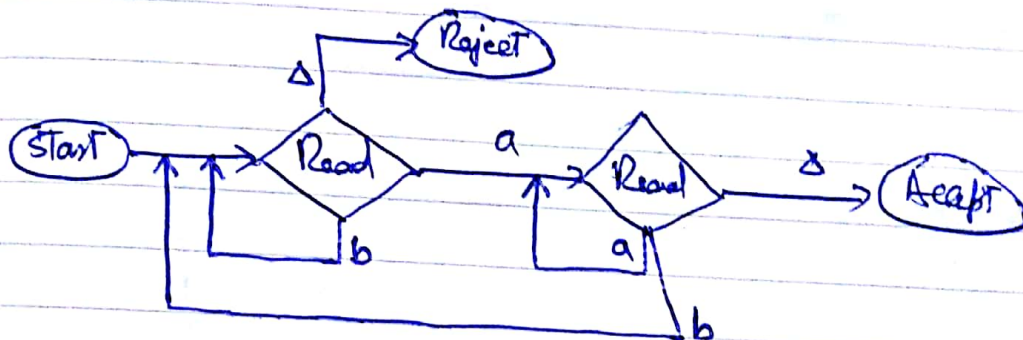


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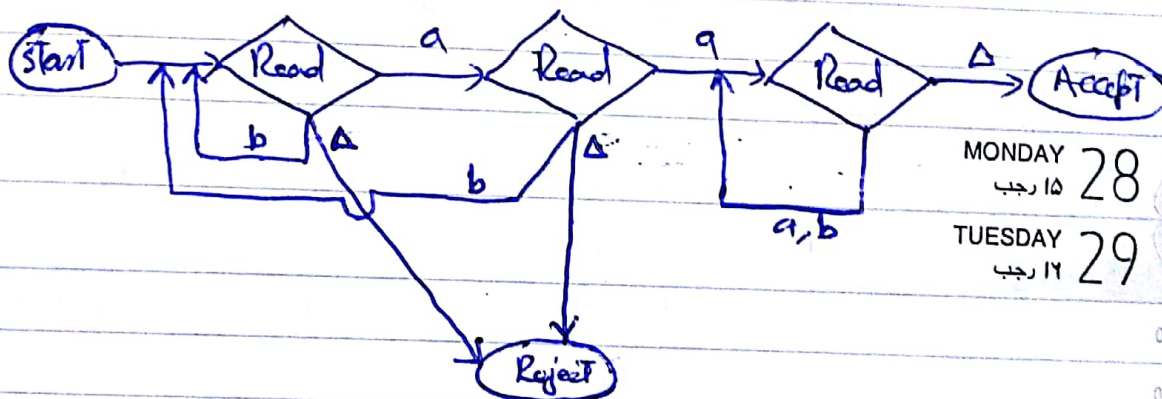
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(IV) - $\Sigma = \{a, b\}$ and $L \triangleq$ which ends with 'a'



(V) - $L \triangleq$ Contains substring 'aa'



MONDAY 28
رجب ۱۵

TUESDAY 29
رجب ۱۶

H.W Design PDA for " $a^n b^n$ "

Theorem: Every CFG has a PDA

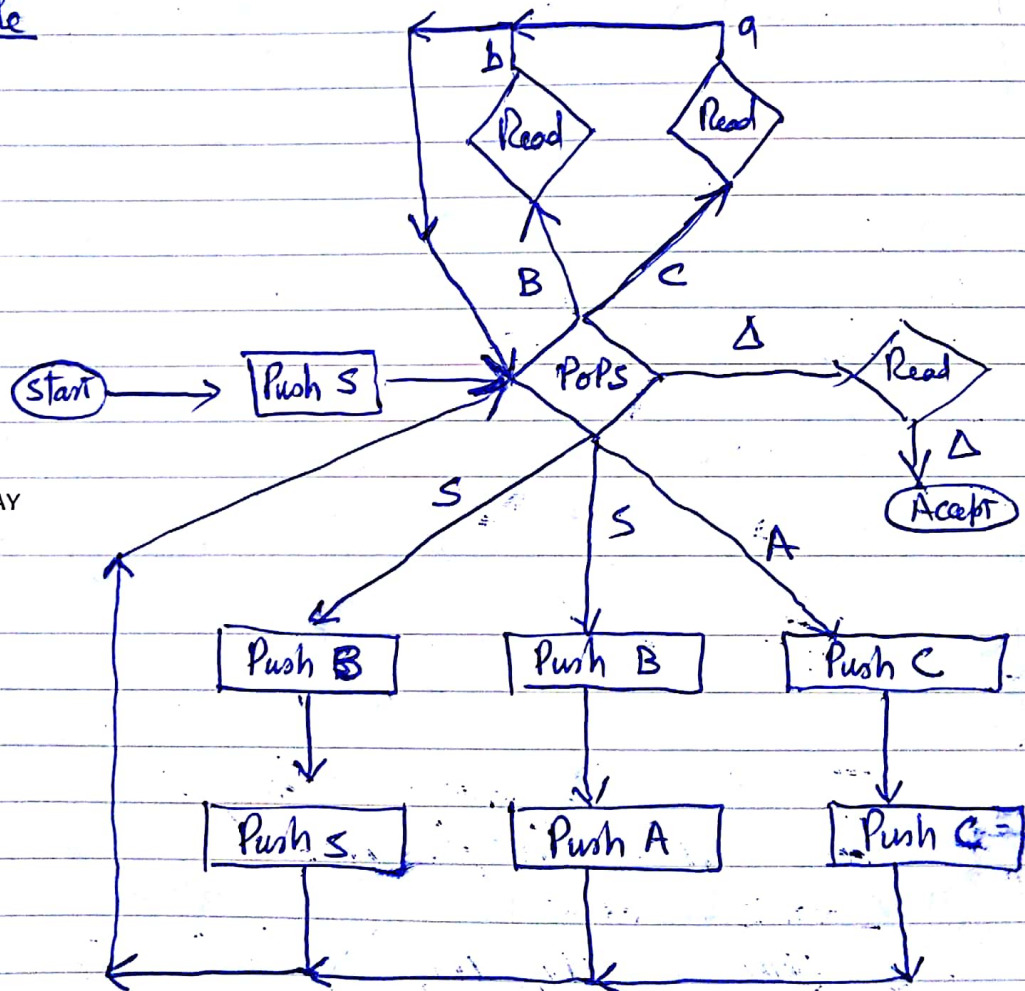
General (Construction of PDA Using CFG)

→ if a word is generated by CFG, then that word should also be accepted by its respective PDA.

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→ if a word can not be generated by CFG then it will be rejected by corresponding PDA

Example



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12 رجب
1 THURSDAY
18 رجب

- S → SB
- S → AB
- A → CC
- B → b
- C → a

JULY						
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JULY 2010

it is better that your CFG should be in CNF form, otherwise it is possibility that some rules stuck or not.

The Rules followed During Construction

→ if non-terminals on R.H.S of production
e.g. $NT \rightarrow NT_1, NT_2 \dots NT_i$

then Push on stack in Reverse direction

→ if all terminals on R.H.S of production
e.g. $NT \rightarrow T_1, T_2, T_3 \dots T_i$

then Read in forward direction

FRIDAY 2
رجب ۱۹

SUNDAY 4 SATURDAY 3
رجب ۲۱ رجب ۲۰

→ if $NT \rightarrow T_1, T_2, T_3 \dots T_i, NT_1, NT_2 \dots NT_j$

Then Read in forward direction ($T_1, T_2 \dots T_i$)
and Push $NT_j, NT_{j-1}, \dots, NT_1$ in Reverse order

→ $NT \rightarrow \underbrace{NT_1, NT_2 \dots NT_j}_1, \underbrace{T_1, T_2 \dots T_i}_2$

Then Push in Reverse order the non terminals while NT_j is Push twice and Read the remaining terminals $T_1, T_2 \dots T_i$ in forward direction.

→ $NT \rightarrow T_1, T_2 \dots T_i, NT_1, NT_2 \dots NT_j, T_1, T_2 \dots T_i$

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Then

- (i) Read $T_1, T_2 \dots T_n$ in forward
- (ii) Push NT's in reverse while pushed NT_2 twice.
- (iii) Read $T_1, T_2 \dots T_n$ in forward direction

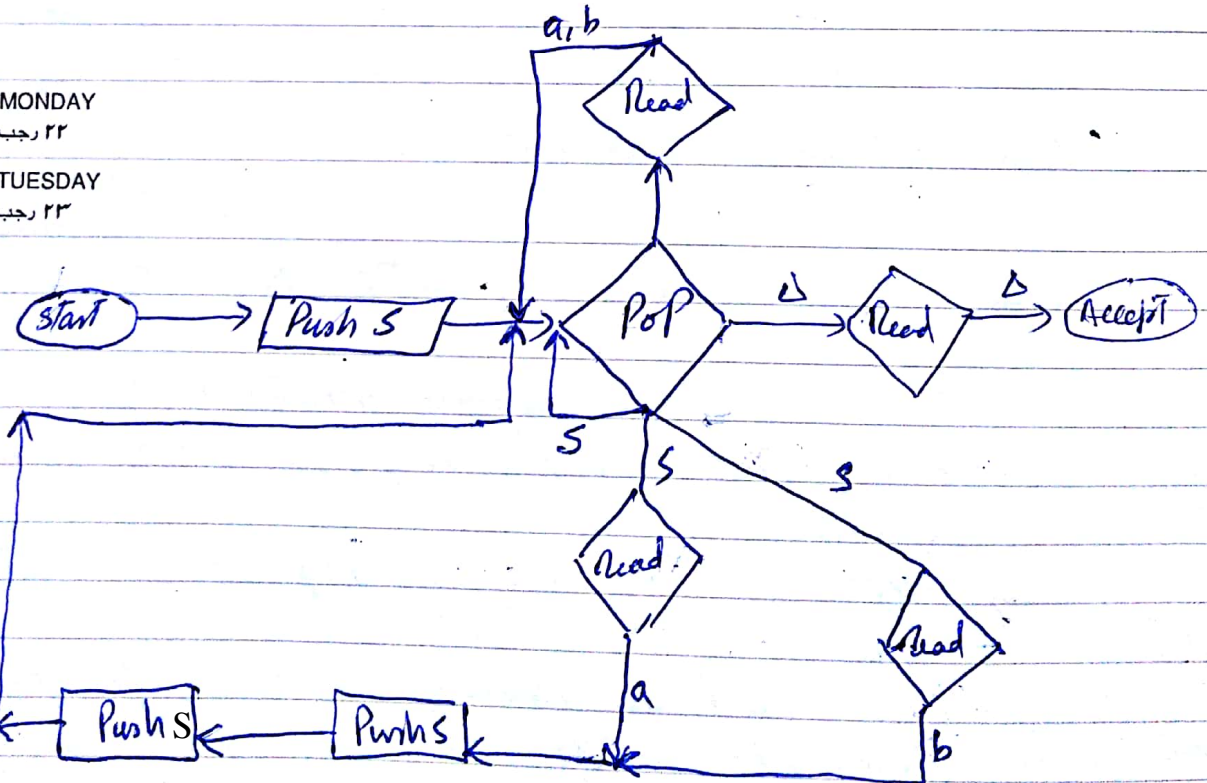
→ Only start symbol 'S' is pushed first

✓ Example

$S \rightarrow aSa / bSb / \Lambda$

5 MONDAY
رجب ۲۲

6 TUESDAY
رجب ۲۳



3
1

JULY

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for 'abba'

Stack

input Tape

Δ	abba	
ΔS	abba	
Δ	abba	(S POP)
ΔSS	a bbba	
ΔS	a bbba	(S POP)
ΔSSS	a bbba	
ΔSS	a bbba	(S POP) Evening
ΔSS	a bbba	
ΔS	a bbba	(S POP)
ΔS	a bbba	WEDNESDAY 7 رجب ۲۳
Δ	a bbba	THURSDAY 8 رجب ۲۴
	a bbba	
	a bbba	

Definition of PDA

A pushdown automaton (PDA) is a 7-tuple $M = \{Q, \Sigma, \Gamma, q_0, z_0, A, \delta\}$ where

Q is a finite set of states

Σ and Γ are finite sets (input & stack alphabets)

q_0 , the initial state

z_0 , the initial stack symbol $\in \Gamma$

A , the accepting state

$\delta: Q \times (\Sigma \cup \{\Delta\}) \times \Gamma \rightarrow$ The set of finite subset of $Q \times \Gamma^*$

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JULY						
M	T	W	T	F	S	S
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			29	30	31	

Acceptance by a PDA :-

If $M = (Q, \Sigma, \Gamma, q_0, z_0, A, \delta)$ is a PDA and $x \in \Sigma^*$, x is accepted by M if $(q_0, x, z_0) \vdash_M^* (q, \Lambda, d)$ for some $d \in \Gamma^*$ and some $q \in A$. (The stack may or may not be empty when x is accepted, because d may or may not be Λ .) A language $L \subseteq \Sigma^*$ is said to be accepted by M if L is precisely the set of strings accepted by M . In this case, we write $L = L(M)$.

Defn of DPDA :-

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10 SATURDAY
رجب ۲۲

11 SUNDAY
رجب ۲۳

Let $M = \{Q, \Sigma, \Gamma, q_0, z_0, A, \delta\}$ be a PDA. M is deterministic if there is no configuration for which M has a choice of more than one move.

A language L is DCFL, if there is a DPDA accepting L .

Union Example :-

$$0^n 1^n \cup 0^n 1^{2n} \text{ where } n \geq 1$$

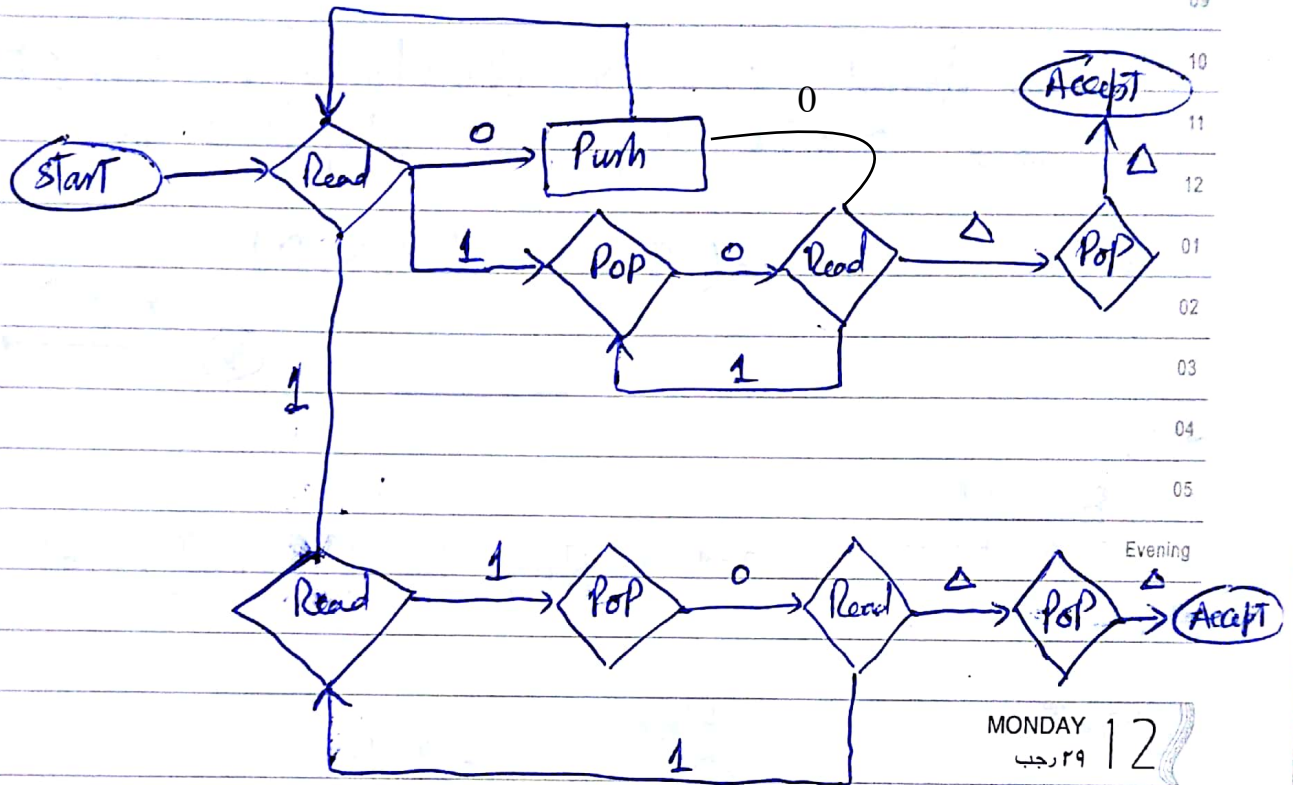
Evening

JULY

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MONDAY 12
 رجب ۲۹
 TUESDAY 13
 رجب ۳۰

H.W PDA if possible $0^n 1^n 0^n$

Defn of Turing Machine

A Turing machine (TM) is a 5-tuple $T = \{Q, \Sigma, \Gamma, q_0, \delta\}$, where

Q is a finite set of states, assumed not to contain h_a or h_r

Σ and Γ are finite sets (input and tape alphabets)

q_0 , the initial state

$\delta: Q \times (\Gamma \cup \{\Delta\}) \rightarrow (Q \cup \{h_a, h_r\}) \times (\Gamma \cup \{\Delta\}) \times \{R, L, S\}$ is a partial