

The space shuttle Discovery is carried out into space by powerful rockets. They are accelerating, increasing in speed rapidly. To do so, a force must be exerted on them according to Newton's second law, $\Sigma \vec{F} = m\vec{a}$. What exerts this force? The rocket engines exert a force on the gases they push out (expel) from the rear of the rockets (labeled \vec{F}_{GR}). According to Newton's third law, these ejected gases exert an equal and opposite force on the rockets in the forward direction. It is this "reaction" force exerted on the rockets by the gases, labeled \vec{F}_{RG} , that accelerates the rockets forward.

CHAPTER 4

Dynamics: Newton's Laws of Motion

CHAPTER-OPENING QUESTIONS—Guess now!

A 150-kg football player collides head-on with a 75-kg running back. During the collision, the heavier player exerts a force of magnitude F_A on the smaller player. If the smaller player exerts a force F_B back on the heavier player, which response is most accurate?

- (a) $F_B = F_A$.
- (b) $F_B < F_A$.
- (c) $F_B > F_A$.
- (d) $F_B = 0$.
- (e) We need more information.

Second Question:

A line by the poet T. S. Eliot (from *Murder in the Cathedral*) has the women of Canterbury say "the earth presses up against our feet." What force is this?

- (a) Gravity.
- (b) The normal force.
- (c) A friction force.
- (d) Centrifugal force.
- (e) No force—they are being poetic.

CONTENTS

- 4-1 Force
- 4-2 Newton's First Law of Motion
- 4-3 Mass
- 4-4 Newton's Second Law of Motion
- 4-5 Newton's Third Law of Motion
- 4-6 Weight—the Force of Gravity; and the Normal Force
- 4-7 Solving Problems with Newton's Laws: Free-Body Diagrams
- 4-8 Problem Solving—A General Approach

83

We have discussed how motion is described in terms of velocity and acceleration. Now we deal with the question of *why* objects move as they do: What makes an object at rest begin to move? What causes an object to accelerate or decelerate? What is involved when an object moves in a curved path? We can answer in each case that a force is required. In this Chapter¹, we will investigate the connection between force and motion, which is the subject called **dynamics**.

4-1 Force

Intuitively, we experience **force** as any kind of a push or a pull on an object. When you push a stalled car or a grocery cart (Fig. 4-1), you are exerting a force on it. When a motor lifts an elevator, or a hammer hits a nail, or the wind blows the leaves of a tree, a force is being exerted. We often call these *contact forces* because the force is exerted when one object comes in contact with another object. On the other hand, we say that an object falls because of the *force of gravity*.

If an object is at rest, to start it moving requires force—that is, a force is needed to accelerate an object from zero velocity to a nonzero velocity. For an object already moving, if you want to change its velocity—either in direction or in magnitude—a force is required. In other words, to accelerate an object, a force is always required. In Section 4-4 we discuss the precise relation between acceleration and net force, which is Newton's second law.

One way to measure the magnitude (or strength) of a force is to use a spring scale (Fig. 4-2). Normally, such a spring scale is used to find the weight of an object; by weight we mean the force of gravity acting on the object (Section 4-6). The spring scale, once calibrated, can be used to measure other kinds of forces as well, such as the pulling force shown in Fig. 4-2.

A force exerted in a different direction has a different effect. Force has direction as well as magnitude, and is indeed a vector that follows the rules of vector addition discussed in Chapter 3. We can represent any force on a diagram by an arrow, just as we did with velocity. The direction of the arrow is the direction of the push or pull, and its length is drawn proportional to the magnitude of the force.



FIGURE 4-1 A force exerted on a grocery cart—in this case exerted by a person.



FIGURE 4-2 A spring scale used to measure a force.

4-2 Newton's First Law of Motion

What is the relationship between force and motion? Aristotle (384–322 B.C.) believed that a force was required to keep an object moving along a horizontal plane. To Aristotle, the natural state of an object was at rest, and a force was believed necessary to keep an object in motion. Furthermore, Aristotle argued, the greater the force on the object, the greater its speed.

Some 2000 years later, Galileo disagreed: he maintained that it is just as natural for an object to be in motion with a constant velocity as it is for it to be at rest.

To understand Galileo's idea, consider the following observations involving motion along a horizontal plane. To push an object with a rough surface along a

¹We treat everyday objects in motion here; the treatment of the submicroscopic world of atoms and molecules, and when velocities are extremely high, close to the speed of light (3.0×10^8 m/s), are treated using quantum theory (Chapter 37 ff), and the theory of relativity (Chapter 36).

tabletop at constant speed requires a certain amount of force. To push an equally heavy object with a very smooth surface across the table at the same speed will require less force. If a layer of oil or other lubricant is placed between the surface of the object and the table, then almost no force is required to keep the object moving. Notice that in each successive step, less force is required. As the next step, we imagine that the object does not rub against the table at all—or there is a perfect lubricant between the object and the table—and theorize that once started, the object would move across the table at constant speed with *no* force applied. A steel ball bearing rolling on a hard horizontal surface approaches this situation. So does a puck on an air table, in which a thin layer of air reduces friction almost to zero.

It was Galileo's genius to imagine such an idealized world—in this case, one where there is no friction—and to see that it could lead to a more accurate and richer understanding of the real world. This idealization led him to his remarkable conclusion that if no force is applied to a moving object, it will continue to move with constant speed in a straight line. An object slows down only if a force is exerted on it. Galileo thus interpreted friction as a force akin to ordinary pushes and pulls.

To push an object across a table at constant speed requires a force from your hand that can balance out the force of friction (Fig. 4-3). When the object moves at constant speed, your pushing force is equal in magnitude to the friction force, but these two forces are in opposite directions, so the *net* force on the object (the vector sum of the two forces) is zero. This is consistent with Galileo's viewpoint, for the object moves with constant speed when no net force is exerted on it.

Upon this foundation laid by Galileo, Isaac Newton (Fig. 4-4) built his great theory of motion. Newton's analysis of motion is summarized in his famous "three laws of motion." In his great work, the *Principia* (published in 1687), Newton readily acknowledged his debt to Galileo. In fact, **Newton's first law of motion** is close to Galileo's conclusions. It states that

Every object continues in its state of rest, or of uniform velocity in a straight line, as long as no net force acts on it.

The tendency of an object to maintain its state of rest or of uniform velocity in a straight line is called **inertia**. As a result, Newton's first law is often called the **law of inertia**.

CONCEPTUAL EXAMPLE 4-1 **Newton's first law.** A school bus comes to a sudden stop, and all of the backpacks on the floor start to slide forward. What force causes them to do that?

RESPONSE It isn't "force" that does it. By Newton's first law, the backpacks continue their state of motion, maintaining their velocity. The backpacks slow down if a force is applied, such as friction with the floor.

Inertial Reference Frames

Newton's first law does not hold in every reference frame. For example, if your reference frame is fixed in an accelerating car, an object such as a cup resting on the dashboard may begin to move toward you (it stayed at rest as long as the car's velocity remained constant). The cup accelerated toward you, but neither you nor anything else exerted a force on it in that direction. Similarly, in the reference frame of the decelerating bus in Example 4-1, there was no force pushing the backpacks forward. In accelerating reference frames, Newton's first law does not hold. Reference frames in which Newton's first law does hold are called **inertial reference frames** (the law of inertia is valid in them). For most purposes, we usually make the approximation that a reference frame fixed on the Earth is an inertial frame. This is not precisely true, due to the Earth's rotation, but usually it is close enough.

Any reference frame that moves with constant velocity (say, a car or an airplane) relative to an inertial frame is also an inertial reference frame. Reference frames where the law of inertia does *not* hold, such as the accelerating reference frames discussed above, are called **noninertial** reference frames. How can we be sure a reference frame is inertial or not? By checking to see if Newton's first law holds. Thus Newton's first law serves as the definition of inertial reference frames.

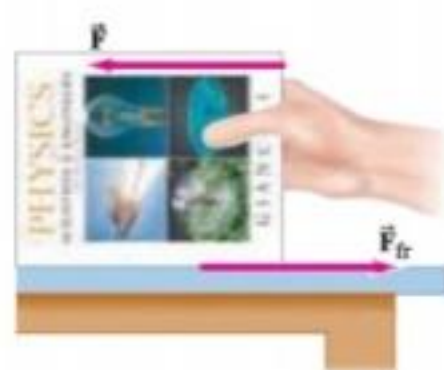


FIGURE 4-3 \vec{F} represents the force applied by the person and \vec{F}_{fr} represents the force of friction.

NEWTON'S FIRST LAW OF MOTION

FIGURE 4-4 Isaac Newton (1642–1727).



4-3 Mass

Newton's second law, which we come to in the next Section, makes use of the concept of mass. Newton used the term *mass* as a synonym for *quantity of matter*. This intuitive notion of the mass of an object is not very precise because the concept "quantity of matter" is not very well defined. More precisely, we can say that **mass** is a *measure of the inertia* of an object. The more mass an object has, the greater the force needed to give it a particular acceleration. It is harder to start it moving from rest, or to stop it when it is moving, or to change its velocity sideways out of a straight-line path. A truck has much more inertia than a baseball moving at the same speed, and a much greater force is needed to change the truck's velocity at the same rate as the ball's. The truck therefore has much more mass.

To quantify the concept of mass, we must define a standard. In SI units, the unit of mass is the **kilogram (kg)**, as we discussed in Chapter 1, Section 1-4.

The terms *mass* and *weight* are often confused with one another, but it is important to distinguish between them. Mass is a property of an object itself (a measure of an object's inertia, or its "quantity of matter"). Weight, on the other hand, is a force, the pull of gravity acting on an object. To see the difference, suppose we take an object to the Moon. The object will weigh only about one-sixth as much as it did on Earth, since the force of gravity is weaker. But its mass will be the same. It will have the same amount of matter as on Earth, and will have just as much inertia—for in the absence of friction, it will be just as hard to start it moving on the Moon as on Earth, or to stop it once it is moving. (More on weight in Section 4-6.)

CAUTION
Distinguish mass from weight

4-4 Newton's Second Law of Motion



FIGURE 4-5 The bobsled accelerates because the team exerts a force.

Newton's first law states that if no net force is acting on an object at rest, the object remains at rest; or if the object is moving, it continues moving with constant speed in a straight line. But what happens if a net force *is* exerted on an object? Newton perceived that the object's velocity will change (Fig. 4-5). A net force exerted on an object may make its velocity increase. Or, if the net force is in a direction opposite to the motion, the force will reduce the object's velocity. If the net force acts sideways on a moving object, the *direction* of the object's velocity changes (and the magnitude may as well). Since a change in velocity is an acceleration (Section 2-4), we can say that *a net force causes acceleration*.

What precisely is the relationship between acceleration and force? Everyday experience can suggest an answer. Consider the force required to push a cart when friction is small enough to ignore. (If there is friction, consider the *net* force, which is the force you exert minus the force of friction.) If you push the cart with a gentle but constant force for a certain period of time, you will make the cart accelerate from rest up to some speed, say 3 km/h. If you push with twice the force, the cart will reach 3 km/h in half the time. The acceleration will be twice as great. If you triple the force, the acceleration is tripled, and so on. Thus, the acceleration of an object is directly proportional to the net applied force. But the acceleration depends on the mass of the object as well. If you push an empty grocery cart with the same force as you push one that is filled with groceries, you will find that the full cart accelerates more slowly. The greater the mass, the less the acceleration for the same net force. The mathematical relation, as Newton argued, is that the acceleration of an object is inversely proportional to its mass. These relationships are found to hold in general and can be summarized as follows:

The acceleration of an object is directly proportional to the net force acting on it, and is inversely proportional to the object's mass. The direction of the acceleration is in the direction of the net force acting on the object.

This is **Newton's second law of motion**.

NEWTON'S SECOND LAW OF MOTION

Newton's second law can be written as an equation:

$$\vec{a} = \frac{\Sigma \vec{F}}{m}$$

where \vec{a} stands for acceleration, m for the mass, and $\Sigma \vec{F}$ for the *net force* on the object. The symbol Σ (Greek "sigma") stands for "sum of"; \vec{F} stands for force, so $\Sigma \vec{F}$ means the *vector sum of all forces* acting on the object, which we define as the **net force**.

We rearrange this equation to obtain the familiar statement of Newton's second law:

$$\Sigma \vec{F} = m\vec{a} \quad (4-1a)$$

Newton's second law relates the description of motion (acceleration) to the cause of motion (force). It is one of the most fundamental relationships in physics. From Newton's second law we can make a more precise definition of **force as an action capable of accelerating an object**.

Every force \vec{F} is a vector, with magnitude and direction. Equation 4-1a is a vector equation valid in any inertial reference frame. It can be written in component form in rectangular coordinates as

$$\Sigma F_x = ma_x, \quad \Sigma F_y = ma_y, \quad \Sigma F_z = ma_z, \quad (4-1b)$$

where

$$\vec{F} = F_x \hat{i} + F_y \hat{j} + F_z \hat{k}$$

The component of acceleration in each direction is affected only by the component of the net force in that direction.

In SI units, with the mass in kilograms, the unit of force is called the **newton (N)**. One newton, then, is the force required to impart an acceleration of 1 m/s^2 to a mass of 1 kg . Thus $1 \text{ N} = 1 \text{ kg} \cdot \text{m/s}^2$.

In cgs units, the unit of mass is the gram (g) as mentioned earlier.¹ The unit of force is the *dyn*e, which is defined as the net force needed to impart an acceleration of 1 cm/s^2 to a mass of 1 g . Thus $1 \text{ dyne} = 1 \text{ g} \cdot \text{cm/s}^2$. It is easy to show that $1 \text{ dyne} = 10^{-5} \text{ N}$.

In the British system, the unit of force is the *pound* (abbreviated lb), where $1 \text{ lb} = 4.448222 \text{ N} \approx 4.45 \text{ N}$. The unit of mass is the *slug*, which is defined as that mass which will undergo an acceleration of 1 ft/s^2 when a force of 1 lb is applied to it. Thus $1 \text{ lb} = 1 \text{ slug} \cdot \text{ft/s}^2$. Table 4-1 summarizes the units in the different systems.

It is very important that only one set of units be used in a given calculation or problem, with the SI being preferred. If the force is given in, say, newtons, and the mass in grams, then before attempting to solve for the acceleration in SI units, we must change the mass to kilograms. For example, if the force is given as 2.0 N along the x axis and the mass is 500 g , we change the latter to 0.50 kg , and the acceleration will then automatically come out in m/s^2 when Newton's second law is used:

$$a_x = \frac{\Sigma F_x}{m} = \frac{2.0 \text{ N}}{0.50 \text{ kg}} = \frac{2.0 \text{ kg} \cdot \text{m/s}^2}{0.50 \text{ kg}} = 4.0 \text{ m/s}^2$$

EXAMPLE 4-2 ESTIMATE Force to accelerate a fast car. Estimate the net force needed to accelerate (a) a 1000-kg car at $\frac{1}{2}g$; (b) a 200-g apple at the same rate.

APPROACH We use Newton's second law to find the net force needed for each object. This is an estimate (the $\frac{1}{2}$ is not said to be precise) so we round off to one significant figure.

SOLUTION (a) The car's acceleration is $a = \frac{1}{2}g = \frac{1}{2}(9.8 \text{ m/s}^2) \approx 5 \text{ m/s}^2$. We use Newton's second law to get the net force needed to achieve this acceleration:

$$\Sigma F = ma \approx (1000 \text{ kg})(5 \text{ m/s}^2) = 5000 \text{ N}$$

(If you are used to British units, to get an idea of what a 5000-N force is, you can divide by 4.45 N/lb and get a force of about 1000 lb .)

(b) For the apple, $m = 200 \text{ g} = 0.2 \text{ kg}$, so

$$\Sigma F = ma \approx (0.2 \text{ kg})(5 \text{ m/s}^2) = 1 \text{ N}$$

¹Be careful not to confuse g for gram with g for the acceleration due to gravity. The latter is always italicized (or boldface when a vector).

NEWTON'S SECOND LAW OF MOTION

TABLE 4-1
Units for Mass and Force

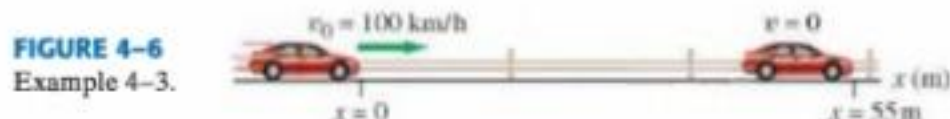
System	Mass	Force
SI	kilogram (kg)	newton (N) (= $\text{kg} \cdot \text{m/s}^2$)
cgs	gram (g)	dyne
British	slug	pound (lb)
Conversion factors: $1 \text{ dyne} = 10^{-5} \text{ N}$; $1 \text{ lb} \approx 4.45 \text{ N}$.		

PROBLEM SOLVING

Use a consistent set of units

EXAMPLE 4-3 Force to stop a car. What average net force is required to bring a 1500-kg car to rest from a speed of 100 km/h within a distance of 55 m ?

APPROACH We use Newton's second law, $\Sigma F = ma$, to determine the force, but first we need to calculate the acceleration a . We assume the acceleration is constant, so we can use the kinematic equations, Eqs. 2-12, to calculate it.



SOLUTION We assume the motion is along the $+x$ axis (Fig. 4-6). We are given the initial velocity $v_0 = 100 \text{ km/h} = 27.8 \text{ m/s}$ (Section 1-5), the final velocity $v = 0$, and the distance traveled $x - x_0 = 55 \text{ m}$. From Eq. 2-12c, we have

$$v^2 = v_0^2 + 2a(x - x_0)$$

so

$$a = \frac{v^2 - v_0^2}{2(x - x_0)} = \frac{0 - (27.8 \text{ m/s})^2}{2(55 \text{ m})} = -7.0 \text{ m/s}^2$$

The net force required is then

$$\Sigma F = ma = (1500 \text{ kg})(-7.1 \text{ m/s}^2) = -1.1 \times 10^4 \text{ N}$$

The force must be exerted in the direction *opposite* to the initial velocity, which is what the negative sign means.

NOTE If the acceleration is not precisely constant, then we are determining an "average" acceleration and we obtain an "average" net force.

Newton's second law, like the first law, is valid only in inertial reference frames (Section 4-2). In the noninertial reference frame of an accelerating car, for example, a cup on the dashboard starts sliding—it accelerates—even though the net force on it is zero; thus $\Sigma \vec{F} = m\vec{a}$ doesn't work in such an accelerating reference frame ($\Sigma \vec{F} = 0$, but $\vec{a} \neq 0$ in this noninertial frame).

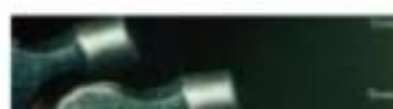
EXERCISE A Suppose you watch a cup slide on the (smooth) dashboard of an accelerating car as we just discussed, but this time from an inertial reference frame outside the car, on the street. From your inertial frame, Newton's laws are valid. What force pushes the cup off the dashboard?

Precise Definition of Mass

As mentioned in Section 4-3, we can quantify the concept of mass using its definition as a measure of inertia. How to do this is evident from Eq. 4-1a, where we see that the acceleration of an object is inversely proportional to its mass. If the same net force ΣF acts to accelerate each of two masses, m_1 and m_2 , then the ratio of their masses can be defined as the inverse ratio of their accelerations:

$$\frac{m_2}{m_1} = \frac{a_1}{a_2}$$

If one of the masses is known (it could be the standard kilogram) and the two accelerations are precisely measured, then the unknown mass is obtained from this definition. For example, if $m_1 = 1.00 \text{ kg}$, and for a particular force $a_1 = 3.00 \text{ m/s}^2$ and $a_2 = 2.00 \text{ m/s}^2$, then $m_2 = 1.50 \text{ kg}$.



4-5 Newton's Third Law of Motion

Newton's second law of motion describes quantitatively how forces affect motion. But where, we may ask, do forces come from? Observations suggest that a force exerted on any object is always exerted *by another object*. A horse pulls a wagon, a person pushes a grocery cart, a hammer pushes on a nail, a magnet attracts a paper clip. In each of these examples, a force is exerted *on* one object, and that force is exerted *by* another object. For example, the force exerted *on* the nail is exerted *by* the hammer.

But Newton realized that things are not so one-sided. True, the hammer exerts a force on the nail (Fig. 4-7). But the nail evidently exerts a force back on the hammer as well, for the hammer's speed is rapidly reduced to zero upon contact. Only a strong force could cause such a rapid deceleration of the hammer. Thus, said Newton, the two objects must be treated on an equal basis. The hammer exerts a force on the nail, and the nail exerts a force back on the hammer. This is the essence of **Newton's third law of motion**:

Whenever one object exerts a force on a second object, the second exerts an equal force in the opposite direction on the first.

This law is sometimes paraphrased as "to every action there is an equal and opposite reaction." This is perfectly valid. But to avoid confusion, it is very important to remember that the "action" force and the "reaction" force are acting on *different* objects.

As evidence for the validity of Newton's third law, look at your hand when you push against the edge of a desk, Fig. 4-8. Your hand's shape is distorted, clear evidence that a force is being exerted on it. You can *see* the edge of the desk pressing into your hand. You can even *feel* the desk exerting a force on your hand; it hurts! The harder you push against the desk, the harder the desk pushes back on your hand. (You only feel forces exerted *on* you; when you exert a force on another object, what you feel is that object pushing back on you.)

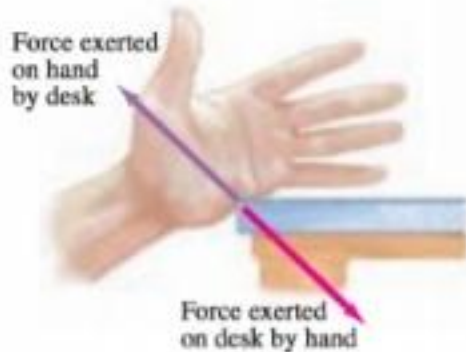


FIGURE 4-8 If your hand pushes against the edge of a desk (the force vector is shown in red), the desk pushes back against your hand (this force vector is shown in a different color, violet, to remind us that this force acts on a different object).

The force the desk exerts on your hand has the same magnitude as the force your hand exerts on the desk. This is true not only if the desk is at rest but is true even if the desk is accelerating due to the force your hand exerts.

As another demonstration of Newton's third law, consider the ice skater in Fig. 4-9. There is very little friction between her skates and the ice, so she will move freely if a force is exerted on her. She pushes against the wall; and then *she* starts moving backward. The force she exerts on the wall cannot make *her* start moving, for that force acts on the wall. Something had to exert a force *on her* to start her moving, and that force could only have been exerted by the wall. The force with which the wall pushes on her is, by Newton's third law, equal and opposite to the force she exerts on the wall.

When a person throws a package out of a small boat (initially at rest), the boat starts moving in the opposite direction. The person exerts a force on the package. The package exerts an equal and opposite force back on the person, and this force propels the person (and the boat) backward slightly.

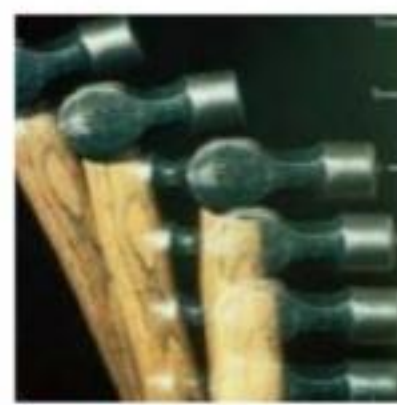


FIGURE 4-7 A hammer striking a nail. The hammer exerts a force on the nail and the nail exerts a force back on the hammer. The latter force decelerates the hammer and brings it to rest.

NEWTON'S THIRD LAW OF MOTION

CAUTION
Action and reaction forces act on different objects

109/1322

FIGURE 4-9 An example of Newton's third law: when an ice skater pushes against the wall, the wall pushes back and this force causes her to accelerate away.

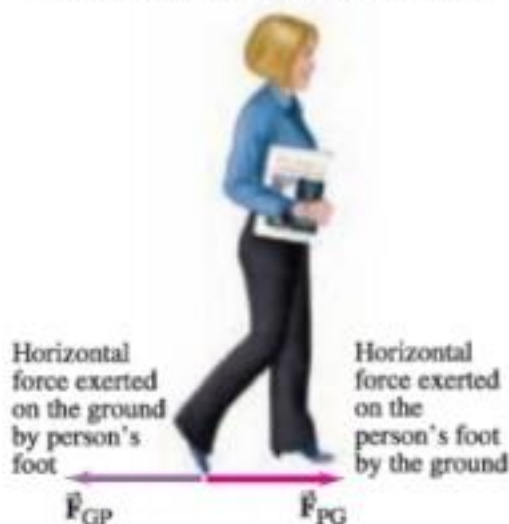


SECTION 4-5 Newton's Third Law of Motion 89



FIGURE 4-10 Another example of Newton's third law: the launch of a rocket. The rocket engine pushes the gases downward, and the gases exert an equal and opposite force upward on the rocket, accelerating it upward. (A rocket does *not* accelerate as a result of its propelling gases pushing against the ground.)

FIGURE 4-11 We can walk forward because, when one foot pushes backward against the ground, the ground pushes forward on that foot (Newton's third law). The two forces shown *act on different objects*.



NEWTON'S THIRD LAW OF MOTION

$$\vec{F}_{GP} = -\vec{F}_{PG} \quad (4-2)$$

\vec{F}_{GP} and \vec{F}_{PG} have the same magnitude (Newton's third law), and the minus sign reminds us that these two forces are in opposite directions.

Note carefully that the two forces shown in Fig. 4-11 act on different objects—hence we used slightly different colors for the vector arrows representing these forces. These two forces would never appear together in a sum of forces in Newton's second law, $\Sigma \vec{F} = m\vec{a}$. Why not? Because they act on different objects: \vec{a} is the acceleration of one particular object, and $\Sigma \vec{F}$ must include *only* the forces on that *one* object.

Rocket propulsion also is explained using Newton's third law (Fig. 4-10). A common misconception is that rockets accelerate because the gases rushing out the back of the engine push against the ground or the atmosphere. Not true. What happens, instead, is that a rocket exerts a strong force on the gases, expelling them; and the gases exert an equal and opposite force *on the rocket*. It is this latter force that propels the rocket forward—the force exerted *on the rocket* by the gases (see Chapter-Opening photo, page 83). Thus, a space vehicle is maneuvered in empty space by firing its rockets in the direction opposite to that in which it needs to accelerate. When the rocket pushes on the gases in one direction, the gases push back on the rocket in the opposite direction. Jet aircraft too accelerate because the gases they thrust out backwards exert a forward force on the engines (Newton's third law).

Consider how we walk. A person begins walking by pushing with the foot backward against the ground. The ground then exerts an equal and opposite force forward on the person (Fig. 4-11), and it is this force, *on the person*, that moves the person forward. (If you doubt this, try walking normally where there is no friction, such as on very smooth slippery ice.) In a similar way, a bird flies forward by exerting a backward force on the air, but it is the air pushing forward (Newton's third law) on the bird's wings that propels the bird forward.

CONCEPTUAL EXAMPLE 4-4 What exerts the force to move a car? What makes a car go forward?

RESPONSE A common answer is that the engine makes the car move forward. But it is not so simple. The engine makes the wheels go around. But if the tires are on slick ice or deep mud, they just spin. Friction is needed. On firm ground, the tires push backward against the ground because of friction. By Newton's third law, the ground pushes on the tires in the opposite direction, accelerating the car forward.

We tend to associate forces with active objects such as humans, animals, engines, or a moving object like a hammer. It is often difficult to see how an inanimate object at rest, such as a wall or a desk, or the wall of an ice rink (Fig. 4-9), can exert a force. The explanation is that every material, no matter how hard, is elastic (springy) at least to some degree. A stretched rubber band can exert a force on a wad of paper and accelerate it to fly across the room. Other materials may not stretch as readily as rubber, but they do stretch or compress when a force is applied to them. And just as a stretched rubber band exerts a force, so does a stretched (or compressed) wall, desk, or car fender.

From the examples discussed above, we can see how important it is to remember *on* what object a given force is exerted and *by* what object that force is exerted. A force influences the motion of an object only when it is applied *on* that object. A force exerted *by* an object does not influence that same object; it only influences the other object *on* which it is exerted. Thus, to avoid confusion, the two prepositions *on* and *by* must always be used—and used with care.

One way to keep clear which force acts on which object is to use double subscripts. For example, the force exerted on the **P**erson by the **G**round as the person walks in Fig. 4-11 can be labeled \vec{F}_{PG} . And the force exerted on the ground by the person is \vec{F}_{GP} . By Newton's third law

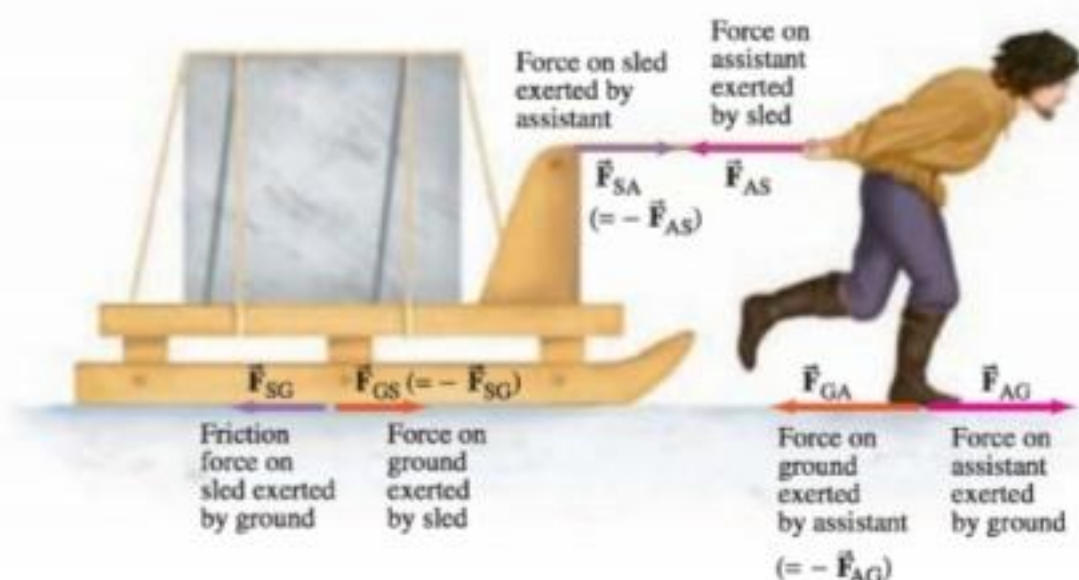


FIGURE 4-12 Example 4-5, showing only horizontal forces. Michelangelo has selected a fine block of marble for his next sculpture. Shown here is his assistant pulling it on a sled away from the quarry. Forces on the assistant are shown as red (magenta) arrows. Forces on the sled are purple arrows. Forces acting on the ground are orange arrows. Action–reaction forces that are equal and opposite are labeled by the same subscripts but reversed (such as \vec{F}_{GA} and \vec{F}_{AG}) and are of different colors because they act on different objects.

CONCEPTUAL EXAMPLE 4-5 Third law clarification. Michelangelo's assistant has been assigned the task of moving a block of marble using a sled (Fig. 4-12). He says to his boss, "When I exert a forward force on the sled, the sled exerts an equal and opposite force backward. So how can I ever start it moving? No matter how hard I pull, the backward reaction force always equals my forward force, so the net force must be zero. I'll never be able to move this load." Is he correct?

RESPONSE No. Although it is true that the action and reaction forces are equal in magnitude, the assistant has forgotten that they are exerted on different objects. The forward ("action") force is exerted by the assistant on the sled (Fig. 4-12), whereas the backward "reaction" force is exerted by the sled on the assistant. To determine if the assistant moves or not, we must consider only the forces on the assistant and then apply $\Sigma \vec{F} = m\vec{a}$, where $\Sigma \vec{F}$ is the net force on the assistant, \vec{a} is the acceleration of the assistant, and m is the assistant's mass. There are two forces on the assistant that affect his forward motion; they are shown as bright red (magenta) arrows in Figs. 4-12 and 4-13: they are (1) the horizontal force \vec{F}_{AG} exerted on the assistant by the ground (the harder he pushes backward against the ground, the harder the ground pushes forward on him—Newton's third law), and (2) the force \vec{F}_{AS} exerted on the assistant by the sled, pulling backward on him; see Fig. 4-13. If he pushes hard enough on the ground, the force on him exerted by the ground, \vec{F}_{AG} , will be larger than the sled pulling back, \vec{F}_{AS} , and the assistant accelerates forward (Newton's second law). The sled, on the other hand, accelerates forward when the force on it exerted by the assistant is greater than the frictional force exerted backward on it by the ground (that is, when \vec{F}_{SA} has greater magnitude than \vec{F}_{SG} in Fig. 4-12).

Using double subscripts to clarify Newton's third law can become cumbersome, and we won't usually use them in this way. We will usually use a single subscript referring to what exerts the force on the object being discussed. Nevertheless, if there is any confusion in your mind about a given force, go ahead and use two subscripts to identify *on* what object and *by* what object the force is exerted.

EXERCISE B Return to the first Chapter-Opening Question, page 83, and answer it again now. Try to explain why you may have answered differently the first time.

EXERCISE C A massive truck collides head-on with a small sports car. (a) Which vehicle experiences the greater force of impact? (b) Which experiences the greater acceleration during the impact? (c) Which of Newton's laws are useful to obtain the correct answers?

EXERCISE D If you push on a heavy desk, does it always push back on you? (a) Not unless someone else also pushes on it. (b) Yes, if it is out in space. (c) A desk never pushes to start with. (d) No. (e) Yes.

PROBLEM SOLVING
111/1322

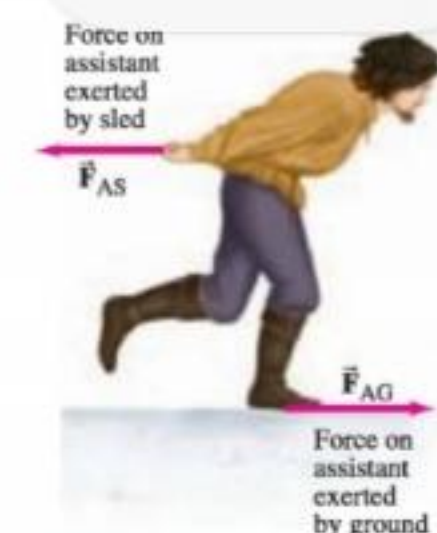


FIGURE 4-13 Example 4-5. The horizontal forces on the assistant.

4-6 Weight—the Force of Gravity; and the Normal Force

As we saw in Chapter 2, Galileo claimed that all objects dropped near the surface of the Earth would fall with the same acceleration, \vec{g} , if air resistance was negligible. The force that causes this acceleration is called the *force of gravity* or *gravitational force*. What exerts the gravitational force on an object? It is the Earth, as we will discuss in Chapter 6, and the force acts vertically¹ downward, toward the center of the Earth. Let us apply Newton's second law to an object of mass m falling freely due to gravity. For the acceleration, \vec{a} , we use the downward acceleration due to gravity, \vec{g} . Thus, the **gravitational force** on an object, \vec{F}_G , can be written as

$$\vec{F}_G = m\vec{g}. \quad (4-3)$$

The direction of this force is down toward the center of the Earth. The magnitude of the force of gravity on an object, mg , is commonly called the object's **weight**.

In SI units, $g = 9.80 \text{ m/s}^2 = 9.80 \text{ N/kg}$,² so the weight of a 1.00-kg mass on Earth is $1.00 \text{ kg} \times 9.80 \text{ m/s}^2 = 9.80 \text{ N}$. We will mainly be concerned with the weight of objects on Earth, but we note that on the Moon, on other planets, or in space, the weight of a given mass will be different than it is on Earth. For example, on the Moon the acceleration due to gravity is about one-sixth what it is on Earth, and a 1.0-kg mass weighs only 1.6 N. Although we will not use British units, we note that for practical purposes on the Earth, a mass of 1 kg weighs about 2.2 lb. (On the Moon, 1 kg weighs only about 0.4 lb.)

The force of gravity acts on an object when it is falling. When an object is at rest on the Earth, the gravitational force on it does not disappear, as we know if we weigh it on a spring scale. The same force, given by Eq. 4-3, continues to act. Why, then, doesn't the object move? From Newton's second law, the net force on an object that remains at rest is zero. There must be another force on the object to balance the gravitational force. For an object resting on a table, the table exerts this upward force; see Fig. 4-14a. The table is compressed slightly beneath the object, and due to its elasticity, it pushes up on the object as shown. The force exerted by the table is often called a **contact force**, since it occurs when two objects are in contact. (The force of your hand pushing on a cart is also a contact force.) When a contact force acts *perpendicular* to the common surface of contact, it is referred to as the **normal force** ("normal" means perpendicular); hence it is labeled \vec{F}_N in Fig. 4-14a.

The two forces shown in Fig. 4-14a are both acting on the statue, which remains at rest, so the vector sum of these two forces must be zero (Newton's second law). Hence \vec{F}_G and \vec{F}_N must be of equal magnitude and in opposite directions. But they are *not* the equal and opposite forces spoken of in Newton's third law. The action and reaction forces of Newton's third law act on *different objects*, whereas the two forces shown in Fig. 4-14a act on the *same* object. For each of the forces shown in Fig. 4-14a, we can ask, "What is the reaction force?" The upward force, \vec{F}_N , on the statue is exerted by the table. The reaction to this force is a force exerted by the statue downward on the table. It is shown in Fig. 4-14b, where it is labeled \vec{F}'_N . This force, \vec{F}'_N , exerted on the table by the statue, is the reaction force to \vec{F}_N in accord with Newton's third law. What about the other force on the statue, the force of gravity \vec{F}_G exerted by the Earth? Can you guess what the reaction is to this force? We will see in Chapter 6 that the reaction force is also a gravitational force, exerted on the Earth by the statue.

EXERCISE E Return to the second Chapter-Opening Question, page 83, and answer it again now. Try to explain why you may have answered differently the first time.

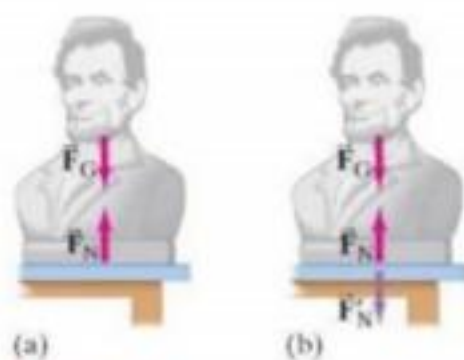


FIGURE 4-14 (a) The net force on an object at rest is zero according to Newton's second law. Therefore the downward force of gravity (\vec{F}_G) on an object at rest must be balanced by an upward force (the normal force \vec{F}_N) exerted by the table in this case. (b) \vec{F}'_N is the force exerted on the table by the statue and is the reaction force to \vec{F}_N by Newton's third law. (\vec{F}'_N is shown in a different color to remind us it acts on a different object.) The reaction force to \vec{F}_G is not shown.

CAUTION
Weight and normal force are *not* action–reaction pairs

¹The concept of "vertical" is tied to gravity. The best definition of *vertical* is that it is the direction in which objects fall. A surface that is "horizontal," on the other hand, is a surface on which a round object won't start rolling; gravity has no effect. Horizontal is perpendicular to vertical.

²Since $1 \text{ N} = 1 \text{ kg} \cdot \text{m/s}^2$ (Section 4-4), then $1 \text{ m/s}^2 = 1 \text{ N/kg}$.

EXAMPLE 4-6 Weight, normal force, and a box. A friend has given you a special gift, a box of mass 10.0 kg with a mystery surprise inside. The box is resting on the smooth (frictionless) horizontal surface of a table (Fig. 4-15a). (a) Determine the weight of the box and the normal force exerted on it by the table. (b) Now your friend pushes down on the box with a force of 40.0 N, as in Fig. 4-15b. Again determine the normal force exerted on the box by the table. (c) If your friend pulls upward on the box with a force of 40.0 N (Fig. 4-15c), what now is the normal force exerted on the box by the table?

APPROACH The box is at rest on the table, so the net force on the box in each case is zero (Newton's second law). The weight of the box has magnitude mg in all three cases.

SOLUTION (a) The weight of the box is $mg = (10.0 \text{ kg})(9.80 \text{ m/s}^2) = 98.0 \text{ N}$, and this force acts downward. The only other force on the box is the normal force exerted upward on it by the table, as shown in Fig. 4-15a. We chose the upward direction as the positive y direction; then the net force ΣF_y on the box is $\Sigma F_y = F_N - mg$; the minus sign means mg acts in the negative y direction (m and g are magnitudes). The box is at rest, so the net force on it must be zero (Newton's second law, $\Sigma F_y = ma_y$, and $a_y = 0$). Thus

$$\begin{aligned}\Sigma F_y &= ma_y \\ F_N - mg &= 0,\end{aligned}$$

so we have

$$F_N = mg.$$

The normal force on the box, exerted by the table, is 98.0 N upward, and has magnitude equal to the box's weight.

(b) Your friend is pushing down on the box with a force of 40.0 N. So instead of only two forces acting on the box, now there are three forces acting on the box, as shown in Fig. 4-15b. The weight of the box is still $mg = 98.0 \text{ N}$. The net force is $\Sigma F_y = F_N - mg - 40.0 \text{ N}$, and is equal to zero because the box remains at rest ($a = 0$). Newton's second law gives

$$\Sigma F_y = F_N - mg - 40.0 \text{ N} = 0.$$

We solve this equation for the normal force:

$$F_N = mg + 40.0 \text{ N} = 98.0 \text{ N} + 40.0 \text{ N} = 138.0 \text{ N},$$

which is greater than in (a). The table pushes back with more force when a person pushes down on the box. The normal force is not always equal to the weight!

(c) The box's weight is still 98.0 N and acts downward. The force exerted by your friend and the normal force both act upward (positive direction), as shown in Fig. 4-15c. The box doesn't move since your friend's upward force is less than the weight. The net force, again set to zero in Newton's second law because $a = 0$, is

$$\Sigma F_y = F_N - mg + 40.0 \text{ N} = 0,$$

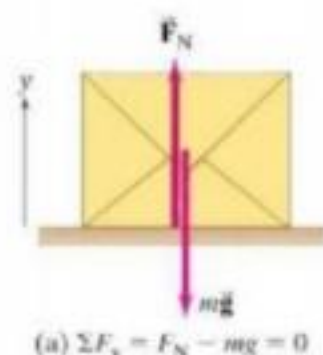
so

$$F_N = mg - 40.0 \text{ N} = 98.0 \text{ N} - 40.0 \text{ N} = 58.0 \text{ N}.$$

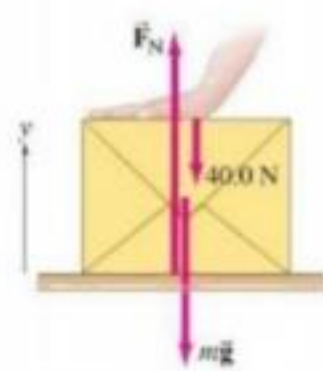
The table does not push against the full weight of the box because of the upward pull exerted by your friend.

NOTE The weight of the box ($= mg$) does not change as a result of your friend's push or pull. Only the normal force is affected.

Recall that the normal force is elastic in origin (the table in Fig. 4-15 sags slightly under the weight of the box). The normal force in Example 4-6 is vertical, perpendicular to the horizontal table. The normal force is not always vertical, however. When you push against a wall, for example, the normal force with which the wall pushes back on you is horizontal (Fig. 4-9). For an object on a plane inclined at an angle to the horizontal, such as a skier or car on a hill, the normal force acts perpendicular to the plane and so is not vertical.



$$(a) \Sigma F_y = F_N - mg = 0$$



$$(b) \Sigma F_y = F_N - mg - 40.0 \text{ N} = 0$$



$$(c) \Sigma F_y = F_N - mg + 40.0 \text{ N} = 0$$

FIGURE 4-15 Example 4-6. (a) A 10-kg gift box is at rest on a table. (b) A person pushes down on the box with a force of 40.0 N. (c) A person pulls upward on the box with a force of 40.0 N. The forces are all assumed to act along a line; they are shown slightly displaced in order to be distinguishable. Only forces acting on the box are shown.

CAUTION
The normal force is not always equal to the weight

CAUTION
The normal force, \vec{F}_N , is not necessarily vertical

SECTION 4-6 Weight—the Force of Gravity; and the Normal Force 93

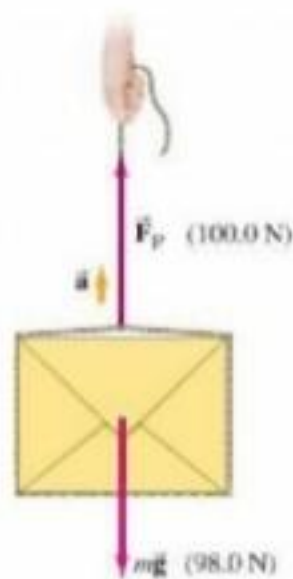


FIGURE 4-16 Example 4-7. The box accelerates upward because $F_P > mg$.

EXAMPLE 4-7 Accelerating the box. What happens when a person pulls upward on the box in Example 4-6c with a force equal to, or greater than, the box's weight? For example, let $F_P = 100.0 \text{ N}$ (Fig. 4-16) rather than the 40.0 N shown in Fig. 4-15c.

APPROACH We can start just as in Example 4-6, but be ready for a surprise.

SOLUTION The net force on the box is

$$\begin{aligned}\Sigma F_y &= F_N - mg + F_P \\ &= F_N - 98.0 \text{ N} + 100.0 \text{ N},\end{aligned}$$

and if we set this equal to zero (thinking the acceleration might be zero), we would get $F_N = -2.0 \text{ N}$. This is nonsense, since the negative sign implies F_N points downward, and the table surely cannot pull down on the box (unless there's glue on the table). The least F_N can be is zero, which it will be in this case. What really happens here is that the box accelerates upward because the net force is not zero. The net force (setting the normal force $F_N = 0$) is

$$\begin{aligned}\Sigma F_y &= F_P - mg = 100.0 \text{ N} - 98.0 \text{ N} \\ &= 2.0 \text{ N}\end{aligned}$$

upward. See Fig. 4-16. We apply Newton's second law and see that the box moves upward with an acceleration

$$\begin{aligned}a_y &= \frac{\Sigma F_y}{m} = \frac{2.0 \text{ N}}{10.0 \text{ kg}} \\ &= 0.20 \text{ m/s}^2.\end{aligned}$$

FIGURE 4-17 Example 4-8. The acceleration vector is shown in gold to distinguish it from the red force vectors.



EXAMPLE 4-8 Apparent weight loss. A 65-kg woman descends in an elevator that briefly accelerates at $0.20g$ downward. She stands on a scale that reads in kg. (a) During this acceleration, what is her weight and what does the scale read? (b) What does the scale read when the elevator descends at a constant speed of 2.0 m/s ?

APPROACH Figure 4-17 shows all the forces that act on the woman (and only those that act on her). The direction of the acceleration is downward, so we choose the positive direction as down (this is the opposite choice from Examples 4-6 and 4-7).

SOLUTION (a) From Newton's second law,

$$\begin{aligned}\Sigma F &= ma \\ mg - F_N &= m(0.20g).\end{aligned}$$

We solve for F_N :

$$F_N = mg - 0.20mg = 0.80mg,$$

and it acts upward. The normal force \vec{F}_N is the force the scale exerts on the person, and is equal and opposite to the force she exerts on the scale: $F_N = 0.80mg$ downward. Her weight (force of gravity on her) is still $mg = (65 \text{ kg})(9.8 \text{ m/s}^2) = 640 \text{ N}$. But the scale, needing to exert a force of only $0.80mg$, will give a reading of $0.80m = 52 \text{ kg}$.

(b) Now there is no acceleration, $a = 0$, so by Newton's second law, $mg - F_N = 0$ and $F_N = mg$. The scale reads her true mass of 65 kg.

NOTE The scale in (a) may give a reading of 52 kg (as an "apparent mass"), but her mass doesn't change as a result of the acceleration: it stays at 65 kg.

4-7 Solving Problems with Newton's Laws: Free-Body Diagrams

Newton's second law tells us that the acceleration of an object is proportional to the **net force** acting on the object. The **net force**, as mentioned earlier, is the **vector sum** of all forces acting on the object. Indeed, extensive experiments have shown that forces do add together as vectors precisely according to the rules we developed in Chapter 3. For example, in Fig. 4-18, two forces of equal magnitude (100 N each) are shown acting on an object at right angles to each other. Intuitively, we can see that the object will start moving at a 45° angle and thus the net force acts at a 45° angle. This is just what the rules of vector addition give. From the **theorem** of Pythagoras, the magnitude of the resultant force is $F_R = \sqrt{(100\text{ N})^2 + (100\text{ N})^2} = 141\text{ N}$.

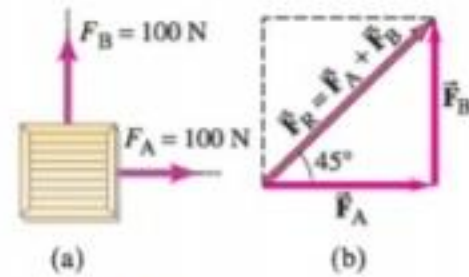


FIGURE 4-18 (a) Two forces, \vec{F}_A and \vec{F}_B , exerted by workers A and B, act on a crate. (b) The sum, or resultant, of \vec{F}_A and \vec{F}_B is \vec{F}_R .

EXAMPLE 4-9 Adding force vectors. Calculate the sum of the two forces exerted on the boat by workers A and B in Fig. 4-19a.

APPROACH We add force vectors like any other vectors as described in Chapter 3. The first step is to choose an xy coordinate system (see Fig. 4-19a), and then resolve vectors into their components.

SOLUTION The two force vectors are shown resolved into components in Fig. 4-19b. We add the forces using the method of components. The components of \vec{F}_A are

$$F_{Ax} = F_A \cos 45.0^\circ = (40.0\text{ N})(0.707) = 28.3\text{ N},$$

$$F_{Ay} = F_A \sin 45.0^\circ = (40.0\text{ N})(0.707) = 28.3\text{ N}.$$

The components of \vec{F}_B are

$$F_{Bx} = +F_B \cos 37.0^\circ = +(30.0\text{ N})(0.799) = +24.0\text{ N},$$

$$F_{By} = -F_B \sin 37.0^\circ = -(30.0\text{ N})(0.602) = -18.1\text{ N}.$$

F_{By} is negative because it points along the negative y axis. The components of the resultant force are (see Fig. 4-19c)

$$F_{Rx} = F_{Ax} + F_{Bx} = 28.3\text{ N} + 24.0\text{ N} = 52.3\text{ N},$$

$$F_{Ry} = F_{Ay} + F_{By} = 28.3\text{ N} - 18.1\text{ N} = 10.2\text{ N}.$$

To find the magnitude of the resultant force, we use the Pythagorean theorem

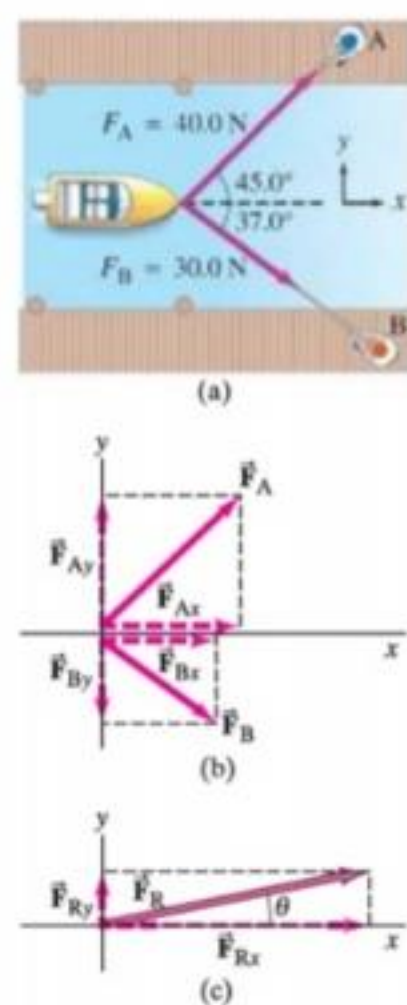
$$F_R = \sqrt{F_{Rx}^2 + F_{Ry}^2} = \sqrt{(52.3)^2 + (10.2)^2}\text{ N} = 53.3\text{ N}.$$

The only remaining question is the angle θ that the net force \vec{F}_R makes with the x axis. We use:

$$\tan \theta = \frac{F_{Ry}}{F_{Rx}} = \frac{10.2\text{ N}}{52.3\text{ N}} = 0.195,$$

and $\tan^{-1}(0.195) = 11.0^\circ$. The net force on the boat has magnitude 53.3 N and acts at an 11.0° angle to the x axis.

FIGURE 4-19 Example 4-9: Two force vectors act on a boat.



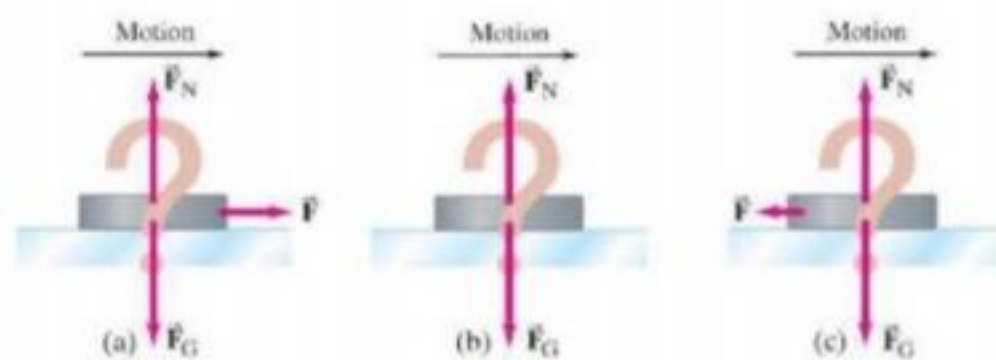
When solving problems involving Newton's laws and force, it is very important to draw a diagram showing all the forces acting *on* each object involved. Such a diagram is called a **free-body diagram**, or **force diagram**: choose one object, and draw an arrow to represent each force acting on it. Include *every* force acting on that object. Do not show forces that the chosen object exerts on *other* objects. To help you identify each and every force that is exerted on your chosen object, ask yourself what other objects could exert a force on it. If your problem involves more than one object, a separate free-body diagram is needed for each object. For now, the likely forces that could be acting are *gravity* and *contact forces* (one object pushing or pulling another, normal force, friction). Later we will consider air resistance, drag, buoyancy, pressure, as well as electric and magnetic forces.

PROBLEM SOLVING

Free-body diagram

SECTION 4-7 Solving Problems with Newton's Laws: Free-Body Diagrams 95

FIGURE 4-20 Example 4-10. Which is the correct free-body diagram for a hockey puck sliding across frictionless ice?



CONCEPTUAL EXAMPLE 4-10 The hockey puck. A hockey puck is sliding at constant velocity across a flat horizontal ice surface that is assumed to be frictionless. Which of the sketches in Fig. 4-20 is the correct free-body diagram for this puck? What would your answer be if the puck slowed down?

RESPONSE Did you choose (a)? If so, can you answer the question: what exerts the horizontal force labeled \vec{F} on the puck? If you say that it is the force needed to maintain the motion, ask yourself: what exerts this force? Remember that another object must exert any force—and there simply isn't any possibility here. Therefore, (a) is wrong. Besides, the force \vec{F} in Fig. 4-20a would give rise to an acceleration by Newton's second law. It is (b) that is correct. No net force acts on the puck, and the puck slides at constant velocity across the ice.

In the real world, where even smooth ice exerts at least a tiny friction force, then (c) is the correct answer. The tiny friction force is in the direction opposite to the motion, and the puck's velocity decreases, even if very slowly.

Here now is a brief summary of how to approach solving problems involving Newton's laws.

PROBLEM SOLVING

Newton's Laws; Free-Body Diagrams

1. Draw a sketch of the situation.
2. Consider only one object (at a time), and draw a **free-body diagram** for that object, showing *all* the forces acting *on* that object. Include any unknown forces that you have to solve for. Do not show any forces that the chosen object exerts on other objects. Draw the arrow for each force vector reasonably accurately for direction and magnitude. Label each force acting on the object, including forces you must solve for, as to its source (gravity, person, friction, and so on). If several objects are involved, draw a free-body diagram for each object *separately*, showing all the forces acting *on that object* (and *only* forces acting on that

- object). For each (and every) force, you must be clear about: *on* what object that force acts, and *by* what object that force is exerted. Only forces acting *on* a given object can be included in $\Sigma \vec{F} = m\vec{a}$ for that object.
3. Newton's second law involves vectors, and it is usually important to **resolve vectors** into components. Choose x and y axes in a way that simplifies the calculation. For example, it often saves work if you choose one coordinate axis to be in the direction of the acceleration.
4. For each object, **apply Newton's second law** to the x and y components separately. That is, the x component of the net force on that object is related to the x component of that object's acceleration: $\Sigma F_x = ma_x$, and similarly for the y direction.
5. **Solve** the equation or equations for the unknown(s).

This Problem Solving Strategy should not be considered a prescription. Rather it is a summary of things to do that will start you thinking and getting involved in the problem at hand.

When we are concerned only about translational motion, all the forces on a given object can be drawn as acting at the center of the object, thus treating the object as a **point particle**. However, for problems involving rotation or statics, the place *where* each force acts is also important, as we shall see in Chapters 10, 11, and 12.

In the Examples that follow, we assume that all surfaces are very smooth so that friction can be ignored. (Friction, and Examples using it, are discussed in Chapter 5).

CAUTION
Treating an object as a particle

EXAMPLE 4-11 Pulling the mystery box. Suppose a friend asks to examine the 10.0-kg box you were given (Example 4-6, Fig. 4-15), hoping to guess what is inside; and you respond, "Sure, pull the box over to you." She then pulls the box by the attached cord, as shown in Fig. 4-21a, along the smooth surface of the table. The magnitude of the force exerted by the person is $F_P = 40.0\text{ N}$, and it is exerted at a 30.0° angle as shown. Calculate (a) the acceleration of the box, and (b) the magnitude of the upward force F_N exerted by the table on the box. Assume that friction can be neglected.

APPROACH We follow the Problem Solving Strategy on the previous page.

SOLUTION

1. **Draw a sketch:** The situation is shown in Fig. 4-21a; it shows the box and the force applied by the person, F_P .

2. **Free-body diagram:** Figure 4-21b shows the free-body diagram of the box. To draw it correctly, we show *all* the forces acting on the box and *only* the forces acting on the box. They are: the force of gravity $m\vec{g}$; the normal force exerted by the table \vec{F}_N ; and the force exerted by the person \vec{F}_P . We are interested only in translational motion, so we can show the three forces acting at a point, Fig. 4-21c.

3. **Choose axes and resolve vectors:** We expect the motion to be horizontal, so we choose the x axis horizontal and the y axis vertical. The pull of 40.0 N has components

$$F_{Px} = (40.0\text{ N})(\cos 30.0^\circ) = (40.0\text{ N})(0.866) = 34.6\text{ N},$$

$$F_{Py} = (40.0\text{ N})(\sin 30.0^\circ) = (40.0\text{ N})(0.500) = 20.0\text{ N}.$$

In the horizontal (x) direction, \vec{F}_N and $m\vec{g}$ have zero components. Thus the horizontal component of the net force is F_{Px} .

4. (a) **Apply Newton's second law** to determine the x component of the acceleration:

$$F_{Px} = ma_x.$$

5. (a) **Solve:**

$$a_x = \frac{F_{Px}}{m} = \frac{(34.6\text{ N})}{(10.0\text{ kg})} = 3.46\text{ m/s}^2.$$

The acceleration of the box is 3.46 m/s^2 to the right.

(b) Next we want to find F_N .

4. (b) **Apply Newton's second law** to the vertical (y) direction, with upward as positive:

$$\Sigma F_y = ma_y$$

$$F_N - mg + F_{Py} = ma_y.$$

5. (b) **Solve:** We have $mg = (10.0\text{ kg})(9.80\text{ m/s}^2) = 98.0\text{ N}$ and, from point 3 above, $F_{Py} = 20.0\text{ N}$. Furthermore, since $F_{Py} < mg$, the box does not move vertically, so $a_y = 0$. Thus

$$F_N - 98.0\text{ N} + 20.0\text{ N} = 0,$$

so

$$F_N = 78.0\text{ N}.$$

NOTE F_N is less than mg : the table does not push against the full weight of the box because part of the pull exerted by the person is in the upward direction.

EXERCISE F A 10.0-kg box is dragged on a horizontal frictionless surface by a horizontal force of 10.0 N. If the applied force is doubled, the normal force on the box will (a) increase; (b) remain the same; (c) decrease.

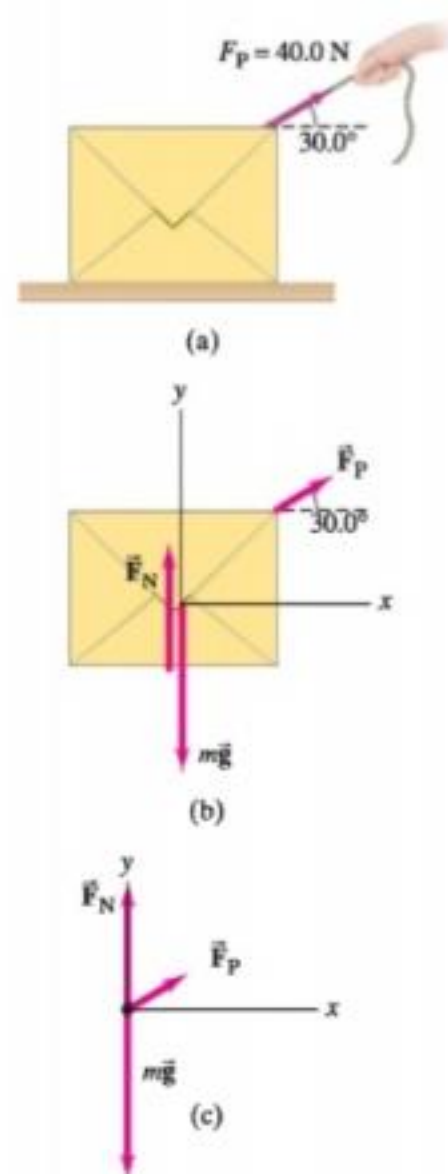


FIGURE 4-21 (a) Pulling the box, Example 4-11; (b) is the free-body diagram for the box, and (c) is the free-body diagram considering all the forces to act at a point (translational motion only, which is what we have here).

Tension in a Flexible Cord

When a flexible cord pulls on an object, the cord is said to be under **tension**, and the force it exerts on the object is the tension F_T . If the cord has negligible mass, the force exerted at one end is transmitted undiminished to each adjacent piece of cord along the entire length to the other end. Why? Because $\Sigma \vec{F} = m\vec{a} = 0$ for the cord if the cord's mass m is zero (or negligible) no matter what \vec{a} is. Hence the forces pulling on the cord at its two ends must add up to zero (F_T and $-F_T$). Note that flexible cords and strings can only pull. They can't push because they bend.

PROBLEM SOLVING
Cords can pull but can't push; tension exists throughout a cord.

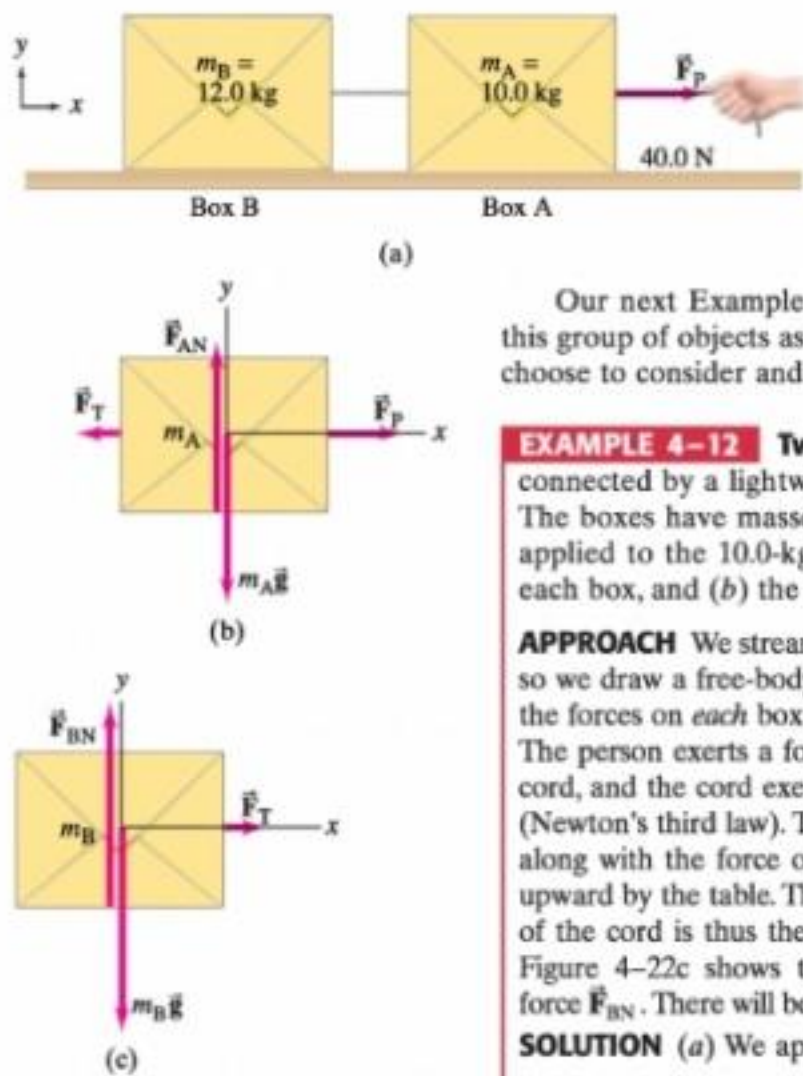


FIGURE 4-22 Example 4-12. (a) Two boxes, A and B, are connected by a cord. A person pulls horizontally on box A with force $F_P = 40.0\text{ N}$. (b) Free-body diagram for box A. (c) Free-body diagram for box B.

Our next Example involves two boxes connected by a cord. We can refer to this group of objects as a **system**. A **system** is any group of one or more objects we choose to consider and study.

EXAMPLE 4-12 Two boxes connected by a cord. Two boxes, A and B, are connected by a lightweight cord and are resting on a smooth (frictionless) table. The boxes have masses of 12.0 kg and 10.0 kg. A horizontal force F_P of 40.0 N is applied to the 10.0-kg box, as shown in Fig. 4-22a. Find (a) the acceleration of each box, and (b) the tension in the cord connecting the boxes.

APPROACH We streamline our approach by not listing each step. We have two boxes so we draw a free-body diagram for each. To draw them correctly, we must consider the forces on *each* box by itself, so that Newton's second law can be applied to each. The person exerts a force F_P on box A. Box A exerts a force F_T on the connecting cord, and the cord exerts an opposite but equal magnitude force F_T back on box A (Newton's third law). These two horizontal forces on box A are shown in Fig. 4-22b, along with the force of gravity $m_A\vec{g}$ downward and the normal force \vec{F}_{AN} exerted upward by the table. The cord is light, so we neglect its mass. The tension at each end of the cord is thus the same. Hence the cord exerts a force F_T on the second box. Figure 4-22c shows the forces on box B, which are \vec{F}_T , $m_B\vec{g}$, and the normal force \vec{F}_{BN} . There will be only horizontal motion. We take the positive x axis to the right.

SOLUTION (a) We apply $\Sigma F_x = ma_x$ to box A:

$$\Sigma F_x = F_P - F_T = m_A a_A. \quad \text{[box A]}$$

For box B, the only horizontal force is F_T , so

$$\Sigma F_x = F_T = m_B a_B. \quad \text{[box B]}$$

The boxes are connected, and if the cord remains taut and doesn't stretch, then the two boxes will have the same acceleration a . Thus $a_A = a_B = a$. We are given $m_A = 10.0\text{ kg}$ and $m_B = 12.0\text{ kg}$. We can add the two equations above to eliminate an unknown (F_T) and obtain

$$(m_A + m_B)a = F_P - F_T + F_T = F_P$$

or

$$a = \frac{F_P}{m_A + m_B} = \frac{40.0\text{ N}}{22.0\text{ kg}} = 1.82\text{ m/s}^2.$$

This is what we sought.

Alternate Solution We would have obtained the same result had we considered a single system, of mass $m_A + m_B$, acted on by a net horizontal force equal to F_P . (The tension forces F_T would then be considered internal to the system as a whole, and summed together would make zero contribution to the net force on the *whole* system.)

(b) From the equation above for box B ($F_T = m_B a_B$), the tension in the cord is

$$F_T = m_B a = (12.0\text{ kg})(1.82\text{ m/s}^2) = 21.8\text{ N}.$$

Thus, F_T is less than $F_P (= 40.0\text{ N})$, as we expect, since F_T acts to accelerate only m_B .

NOTE It might be tempting to say that the force the person exerts, F_P , acts not only on box A but also on box B. It doesn't. F_P acts only on box A. It affects box B via the tension in the cord, F_T , which acts on box B and accelerates it.

CAUTION
For any object, use only the forces on that object in calculating $\Sigma F = ma$

EXAMPLE 4-13 Elevator and counterweight (Atwood's machine). A system of two objects suspended over a pulley by a flexible cable, as shown in Fig. 4-23a, is sometimes referred to as an *Atwood's machine*. Consider the real-life application of an elevator (m_E) and its counterweight (m_C). To minimize the work done by the motor to raise and lower the elevator safely, m_E and m_C are made similar in mass. We leave the motor out of the system for this calculation, and assume that the cable's mass is negligible and that the mass of the pulley, as well as any friction, is small and ignorable. These assumptions ensure that the tension F_T in the cable has the same magnitude on both sides of the pulley. Let the mass of the counterweight be $m_C = 1000$ kg. Assume the mass of the empty elevator is 850 kg, and its mass when carrying four passengers is $m_E = 1150$ kg. For the latter case ($m_E = 1150$ kg), calculate (a) the acceleration of the elevator and (b) the tension in the cable.

APPROACH Again we have two objects, and we will need to apply Newton's second law to each of them separately. Each mass has two forces acting on it: gravity downward and the cable tension pulling upward, \vec{F}_T . Figures 4-23b and c show the free-body diagrams for the elevator (m_E) and for the counterweight (m_C). The elevator, being the heavier, will accelerate downward, whereas the counterweight will accelerate upward. The magnitudes of their accelerations will be equal (we assume the cable doesn't stretch). For the counterweight, $m_C g = (1000 \text{ kg})(9.80 \text{ m/s}^2) = 9800 \text{ N}$, so F_T must be greater than 9800 N (in order that m_C will accelerate upward). For the elevator, $m_E g = (1150 \text{ kg})(9.80 \text{ m/s}^2) = 11,300 \text{ N}$, which must have greater magnitude than F_T so that m_E accelerates downward. Thus our calculation must give F_T between 9800 N and 11,300 N.

SOLUTION (a) To find F_T as well as the acceleration a , we apply Newton's second law, $\Sigma F = ma$, to each object. We take upward as the positive y direction for both objects. With this choice of axes, $a_C = a$ because m_C accelerates upward, and $a_E = -a$ because m_E accelerates downward. Thus

$$\begin{aligned} F_T - m_E g &= m_E a_E = -m_E a \\ F_T - m_C g &= m_C a_C = +m_C a. \end{aligned}$$

We can subtract the first equation from the second to get

$$(m_C - m_E)g = (m_C + m_E)a,$$

where a is now the only unknown. We solve this for a :

$$a = \frac{m_C - m_E}{m_C + m_E} g = \frac{1000 \text{ kg} - 1150 \text{ kg}}{1000 \text{ kg} + 1150 \text{ kg}} g = 0.070g = 0.68 \text{ m/s}^2.$$

The elevator (m_E) accelerates downward (and the counterweight m_C upward) at $a = 0.070g = 0.68 \text{ m/s}^2$.

(b) The tension in the cable F_T can be obtained from either of the two $\Sigma F = ma$ equations, setting $a = 0.070g = 0.68 \text{ m/s}^2$:

$$\begin{aligned} F_T - m_E g - m_E a &= m_E (g - a) \\ &= 1150 \text{ kg} (9.80 \text{ m/s}^2 - 0.68 \text{ m/s}^2) = 10,500 \text{ N}, \end{aligned}$$

or

$$\begin{aligned} F_T - m_C g + m_C a &= m_C (g + a) \\ &= 1000 \text{ kg} (9.80 \text{ m/s}^2 + 0.68 \text{ m/s}^2) = 10,500 \text{ N}, \end{aligned}$$

which are consistent. As predicted, our result lies between 9800 N and 11,300 N.

NOTE We can check our equation for the acceleration a in this Example by noting that if the masses were equal ($m_E = m_C$), then our equation above for a would give $a = 0$, as we should expect. Also, if one of the masses is zero (say, $m_C = 0$), then the other mass ($m_E \neq 0$) would be predicted by our equation to accelerate at $a = g$, again as expected.

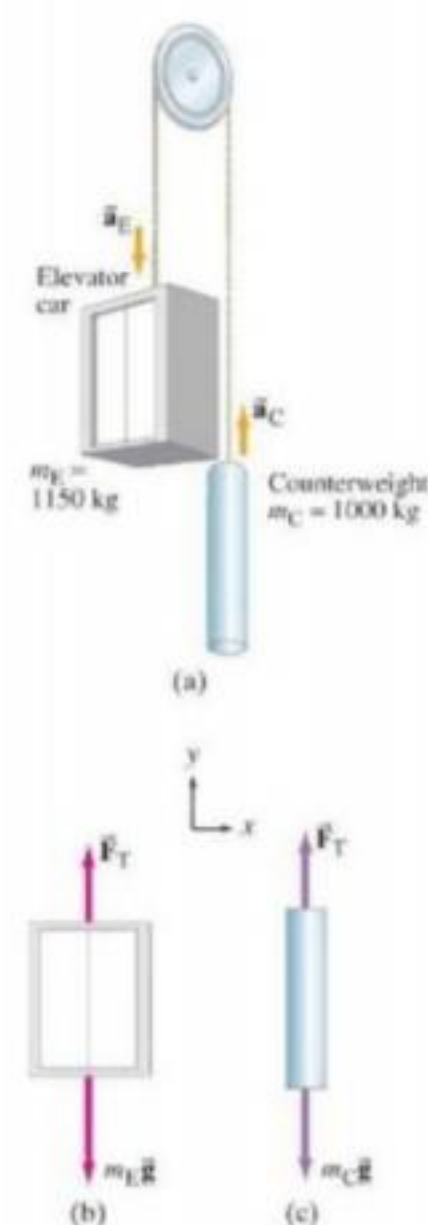


FIGURE 4-23 Example 4-13. (a) Atwood's machine in the form of an elevator-counterweight system. (b) and (c) Free-body diagrams for the two objects.

PROBLEM SOLVING
Check your result by seeing if it works in situations where the answer is easily guessed.

SECTION 4-7 Solving Problems with Newton's Laws: Free-Body Diagrams 99

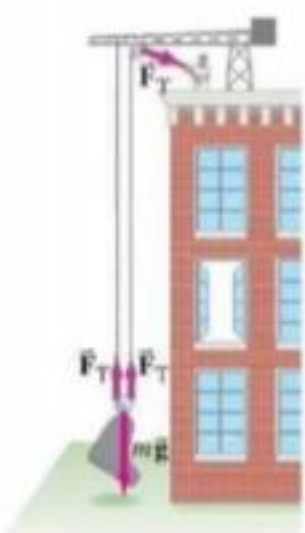


FIGURE 4-24 Example 4-14.

CONCEPTUAL EXAMPLE 4-14 The advantage of a pulley. A mover is trying to lift a piano (slowly) up to a second-story apartment (Fig. 4-24). He is using a rope looped over two pulleys as shown. What force must he exert on the rope to slowly lift the piano's 2000-N weight?

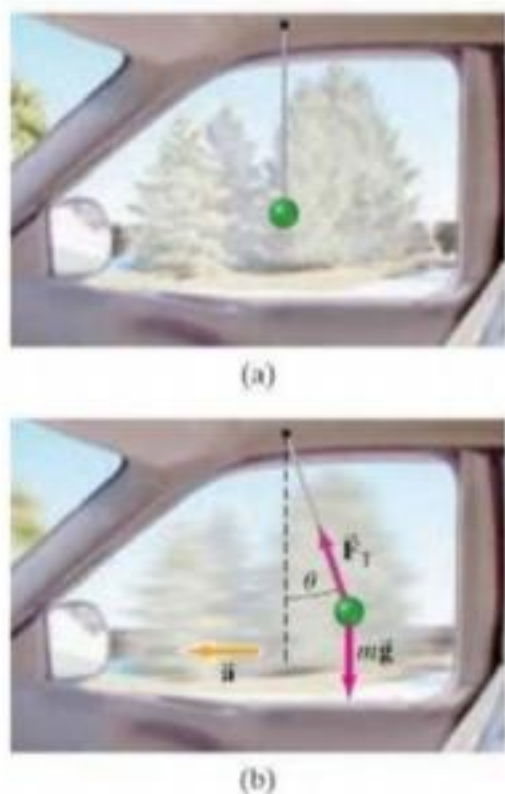
RESPONSE The magnitude of the tension force F_T within the rope is the same at any point along the rope if we assume we can ignore its mass. First notice the forces acting on the lower pulley at the piano. The weight of the piano pulls down on the pulley via a short cable. The tension in the rope, looped through this pulley, pulls up *twice*, once on each side of the pulley. Let us apply Newton's second law to the pulley-piano combination (of mass m), choosing the upward direction as positive:

$$2F_T - mg = ma.$$

To move the piano with constant speed (set $a = 0$ in this equation) thus requires a tension in the rope, and hence a pull on the rope, of $F_T = mg/2$. The mover can exert a force equal to half the piano's weight. We say the pulley has given a **mechanical advantage** of 2, since without the pulley the mover would have to exert twice the force.

PHYSICS APPLIED
Accelerometer

FIGURE 4-25 Example 4-15.



EXAMPLE 4-15 Accelerometer. A small mass m hangs from a thin string and can swing like a pendulum. You attach it above the window of your car as shown in Fig. 4-25a. When the car is at rest, the string hangs vertically. What angle θ does the string make (a) when the car accelerates at a constant $a = 1.20 \text{ m/s}^2$, and (b) when the car moves at constant velocity, $v = 90 \text{ km/h}$?

APPROACH The free-body diagram of Fig. 4-25b shows the pendulum at some angle θ and the forces on it: $m\vec{g}$ downward, and the tension \vec{F}_T in the cord. These forces do not add up to zero if $\theta \neq 0$, and since we have an acceleration a , we therefore expect $\theta \neq 0$. Note that θ is the angle relative to the vertical.

SOLUTION (a) The acceleration $a = 1.20 \text{ m/s}^2$ is horizontal, so from Newton's second law,

$$ma = F_T \sin \theta$$

for the horizontal component, whereas the vertical component gives

$$0 = F_T \cos \theta - mg.$$

Dividing these two equations, we obtain

$$\tan \theta = \frac{F_T \sin \theta}{F_T \cos \theta} = \frac{ma}{mg} = \frac{a}{g}$$

or

$$\begin{aligned} \tan \theta &= \frac{1.20 \text{ m/s}^2}{9.80 \text{ m/s}^2} \\ &= 0.122, \end{aligned}$$

so

$$\theta = 7.0^\circ.$$

(b) The velocity is constant, so $a = 0$ and $\tan \theta = 0$. Hence the pendulum hangs vertically ($\theta = 0^\circ$).

NOTE This simple device is an **accelerometer**—it can be used to measure acceleration.

Inclines

Now we consider what happens when an object slides down an incline, such as a hill or ramp. Such problems are interesting because gravity is the accelerating force, yet the acceleration is not vertical. Solving such problems is usually easier if we choose the xy coordinate system so that one axis points in the direction of the acceleration. Thus we often take the x axis to point along the incline and the y axis perpendicular to the incline, as shown in Fig. 4–26a. Note also that the normal force is not vertical, but is perpendicular to the plane, Fig. 4–26b.

EXAMPLE 4–16 **Box slides down an incline.** A box of mass m is placed on a smooth (frictionless) incline that makes an angle θ with the horizontal, as shown in Fig. 4–26a. (a) Determine the normal force on the box. (b) Determine the box's acceleration. (c) Evaluate for a mass $m = 10 \text{ kg}$ and an incline of $\theta = 30^\circ$.

APPROACH We expect the motion to be along the incline, so we choose the x axis along the slope, positive down the slope (the direction of motion). The y axis is perpendicular to the incline, upward. The free-body diagram is shown in Fig. 4–26b. The forces on the box are its weight mg vertically downward, which is shown resolved into its components parallel and perpendicular to the incline, and the normal force F_N . The incline acts as a constraint, allowing motion along its surface. The “constraining” force is the normal force.

SOLUTION (a) There is no motion in the y direction, so $a_y = 0$. Applying Newton's second law we have

$$F_y = ma_y$$

$$F_N - mg \cos \theta = 0,$$

where F_N and the y component of gravity ($mg \cos \theta$) are all the forces acting on the box in the y direction. Thus the normal force is given by

$$F_N = mg \cos \theta.$$

Note carefully that unless $\theta = 0^\circ$, F_N has magnitude less than the weight mg .

(b) In the x direction the only force acting is the x component of $m\mathbf{g}$, which we see from the diagram is $mg \sin \theta$. The acceleration a is in the x direction so

$$F_x = ma_x$$

$$mg \sin \theta = ma,$$

and we see that the acceleration down the plane is

$$a = g \sin \theta.$$

Thus the acceleration along an incline is always less than g , except at $\theta = 90^\circ$, for which $\sin \theta = 1$ and $a = g$. This makes sense since $\theta = 90^\circ$ is pure vertical fall. For $\theta = 0^\circ$, $a = 0$, which makes sense because $\theta = 0^\circ$ means the plane is horizontal so gravity causes no acceleration. Note too that the acceleration does not depend on the mass m .

(c) For $\theta = 30^\circ$, $\cos \theta = 0.866$ and $\sin \theta = 0.500$, so

$$F_N = 0.866mg = 85 \text{ N},$$

and

$$a = 0.500g = 4.9 \text{ m/s}^2.$$

We will discuss more Examples of motion on an incline in the next Chapter, where friction will be included.

PROBLEM SOLVING
Good choice of coordinate system simplifies the calculation

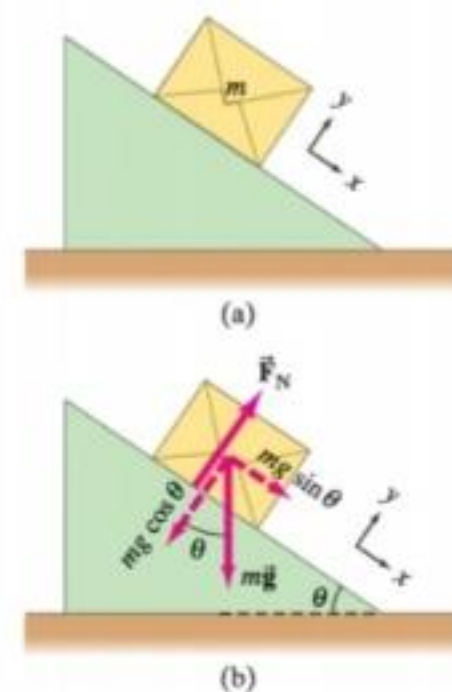


FIGURE 4–26 Example 4–16. (a) Box sliding on inclined plane. (b) Free-body diagram of box.

SECTION 4–7 Solving Problems with Newton's Laws: Free-Body Diagrams 101

4–8 Problem Solving—A General Approach

A basic part of a physics course is solving problems effectively. The approach discussed here, though emphasizing Newton's laws, can be applied generally for other topics discussed throughout this book.

PROBLEM SOLVING

In General

1. **Read** and reread written problems carefully. A common error is to skip a word or two when reading, which can completely change the meaning of a problem.
2. **Draw** an accurate picture or diagram of the situation. (This is probably the most overlooked, yet most crucial, part of solving a problem.) Use arrows to represent vectors such as velocity or force, and label the vectors with appropriate symbols. When dealing with forces and applying Newton's laws, make sure to include all forces on a given object, including unknown ones, and make clear what forces act on what object (otherwise you may make an error in determining the *net force* on a particular object).
3. A separate **free-body diagram** needs to be drawn for each object involved, and it must show *all* the forces acting on a given object (and only on that object). Do not show forces that act on other objects.
4. Choose a convenient xy **coordinate system** (one that makes your calculations easier, such as one axis in the direction of the acceleration). Vectors are to be resolved into components along the coordinate axes. When using Newton's second law, apply $\Sigma \mathbf{F} = m\mathbf{a}$ separately to x and y components, remembering that x direction forces are related to a_x , and similarly for y . If more than one object is involved, you can choose different (convenient) coordinate systems for each.
5. List the knowns and the unknowns (what you are trying to determine), and decide what you need in order to find the unknowns. For problems in the present Chapter, we use Newton's laws. More generally, it may help to see if one or more **relationships** (or **equations**) relate the unknowns to the knowns.

But be sure each relationship is applicable in the given case. It is very important to know the limitations of each formula or relationship—when it is valid and when not. In this book, the more general equations have been given numbers, but even these can have a limited range of validity (often stated in brackets to the right of the equation).

6. Try to solve the problem approximately, to see if it is doable (to check if enough information has been given) and reasonable. Use your intuition, and make **rough calculations**—see “Order of Magnitude Estimating” in Section 1–6. A rough calculation, or a reasonable guess about what the range of final answers might be, is very useful. And a rough calculation can be checked against the final answer to catch errors in calculation, such as in a decimal point or the powers of 10.
7. **Solve** the problem, which may include algebraic manipulation of equations and/or numerical calculations. Recall the mathematical rule that you need as many independent equations as you have unknowns; if you have three unknowns, for example, then you need three independent equations. It is usually best to work out the algebra symbolically before putting in the numbers. Why? Because (a) you can then solve a whole class of similar problems with different numerical values; (b) you can check your result for cases already understood (say, $\theta = 0^\circ$ or 90°); (c) there may be cancellations or other simplifications; (d) there is usually less chance for numerical error; and (e) you may gain better insight into the problem.
8. Be sure to keep track of **units**, for they can serve as a check (they must balance on both sides of any equation).
9. Again consider if your answer is **reasonable**. The use of dimensional analysis, described in Section 1–7, can also serve as a check for many problems.

Summary

Newton's three laws of motion are the basic classical laws describing motion.

Newton's first law (the **law of inertia**) states that if the net force on an object is zero, an object originally at rest remains at rest, and an object in motion remains in motion in a straight line with constant velocity.

Newton's second law states that the acceleration of an object is directly proportional to the net force acting on it, and inversely proportional to its mass:

$$\Sigma \mathbf{F} = m\mathbf{a}. \quad (4-1a)$$

Newton's second law is one of the most important and fundamental laws in classical physics.

Newton's third law states that whenever one object exerts a force on a second object, the second object always exerts a force on the first object which is equal in magnitude but opposite in direction:

$$\vec{F}_{AB} = -\vec{F}_{BA}, \quad (4-2)$$

where \vec{F}_{BA} is the force on object B exerted by object A. This is true even if objects are moving and accelerating, and/or have different masses.

The tendency of an object to resist a change in its motion is called **inertia**. **Mass** is a measure of the inertia of an object.

Weight refers to the **gravitational force** on an object, and is

equal to the product of the object's mass m and the acceleration of gravity \vec{g} :

$$\vec{F}_G = m\vec{g}. \quad (4-3)$$

Force, which is a vector, can be considered as a push or pull; or, from Newton's second law, force can be defined as an action capable of giving rise to acceleration. The **net force** on an object is the vector sum of all forces acting on that object.

For solving problems involving the forces on one or more objects, it is essential to draw a **free-body diagram** for each object, showing all the forces acting on only that object. Newton's second law can be applied to the vector components for each object.

Questions

- Why does a child in a wagon seem to fall backward when you give the wagon a sharp pull forward?
- A box rests on the (frictionless) bed of a truck. The truck driver starts the truck and accelerates forward. The box immediately starts to slide toward the rear of the truck bed. Discuss the motion of the box, in terms of Newton's laws, as seen (a) by Andrea standing on the ground beside the truck, and (b) by Jim who is riding on the truck (Fig. 4-27).



FIGURE 4-27 Question 2.

- If the acceleration of an object is zero, are no forces acting on it? Explain.
- If an object is moving, is it possible for the net force acting on it to be zero?
- Only one force acts on an object. Can the object have zero acceleration? Can it have zero velocity? Explain.
- When a golf ball is dropped to the pavement, it bounces back up. (a) Is a force needed to make it bounce back up? (b) If so, what exerts the force?
- If you walk along a log floating on a lake, why does the log move in the opposite direction?
- Why might your foot hurt if you kick a heavy desk or a wall?
- When you are running and want to stop quickly, you must decelerate quickly. (a) What is the origin of the force that causes you to stop? (b) Estimate (using your own experience) the maximum rate of deceleration of a person running at top speed to come to rest.
- (a) Why do you push down harder on the pedals of a bicycle when first starting out than when moving at constant speed? (b) Why do you need to pedal at all when cycling at constant speed?

- A father and his young daughter are ice skating. They face each other at rest and push each other, moving in opposite directions. Which one has the greater final speed?
- Suppose that you are standing on a cardboard carton that just barely supports you. What would happen to it if you jumped up into the air? It would (a) collapse; (b) be unaffected; (c) spring upward a bit; (d) move sideways.
- A stone hangs by a fine thread from the ceiling, and a section of the same thread dangles from the bottom of the stone (Fig. 4-28). If a person gives a sharp pull on the dangling thread, where is the thread likely to break: below the stone or above it? What if the person gives a slow and steady pull? Explain your answers.



FIGURE 4-28 Question 13.

- The force of gravity on a 2-kg rock is twice as great as that on a 1-kg rock. Why then doesn't the heavier rock fall faster?
- Would a spring scale carried to the Moon give accurate results if the scale had been calibrated on Earth, (a) in pounds, or (b) in kilograms?
- You pull a box with a constant force across a frictionless table using an attached rope held horizontally. If you now pull the rope with the same force at an angle to the horizontal (with the box remaining flat on the table), does the acceleration of the box (a) remain the same, (b) increase, or (c) decrease? Explain.
- When an object falls freely under the influence of gravity there is a net force mg exerted on it by the Earth. Yet by Newton's third law the object exerts an equal and opposite force on the Earth. Does the Earth move?
- Compare the effort (or force) needed to lift a 10-kg object when you are on the Moon with the force needed to lift it on Earth. Compare the force needed to throw a 2-kg object horizontally with a given speed on the Moon and on Earth.

Questions 103

- Which of the following objects weighs about 1 N: (a) an apple, (b) a mosquito, (c) this book, (d) you?
- According to Newton's third law, each team in a tug of war (Fig. 4-29) pulls with equal force on the other team. What, then, determines which team will win?



FIGURE 4-29 Question 20. A tug of war. Describe the forces on each of the teams and on the rope.

- When you stand still on the ground, how large a force does the ground exert on you? Why doesn't this force make you rise up into the air?
- Whiplash sometimes results from an automobile accident when the victim's car is struck violently from the rear. Explain why the head of the victim seems to be thrown backward in this situation. Is it really?

- Mary exerts an upward force of 40 N to hold a bag of groceries. Describe the "reaction" force (Newton's third law) by stating (a) its magnitude, (b) its direction, (c) on what object it is exerted, and (d) by what object it is exerted.
- A bear sling, Fig. 4-30, is used in some national parks for placing backpackers' food out of the reach of bears. Explain why the force needed to pull the backpack up increases as the backpack gets higher and higher. Is it possible to pull the rope hard enough so that it doesn't sag at all?



FIGURE 4-30 Question 24.

Problems

4-4 to 4-6 Newton's Laws, Gravitational Force, Normal Force

- (I) What force is needed to accelerate a child on a sled (total mass = 55 kg) at 1.4 m/s^2 ?
- (I) A net force of 265 N accelerates a bike and rider at 2.30 m/s^2 . What is the mass of the bike and rider together?
- (I) What is the weight of a 68-kg astronaut (a) on Earth, (b) on the Moon ($g = 1.7 \text{ m/s}^2$), (c) on Mars ($g = 3.7 \text{ m/s}^2$), (d) in outer space traveling with constant velocity?
- (I) How much tension must a rope withstand if it is used to accelerate a 1210-kg car horizontally along a frictionless surface at 1.20 m/s^2 ?
- (II) Superman must stop a 120-km/h train in 150 m to keep it from hitting a stalled car on the tracks. If the train's mass is $3.6 \times 10^5 \text{ kg}$, how much force must he exert? Compare to the weight of the train (give as %). How much force does the train exert on Superman?
- (II) What average force is required to stop a 950-kg car in 8.0 s if the car is traveling at 95 km/h?
- (II) Estimate the average force exerted by a shot-putter on a 7.0-kg shot if the shot is moved through a distance of 2.8 m and is released with a speed of 13 m/s.
- (II) A 0.140-kg baseball traveling 35.0 m/s strikes the catcher's mitt, which, in bringing the ball to rest, recoils backward 11.0 cm.

- (II) A 20.0-kg box rests on a table. (a) What is the weight of the box and the normal force acting on it? (b) A 10.0-kg box is placed on top of the 20.0-kg box, as shown in Fig. 4-31. Determine the normal force that the table exerts on the 20.0-kg box and the normal force that the 20.0-kg box exerts on the 10.0-kg box.

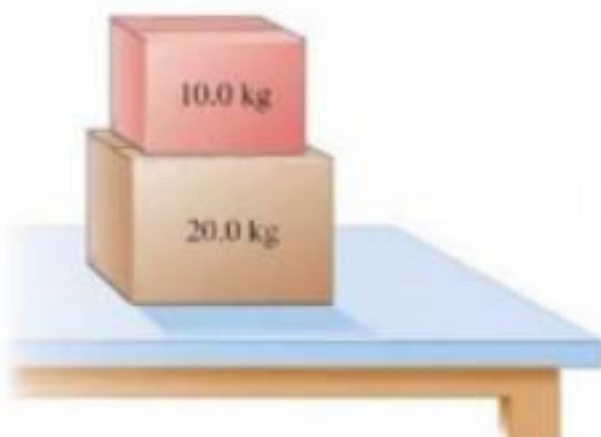


FIGURE 4-31 Problem 10.

- (II) What average force is needed to accelerate a 9.20-gram pellet from rest to 125 m/s over a distance of 0.800 m along the barrel of a rifle?
- (II) How much tension must a cable withstand if it is used to accelerate a 1200-kg car vertically upward at 0.70 m/s^2 ?
- (II) A 14.0-kg bucket is lowered vertically by a rope in which there is 163 N of tension at a given instant. What is

15. (II) A 75-kg petty thief wants to escape from a third-story jail window. Unfortunately, a makeshift rope made of sheets tied together can support a mass of only 58 kg. How might the thief use this "rope" to escape? Give a quantitative answer.
16. (II) An elevator (mass 4850 kg) is to be designed so that the maximum acceleration is $0.0680g$. What are the maximum and minimum forces the motor should exert on the supporting cable?
17. (II) Can cars "stop on a dime"? Calculate the acceleration of a 1400-kg car if it can stop from 35 km/h on a dime (diameter = 1.7 cm.) How many g 's is this? What is the force felt by the 68-kg occupant of the car?
18. (II) A person stands on a bathroom scale in a motionless elevator. When the elevator begins to move, the scale briefly reads only 0.75 of the person's regular weight. Calculate the acceleration of the elevator, and find the direction of acceleration.
19. (II) High-speed elevators function under two limitations: (1) the maximum magnitude of vertical acceleration that a typical human body can experience without discomfort is about 1.2 m/s^2 , and (2) the typical maximum speed attainable is about 9.0 m/s . You board an elevator on a skyscraper's ground floor and are transported 180 m above the ground level in three steps: acceleration of magnitude 1.2 m/s^2 from rest to 9.0 m/s , followed by constant upward velocity of 9.0 m/s , then deceleration of magnitude 1.2 m/s^2 from 9.0 m/s to rest. (a) Determine the elapsed time for each of these 3 stages. (b) Determine the change in the magnitude of the normal force, expressed as a % of your normal weight during each stage. (c) What fraction of the total transport time does the normal force not equal the person's weight?
20. (II) Using focused laser light, *optical tweezers* can apply a force of about 10 pN to a $1.0\text{-}\mu\text{m}$ diameter polystyrene bead, which has a density about equal to that of water: a volume of 1.0 cm^3 has a mass of about 1.0 g . Estimate the bead's acceleration in g 's.
21. (II) A rocket with a mass of $2.75 \times 10^6 \text{ kg}$ exerts a vertical force of $3.55 \times 10^7 \text{ N}$ on the gases it expels. Determine (a) the acceleration of the rocket, (b) its velocity after 8.0 s, and (c) how long it takes to reach an altitude of 9500 m. Assume g remains constant, and ignore the mass of gas expelled (not realistic).
22. (II) (a) What is the acceleration of two falling sky divers (mass = 132 kg including parachute) when the upward force of air resistance is equal to one-fourth of their weight? (b) After popping open the parachute, the divers descend leisurely to the ground at constant speed. What now is the force of air resistance on the sky divers and their parachute? See Fig. 4–32.



FIGURE 4–32 Problem 22.

23. (II) An exceptional standing jump would raise a person 0.80 m off the ground. To do this, what force must a 68-kg person exert against the ground? Assume the person crouches a distance of 0.20 m prior to jumping, and thus the upward force has this distance to act over before he leaves the ground.
24. (II) The cable supporting a 2125-kg elevator has a maximum strength of 21,750 N. What maximum upward acceleration can it give the elevator without breaking?
25. (III) The 100-m dash can be run by the best sprinters in 10.0 s. A 66-kg sprinter accelerates uniformly for the first 45 m to reach top speed, which he maintains for the remaining 55 m. (a) What is the average horizontal component of force exerted on his feet by the ground during acceleration? (b) What is the speed of the sprinter over the last 55 m of the race (i.e., his top speed)?
26. (III) A person jumps from the roof of a house 3.9-m high. When he strikes the ground below, he bends his knees so that his torso decelerates over an approximate distance of 0.70 m. If the mass of his torso (excluding legs) is 42 kg, find (a) his velocity just before his feet strike the ground, and (b) the average force exerted on his torso by his legs during deceleration.

4–7 Using Newton's Laws

27. (I) A box weighing 77.0 N rests on a table. A rope tied to the box runs vertically upward over a pulley and a weight is hung from the other end (Fig. 4–33). Determine the force the table exerts on the box if the weight hanging on the other end of the pulley weighs (a) 30.0 N, (b) 60.0 N, and (c) 90.0 N.

125/1322



FIGURE 4–33 Problem 27.

28. (I) Draw the free-body diagram for a basketball player (a) just before leaving the ground on a jump, and (b) while in the air. See Fig. 4–34.



FIGURE 4–34 Problem 28.

29. (I) Sketch the free-body diagram of a baseball (a) at the moment it is hit by the bat, and again (b) after it has left the bat and is flying toward the outfield.

Problems 105

30. (I) A 650-N force acts in a northwesterly direction. A second 650-N force must be exerted in what direction so that the resultant of the two forces points westward? Illustrate your answer with a vector diagram.
31. (II) Christian is making a Tyrolean traverse as shown in Fig. 4–35. That is, he traverses a chasm by stringing a rope between a tree on one side of the chasm and a tree on the opposite side, 25 m away. The rope must sag sufficiently so it won't break. Assume the rope can provide a tension force of up to 29 kN before breaking, and use a "safety factor" of 10 (that is, the rope should only be required to undergo a tension force of 2.9 kN) at the center of the Tyrolean traverse. (a) Determine the distance x that the rope must sag if it is to be within its recommended safety range and Christian's mass is 72.0 kg. (b) If the Tyrolean traverse is incorrectly set up so that the rope sags by only one-fourth the distance found in (a), determine the tension force in the rope. Will the rope break?



FIGURE 4–35 Problem 31.

32. (II) A window washer pulls herself upward using the bucket-pulley apparatus shown in Fig. 4–36. (a) How hard must she pull downward to raise herself slowly at constant speed? (b) If she increases this force by 15%, what will her acceleration be? The mass of the person plus the bucket is 72 kg.



FIGURE 4–36 Problem 32.

33. (II) One 3.2-kg paint bucket is hanging by a massless cord from another 3.2-kg paint bucket, also hanging by a massless cord, as shown in Fig. 4–37. (a) If the buckets are at rest, what is the tension in each cord? (b) If the two buckets are pulled upward with an acceleration of 1.25 m/s^2 by the upper cord, calculate the tension in each cord.



FIGURE 4–37 Problems 33 and 34.

35. (II) Two snowcats in Antarctica are towing a housing unit to a new location, as shown in Fig. 4–38. The sum of the forces \vec{F}_A and \vec{F}_B exerted on the unit by the horizontal cables is parallel to the line L , and $F_A = 4500 \text{ N}$. Determine F_B and the magnitude of $\vec{F}_A + \vec{F}_B$.

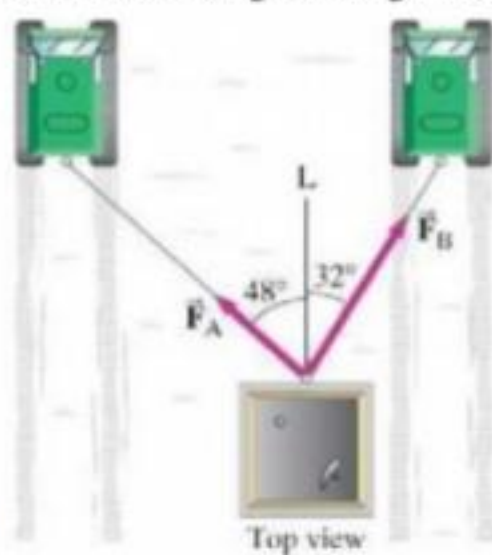


FIGURE 4–38 Problem 35.

36. (II) A train locomotive is pulling two cars of the same mass behind it, Fig. 4–39. Determine the ratio of the tension in the coupling (think of it as a cord) between the locomotive and the first car (F_{T1}), to that between the first car and the second car (F_{T2}), for any nonzero acceleration of the train.



FIGURE 4–39 Problem 36.

37. (II) The two forces \vec{F}_1 and \vec{F}_2 shown in Fig. 4–40a and b (looking down) act on a 18.5-kg object on a frictionless tabletop. If $F_1 = 10.2 \text{ N}$ and $F_2 = 16.0 \text{ N}$, find the net force on the object and its acceleration for (a) and (b).

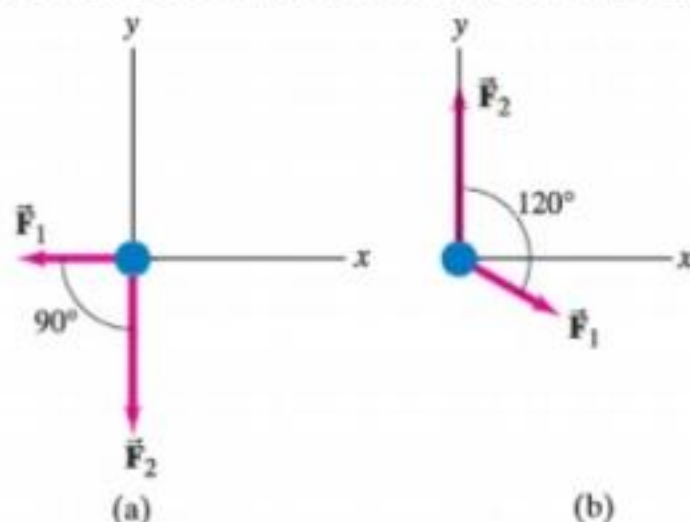


FIGURE 4–40 Problem 37.

38. (II) At the instant a race began, a 65-kg sprinter exerted a force of 720 N on the starting block at a 22° angle with respect to the ground. (a) What was the horizontal acceleration of the sprinter? (b) If the force was exerted for 0.32 s, with what speed did the sprinter leave the starting block?
39. (II) A mass m is at rest on a horizontal frictionless surface at $t = 0$. Then a constant force F_0 acts on it for a time t_0 . Suddenly the force doubles to $2F_0$ and remains constant until $t = 2t_0$. Determine the total distance traveled from $t = 0$ to $t = 2t_0$.
40. (II) A 3.0-kg object has the following two forces acting on it:

$$\vec{F}_1 = (16\hat{i} + 12\hat{j}) \text{ N}$$

41. (II) Uphill escape ramps are sometimes provided to the side of steep downhill highways for trucks with overheated brakes. For a simple 11° upward ramp, what length would be needed for a runaway truck traveling 140 km/h? Note the large size of your calculated length. (If sand is used for the bed of the ramp, its length can be reduced by a factor of about 2.)
42. (II) A child on a sled reaches the bottom of a hill with a velocity of 10.0 m/s and travels 25.0 m along a horizontal straightaway to a stop. If the child and sled together have a mass of 60.0 kg, what is the average retarding force on the sled on the horizontal straightaway?
43. (II) A skateboarder, with an initial speed of 2.0 m/s, rolls virtually friction free down a straight incline of length 18 m in 3.3 s. At what angle θ is the incline oriented above the horizontal?
44. (II) As shown in Fig. 4-41, five balls (masses 2.00, 2.05, 2.10, 2.15, 2.20 kg) hang from a crossbar. Each mass is supported by "5-lb test" fishing line which will break when its tension force exceeds 22.2 N (= 5 lb). When this device is placed in an elevator, which accelerates upward, only the lines attached to the 2.05 and 2.00 kg masses do not break. Within what range is the elevator's acceleration?

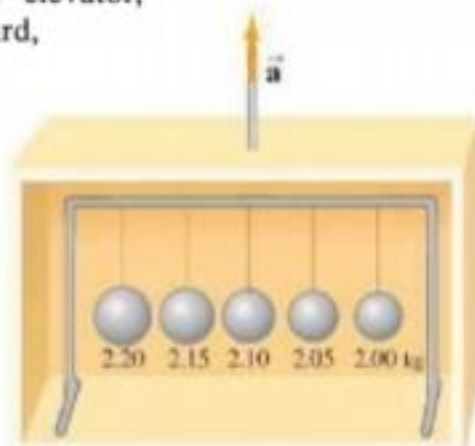


FIGURE 4-41 Problem 44.

45. (II) A 27-kg chandelier hangs from a ceiling on a vertical 4.0-m-long wire. (a) What horizontal force would be necessary to displace its position 0.15 m to one side? (b) What will be the tension in the wire?
46. (II) Three blocks on a frictionless horizontal surface are in contact with each other as shown in Fig. 4-42. A force \vec{F} is applied to block A (mass m_A). (a) Draw a free-body diagram for each block. (b) Determine the acceleration of the system (in terms of m_A , m_B , and m_C), (c) the net force on each block, and (d) the force of contact that each block exerts on its neighbor. (e) If $m_A = m_B = m_C = 10.0$ kg and $F = 96.0$ N, give numerical answers to (b), (c), and (d). Explain how your answers make sense intuitively.

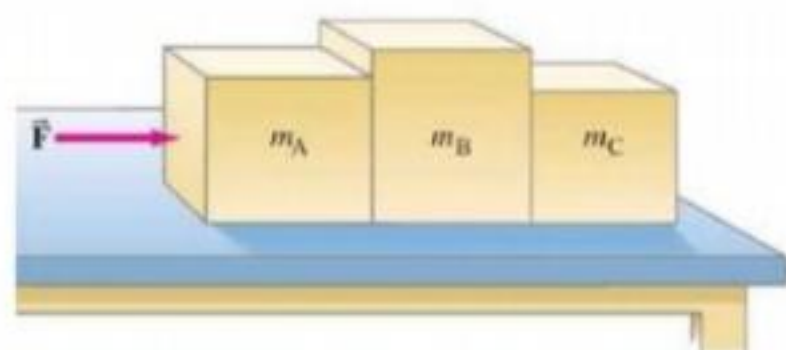


FIGURE 4-42 Problem 46.

47. (II) Redo Example 4-13 but (a) set up the equations so that the direction of the acceleration \vec{a} of each object is in the direction of motion of that object. (In Example 4-13, we took \vec{a} as positive upward for both masses.) (b) Solve the equations to obtain the same answers as in Example 4-13.

48. (II) The block shown in Fig. 4-43 has mass $m = 7.0$ kg and lies on a fixed smooth frictionless plane tilted at an angle $\theta = 22.0^\circ$ to the horizontal. (a) Determine the acceleration of the block as it slides down the plane. (b) If the block starts from rest 12.0 m up the plane from its base, what will be the block's speed when it reaches the bottom of the incline?

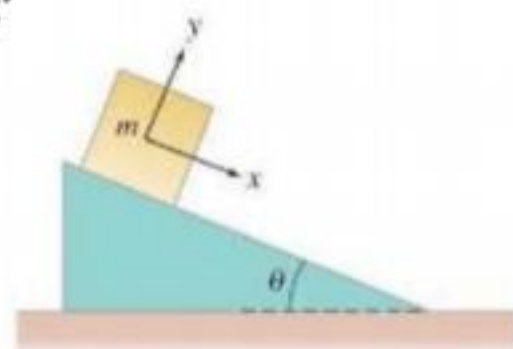


FIGURE 4-43 Block on inclined plane. Problems 48 and 49.

49. (II) A block is given an initial speed of 4.5 m/s up the 22° plane shown in Fig. 4-43. (a) How far up the plane will it go? (b) How much time elapses before it returns to its starting point? Ignore friction.
50. (II) An object is hanging by a string from your rearview mirror. While you are accelerating at a constant rate from rest to 28 m/s in 6.0 s, what angle θ does the string make with the vertical? See Fig. 4-44.

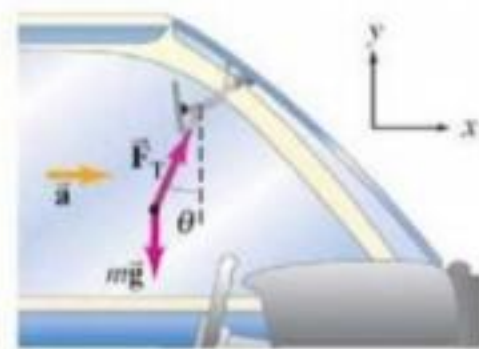


FIGURE 4-44 Problem 50.

51. (II) Figure 4-45 shows a block (mass m_A) on a smooth horizontal surface, connected by a thin cord that passes over a pulley to a second block (m_B), which hangs vertically. (a) Draw a free-body diagram for each block, showing the force of gravity on each, the force (tension) exerted by the cord, and any normal force. (b) Apply Newton's second law to find formulas for the acceleration of the system and for the tension in the cord. Ignore friction and the masses of the pulley and cord.

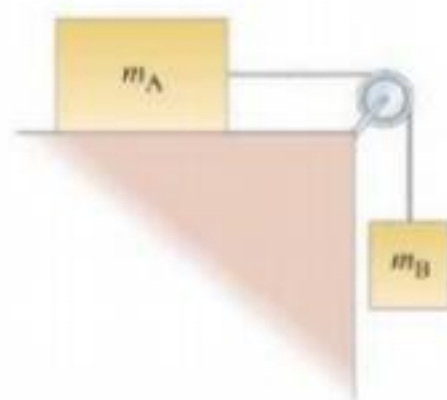


FIGURE 4-45 Problems 51, 52, and 53. Mass m_A rests on a smooth horizontal surface, m_B hangs vertically.

52. (II) (a) If $m_A = 13.0$ kg and $m_B = 5.0$ kg in Fig. 4-45, determine the acceleration of each block. (b) If initially m_A is at rest 1.250 m from the edge of the table, how long does it take to reach the edge of the table if the system is allowed to move freely? (c) If $m_B = 1.0$ kg, how large must m_A be if the acceleration of the system is to be kept at $\frac{1}{100}g$?
53. (III) Determine a formula for the acceleration of the system shown in Fig. 4-45 (see Problem 51) if the cord has a non-negligible mass m_C . Specify in terms of ℓ_A and ℓ_B , the lengths of cord from the respective masses to the pulley. (The total cord length is $\ell = \ell_A + \ell_B$.)

54. (III) Suppose the pulley in Fig. 4-46 is suspended by a cord C. Determine the tension in this cord after the masses are released and before one hits the ground. Ignore the mass of the pulley and cords.

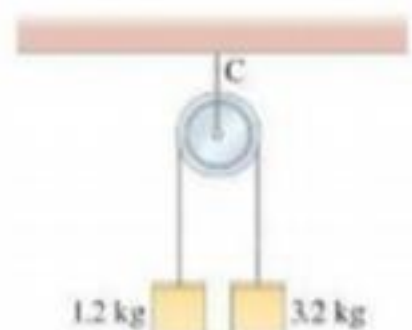


FIGURE 4-46 Problem 54.

55. (III) A small block of mass m rests on the sloping side of a triangular block of mass M which itself rests on a horizontal table as shown in Fig. 4-47. Assuming all surfaces are frictionless, determine the magnitude of the force \vec{F} that must be applied to M so that m remains in a fixed position relative to M (that is, m doesn't move on the incline). [Hint: Take x and y axes horizontal and vertical.]

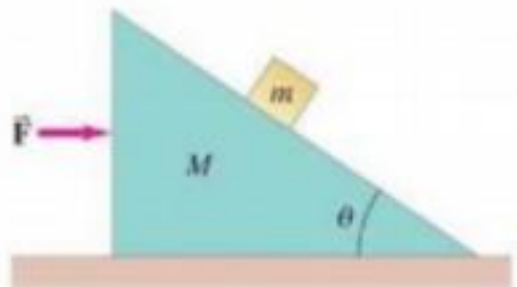


FIGURE 4-47 Problem 55.

56. (III) The double Atwood machine shown in Fig. 4-48 has frictionless, massless pulleys and cords. Determine (a) the acceleration of masses m_A , m_B , and m_C , and (b) the tensions F_{TA} and F_{TC} in the cords.

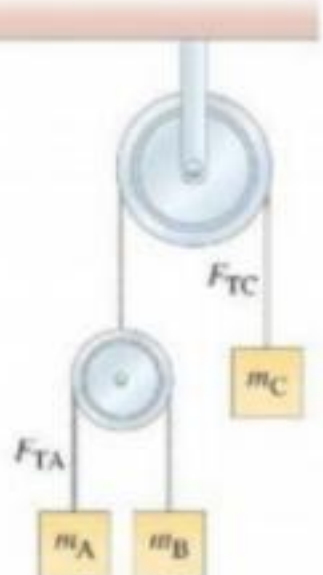


FIGURE 4-48 Problem 56.

57. (III) Suppose two boxes on a frictionless table are connected by a heavy cord of mass 1.0 kg. Calculate the acceleration of each box and the tension at each end of the cord, using the free-body diagrams shown in Fig. 4-49. Assume $F_p = 35.0$ N, and ignore sagging of the cord. Compare your results to Example 4-12 and Fig. 4-22.

58. (III) The two masses shown in Fig. 4-50 are each initially 1.8 m above the ground, and the massless frictionless pulley is 4.8 m above the ground. What maximum height does the lighter object reach after the system is released? [Hint: First determine the acceleration of the lighter mass and then its velocity at the moment the heavier one hits the ground. This is its "launch" speed. Assume the mass doesn't hit the pulley. Ignore the mass of the cord.]

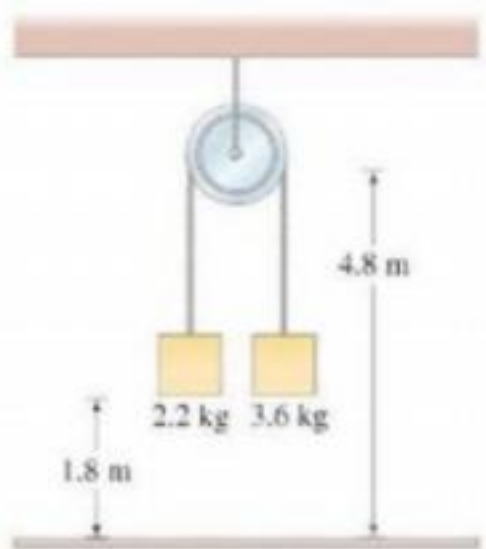


FIGURE 4-50 Problem 58.

59. (III) Determine a formula for the magnitude of the force \vec{F} exerted on the large block (m_C) in Fig. 4-51 so that the mass m_A does not move relative to m_C . Ignore all friction. Assume m_B does not make contact with m_C .

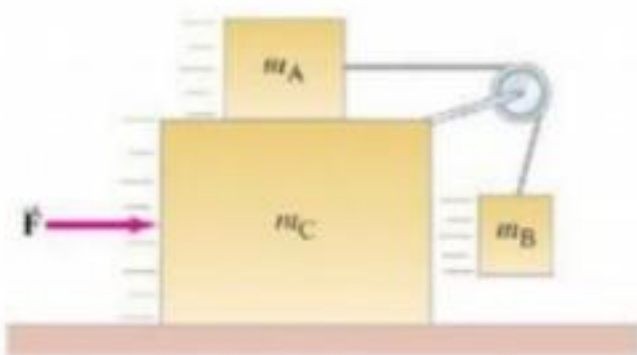


FIGURE 4-51 Problem 59.

60. (III) A particle of mass m , initially at rest at $x = 0$, is accelerated by a force that increases in time as $F = Ct^2$. Determine its velocity v and position x as a function of time.
61. (III) A heavy steel cable of length ℓ and mass M passes over a small massless, frictionless pulley. (a) If a length y hangs on one side of the pulley (so $\ell - y$ hangs on the other side), calculate the acceleration of the cable as a function of y . (b) Assuming the cable starts from rest with length y_0 on one side of the pulley, determine the velocity v_f at the moment the whole cable has fallen from the pulley. (c) Evaluate v_f for $y_0 = \frac{2}{3}\ell$. [Hint: Use the chain rule, $dv/dt = (dv/dy)(dy/dt)$, and integrate.]

62. A person has a reasonable chance of surviving an automobile crash if the deceleration is no more than $30g$'s. Calculate the force on a 65-kg person accelerating at this rate. What distance is traveled if brought to rest at this rate from 95 km/h?
63. A 2.0-kg purse is dropped 58 m from the top of the Leaning Tower of Pisa and falls 55 m before reaching the ground with a speed of 27 m/s. What was the average force of air resistance?
64. Tom's hang glider supports his weight using the six ropes shown in Fig. 4-52. Each rope is designed to support an equal fraction of Tom's weight. Tom's mass is 74.0 kg. What is the tension in each of the support ropes?

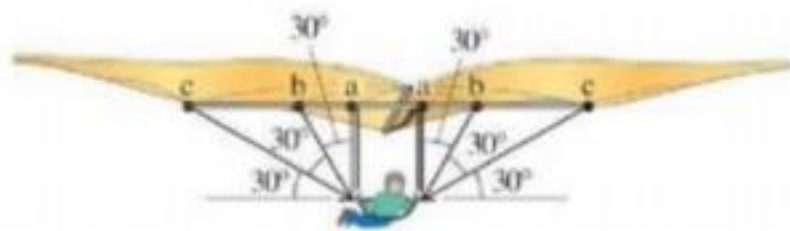


FIGURE 4-52 Problem 64.

65. A wet bar of soap ($m = 150$ g) slides freely down a ramp 3.0 m long inclined at 8.5° . How long does it take to reach the bottom? How would this change if the soap's mass were 300 g?
66. A crane's trolley at point P in Fig. 4-53 moves for a few seconds to the right with constant acceleration, and the 870-kg load hangs at a 5.0° angle to the vertical as shown. What is the acceleration of the trolley and load?



FIGURE 4-53 Problem 66.

67. A block (mass m_A) lying on a fixed frictionless inclined plane is connected to a mass m_B by a cord passing over a pulley, as shown in Fig. 4-54. (a) Determine a formula for the acceleration of the system in terms of m_A , m_B , θ , and g . (b) What conditions apply to masses m_A and m_B for the acceleration to be in one direction (say, m_A down the plane), or in the opposite direction? Ignore the mass of the cord and pulley.

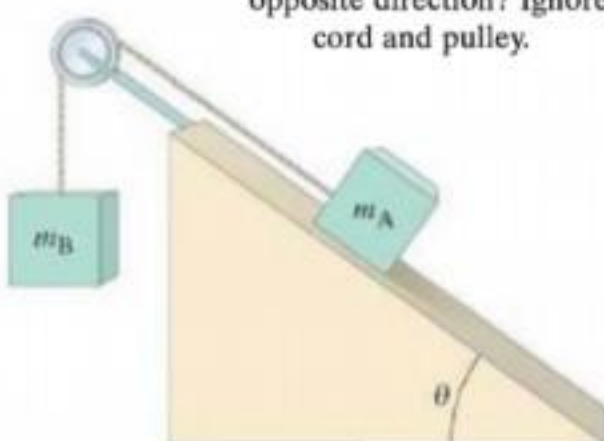


FIGURE 4-54 Problems 67 and 68.

68. (a) In Fig. 4-54, if $m_A = m_B = 1.00$ kg and $\theta = 35.0^\circ$, what will be the acceleration of the system? (b) If $m_A = 1.00$ kg and the system remains at rest, what must the mass m_B be? (c) Calculate the tension in the cord for (a) and (b).
69. The masses m_A and m_B slide on the smooth (frictionless) inclines fixed as shown in Fig. 4-55. (a) Determine a formula for the acceleration of the system in terms of m_A , m_B , θ_A , θ_B , and g . (b) If $\theta_A = 32^\circ$, $\theta_B = 23^\circ$, and $m_A = 5.0$ kg, what value of m_B would keep the system at rest? What would be the tension in the cord (negligible mass) in this case? (c) What ratio, m_A/m_B , would allow the masses to move at constant speed along their ramps in either direction?

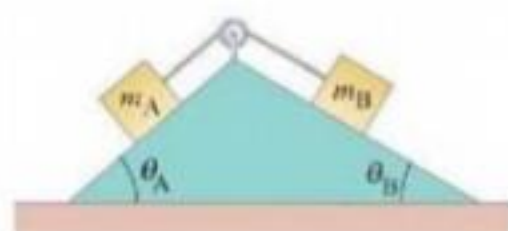


FIGURE 4-55 Problem 69.

70. A 75.0-kg person stands on a scale in an elevator. What does the scale read (in N and in kg) when (a) the elevator is at rest, (b) the elevator is climbing at a constant speed of 3.0 m/s, (c) the elevator is descending at 3.0 m/s, (d) the elevator is accelerating upward at 3.0 m/s², (e) the elevator is accelerating downward at 3.0 m/s²?
71. A city planner is working on the redesign of a hilly portion of a city. An important consideration is how steep the roads can be so that even low-powered cars can get up the hills without slowing down. A particular small car, with a mass of 920 kg, can accelerate on a level road from rest to 21 m/s (75 km/h) in 12.5 s. Using these data, calculate the maximum steepness of a hill.
72. If a bicyclist of mass 65 kg (including the bicycle) can coast down a 6.5° hill at a steady speed of 6.0 km/h because of air resistance, how much force must be applied to climb the hill at the same speed (and the same air resistance)?
73. A bicyclist can coast down a 5.0° hill at a constant speed of 6.0 km/h. If the force of air resistance is proportional to the speed v so that $F_{\text{air}} = cv$, calculate (a) the value of the constant c , and (b) the average force that must be applied in order to descend the hill at 18.0 km/h. The mass of the cyclist plus bicycle is 80.0 kg.
74. Francesca dangles her watch from a thin piece of string while the jetliner she is in accelerates for takeoff, which takes about 16 s. Estimate the takeoff speed of the aircraft if the string makes an angle of 25° with respect to the vertical, Fig. 4-56.

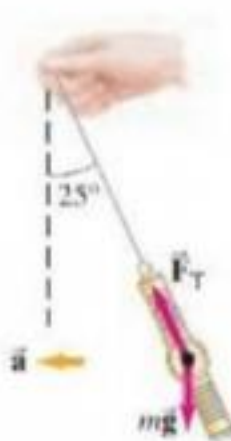


FIGURE 4-56 Problem 74.

75. (a) What minimum force F is needed to lift the piano (mass M) using the pulley apparatus shown in Fig. 4-57? (b) Determine the tension in each section of rope: F_{T1} , F_{T2} , F_{T3} , and F_{T4} .

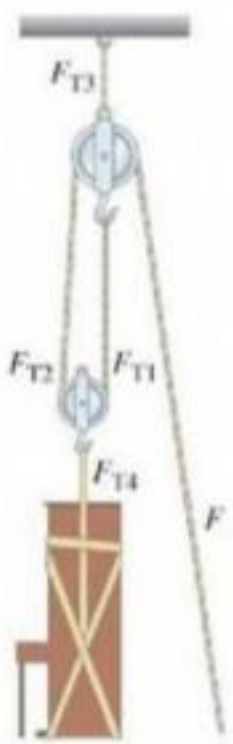


FIGURE 4-57 Problem 75.

76. In the design of a supermarket, there are to be several ramps connecting different parts of the store. Customers will have to push grocery carts up the ramps and it is obviously desirable that this not be too difficult. The engineer has done a survey and found that almost no one complains if the force required is no more than 18 N. Ignoring friction, at what maximum angle θ should the ramps be built, assuming a full 25-kg grocery cart?
77. A jet aircraft is accelerating at 3.8 m/s² as it climbs at an angle of 18° above the horizontal (Fig. 4-58). What is the total force that the cockpit seat exerts on the 75-kg pilot?

FIGURE 4-58 Problem 77.



78. A 7650-kg helicopter accelerates upward at 0.80 m/s² while lifting a 1250-kg frame at a construction site, Fig. 4-59. (a) What is the lift force exerted by the air on the helicopter rotors? (b) What is the tension in the cable (ignore its mass) that connects the frame to the helicopter? (c) What force does the cable exert on the helicopter?



FIGURE 4-59 Problem 78.

79. A super high-speed 14-car Italian train has a mass of 640 metric tons (640,000 kg). It can exert a maximum force of 400 kN horizontally against the tracks, whereas at maximum constant velocity (300 km/h), it exerts a force of about 150 kN. Calculate (a) its maximum acceleration, and (b) estimate the force of friction and air resistance at top speed.

80. A fisherman in a boat is using a "10-lb test" fishing line. This means that the line can exert a force of 45 N without breaking (1 lb = 4.45 N). (a) How heavy a fish can the fisherman land if he pulls the fish up vertically at constant speed? (b) If he accelerates the fish upward at 2.0 m/s², what maximum weight fish can he land? (c) Is it possible to land a 15-lb trout on 10-lb test line? Why or why not?
81. An elevator in a tall building is allowed to reach a maximum speed of 3.5 m/s going down. What must the tension be in the cable to stop this elevator over a distance of 2.6 m if the elevator has a mass of 1450 kg including occupants?
82. Two rock climbers, Bill and Karen, use safety ropes of similar length. Karen's rope is more elastic, called a *dynamic rope* by climbers. Bill has a *static rope*, not recommended for safety purposes in pro climbing. (a) Karen falls freely about 2.0 m and then the rope stops her over a distance of 1.0 m (Fig. 4-60). Estimate how large a force (assume constant) she will feel from the rope. (Express the result in multiples of her weight.) (b) In a similar fall, Bill's rope stretches by only 30 cm. How many times his weight will the rope pull on him? Which climber is more likely to be hurt?



FIGURE 4-60 Problem 82.

83. Three mountain climbers who are roped together in a line are ascending an icefield inclined at 31.0° to the horizontal (Fig. 4-61). The last climber slips, pulling the second climber off his feet. The first climber is able to hold them both. If each climber has a mass of 75 kg, calculate the tension in each of the two sections of rope between the three climbers. Ignore friction between the ice and the fallen climbers.



FIGURE 4-61 Problem 83.

84. A "doomsday" asteroid with a mass of 1.0×10^{10} kg is hurtling through space. Unless the asteroid's speed is changed by about 0.20 cm/s, it will collide with Earth and cause tremendous damage. Researchers suggest that a small "space tug" sent to the asteroid's surface could exert a gentle constant force of 2.5 N. For how long must this force act?