





$$\frac{P}{Q} = \frac{X + \alpha}{Y + \beta}$$

$$\frac{P}{Q} = \frac{X + \sigma l_1 + k_1}{Y + \sigma(L - l_1) + k_2}$$

$$\sigma l_1 + k_1 = \alpha$$

$$\sigma(L - l_1) + k_2 = \beta$$

$$\frac{P}{Q} + 1 = \frac{X + \cancel{\sigma l_1} + k_1 + Y + \sigma L - \cancel{\sigma l_1} + k_2}{Y + \sigma L - \sigma L + k_2} \quad \text{--- (1)}$$

Swap $X \xi Y$

$$\frac{P}{Q} = \frac{\cancel{X} + \alpha'}{X + B'}$$

$$= \frac{Y + \sigma l_2 + k_1}{X + \sigma(L - l_2) + k_2}$$

$$\frac{P+1}{Q} = \frac{Y + \cancel{\sigma l_2} + k_1 + X + \sigma L - \cancel{\sigma l_2} + k_2}{X + \sigma L - \sigma l_2 + k_2}$$

equate ① & ②

Nominator cancelled out

$$X + \sigma L - \sigma l_2 + k_2 = Y + \sigma L - \sigma l_1 + k_2$$

$$X - Y = \sigma l_2 - \sigma l_1$$

$$\boxed{X - Y = \sigma(l_2 - l_1)}$$