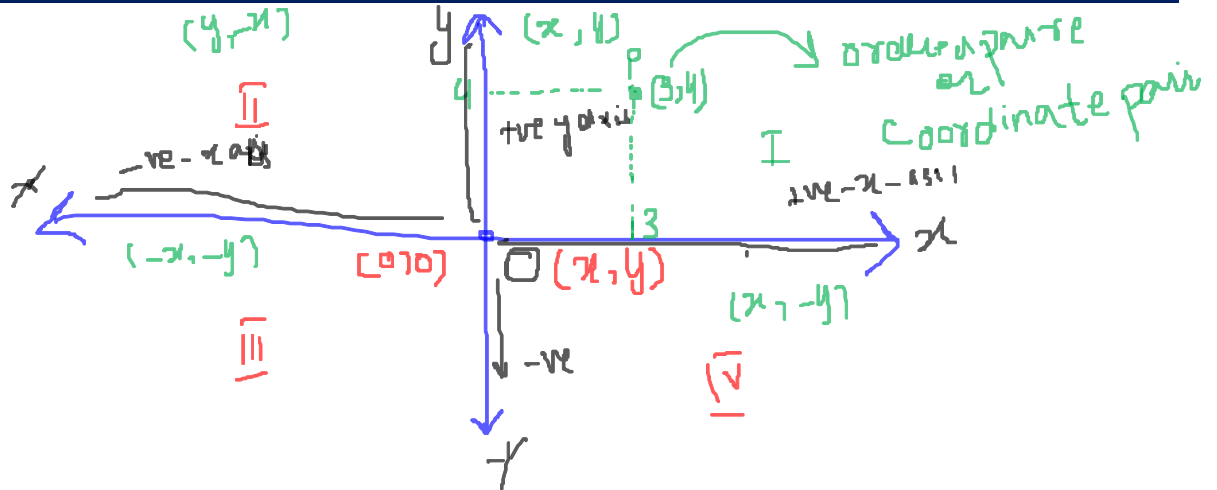


Coordinate axes

Two Perpendicular Coordinate lines that intersect at the **O- point** these lines are called coordinate axes in the plane.



Origin ✓

The coordinate system is the point in the plane where x and y are both zero

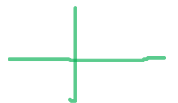
Coordinate pair

The ordered pair (a,b) is assigned to the point P

$$P(3,1) \Rightarrow (3,0) = (0,3)$$

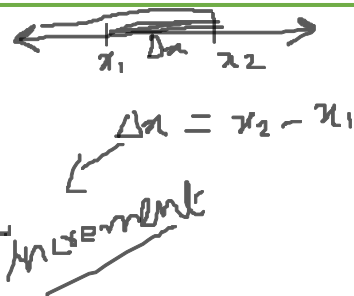
Quadrant

Coordinate axes divide into four regions is called quadrant



Increment and straight lines

When particles move from one point to another point, the net changes is called increment



$$A = (x_1, y_1) = (4, -3) \quad \begin{matrix} x_1 = 4 \\ y_1 = -3 \end{matrix} \quad \left| \quad B = (x_2, y_2) = (2, 5) \quad \begin{matrix} x_2 = 2 \\ y_2 = 5 \end{matrix}$$

Example: 01

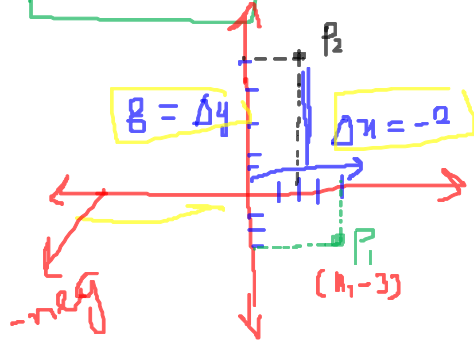
In going from the point A(4,-3) to the point B(2,5) the increments in the x and y coordinate are?

x-coordinate

$$\Delta x = x_2 - x_1$$

$$\Delta x = 2 - 4 = -2$$

$$\Delta x = -2$$



y-coordinate

$$\Delta y = y_2 - y_1$$

$$\Delta y = 5 - (-3)$$

$$\Delta y = 5 + 3 = 8$$

$$\Delta y = 8$$

$$P_1 = (x_1, y_1)$$

$$P_2 = (x_2, y_2)$$

Example: 02

The coordinate increments from C(5,6) to D(5,1)?

$$x_1 = 5 \quad y_1 = 6$$

$$x_2 = 5 \quad y_2 = 1$$

$$\Delta x = x_2 - x_1$$

$$5 - 5$$

$$\Delta x = 0$$

$$y_1 = 6 \quad y_2 = 1$$

$$\Delta y = y_2 - y_1$$

$$\Delta y = 1 - 6$$

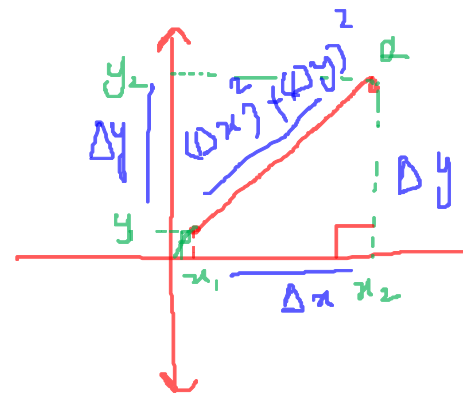
$$\Delta y = -5$$

Distance formula for a point in the plane

The distance between the points $P(x_1, y_1)$ and $Q(x_2, y_2)$

$$d = \sqrt{(\Delta x)^2 + (\Delta y)^2}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



$$H^2 = B^2 + P^2$$

$$d^2 = (\Delta x)^2 + (\Delta y)^2$$

$$d = H = \sqrt{(\Delta x)^2 + (\Delta y)^2}$$

Example: 03

The distance between $P(x_1, y_1)$ $(-1, 2)$ and $Q(x_2, y_2)$ $(3, 4)$ is

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Example: 04

The distance from origin to $P(x, y)$ is

$$O(0, 0) \text{ to } P(x, y)$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(x - 0)^2 + (y - 0)^2}$$

$$d = \sqrt{x^2 + y^2}$$

Graph

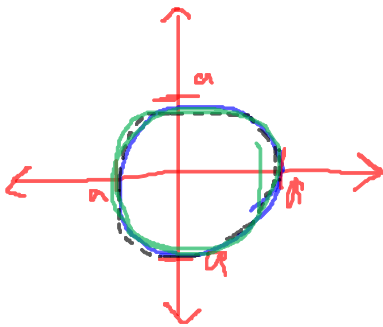
Involving the variable x and y is the set of the all point $P(x,y)$ whose coordinate satisfy the equation and inequality.

Example: 05

a) $x^2 + y^2 = a^2$ ✓
 b) $x^2 + y^2 \leq a^2$ ✓

$x = f(x)$
 $x = y$

a)



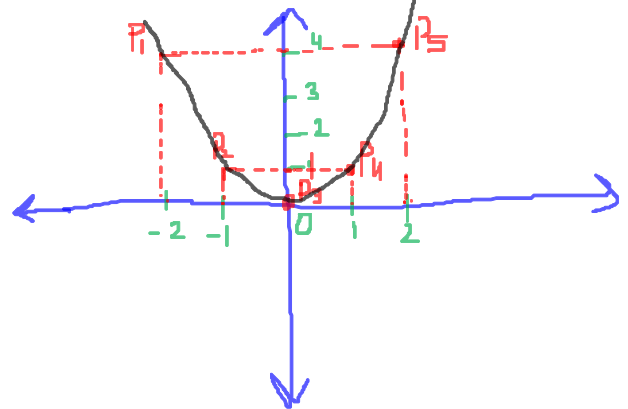
Example: 06

The equation $y = x^2$ $x \in [-2, 2]$

x	$y = x^2$
$x_1 = -2$	$y_1 = 4$
$x_2 = -1$	$y_2 = 1$
$x_3 = 0$	$y_3 = 0$
$x_4 = 1$	$y_4 = 1$
$x_5 = 2$	$y_5 = 4$

$P_1(-2, 4), P_2(-1, 1), P_3(0, 0)$
 $P_4(1, 1), P_5(2, 4)$

$y = (-2)^2 = 4$
 $y = (-1)^2 = 1$
 $y = (0)^2 = 0$
 $y = 1^2 = 1$
 $y = 2^2 = 4$

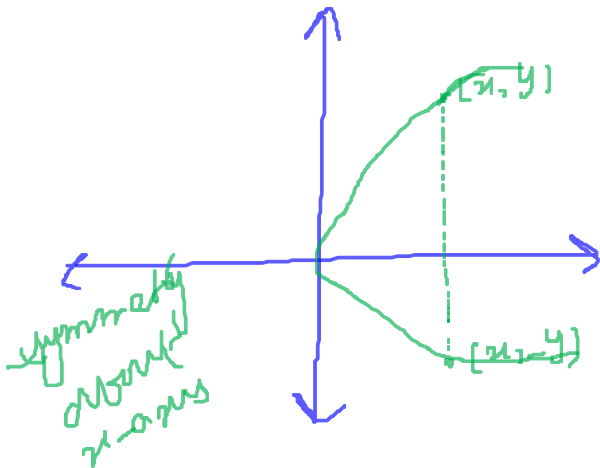


Properties:

SYMMETRY

There are three type of symmetry

- ✓ Symmetry about x - axis
- ✓ Symmetry about y - axis
- ✓ Symmetry about origin



$$f(x, y)$$

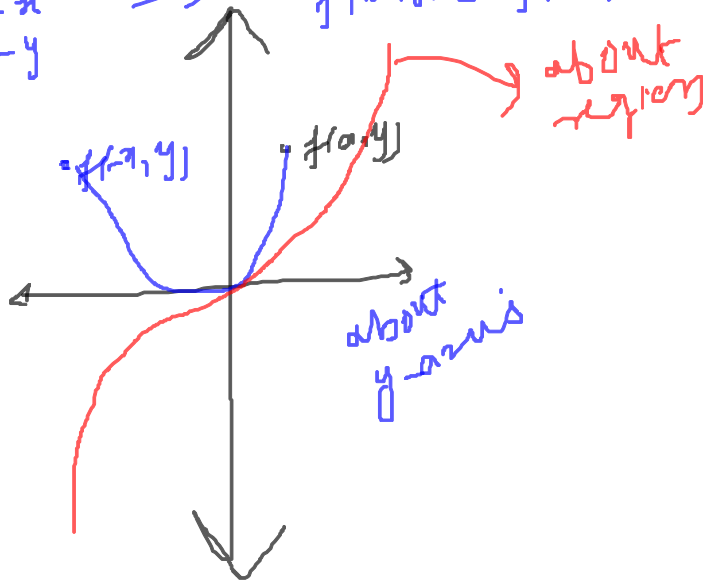
y-axis
x = -x

$$f(-x, y) = f(x, y)$$

$$y = -y \Rightarrow f(x, y) = f(x, -y)$$

$$x = -x \Rightarrow f(x, y) = f(-x, y)$$

$$y = -y \Rightarrow f(x, y) = f(x, -y)$$



x-axis
y = -y

$$\Rightarrow f(-x, -y) = f(x, y)$$

Even and odd function:

$$y = f(x)$$

$$f(-x) = f(x) = \text{even}$$

$$f(-x) = -f(x) = \text{odd}$$