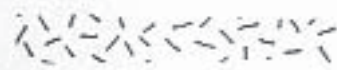
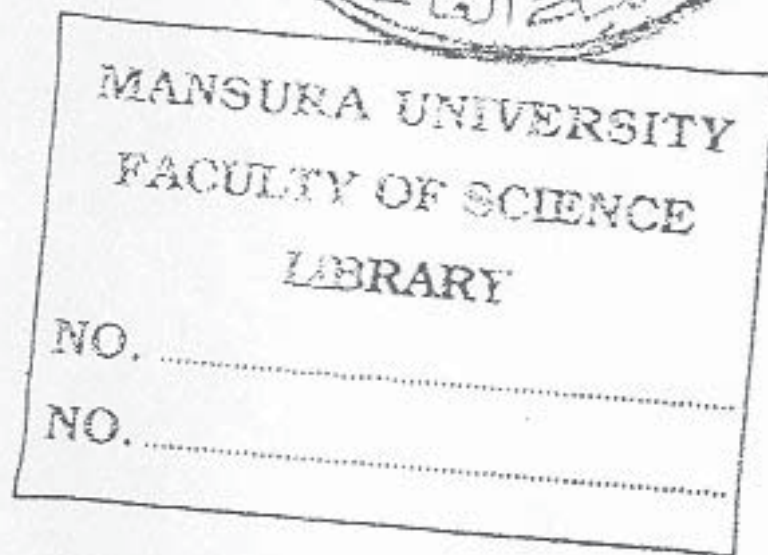


Seismic Waves



Seismic waves are messengers that convey information about the earth's interior. Basically, these waves test the extent to which earth materials can be stretched or squeezed somewhat as you can squeeze a sponge. They cause the particles of material to vibrate, which means that these particles are temporarily stretched out of position as they move back and forth. The capacity of a material to be temporarily deformed by passing seismic waves can be described by its properties of *elasticity*. These physical properties

can be used to distinguish different materials. They influence the speeds of seismic waves through those materials. In this chapter, we will discuss the elastic properties of earth materials and the different kinds of seismic waves that can travel in these materials. Then we will discuss how elastic properties influence the paths of seismic waves. Finally, we will look at methods for recording seismic waves and the typical patterns of vibration displayed on seismograms.

ELASTICITY

Stress and Strain

We can deform an object in different ways by stretching, squeezing, and twisting it. To accomplish this distortion, we must apply force on the sides of the object. Such application of force on the surface of an object is called *stress*, and it is expressed in units of force divided by area. The SI unit of stress is called a *pascal* and is equivalent to one newton (N) of force applied over a surface one meter square: $1 \text{ Pa} = 1 \text{ N/m}^2$.

When an object is placed at some depth in a pond or lake, the water presses against its sides from all directions. This is a *nondirected* stress which we call hydrostatic pressure. It is the pressure felt in the ears of a swimmer who dives deeply into the water. The fact that the swimmer feels the same pressure on both ears is evidence of equal stress in all directions. Other kinds of stress can be applied in a particular direction. An example of such a *directed* stress is the force of a hammer striking the head of a nail.

What is the effect of stress on an object? It deforms that object by changing its shape and size. The deformation is called *strain*. The different kinds of strain that can be produced depend on the strength and direction of stress and the nature of the substance being deformed. First, let us consider *elastic* strain. This kind of strain is proportional to the applied stress, and it disappears when that stress ceases. For example, we can apply stress by

pulling a rubber band, and the amount by which it stretches is a measure of strain. The harder we pull, the farther it stretches. But when we release one end, it returns to its unstretched size. This is the nature of elastic strain.

Something different happens when we stretch a lump of soft clay. It does not return to its original shape after we release it. This permanent deformation is evidence of *plastic* strain. Most substances ordinarily respond elastically to weak, short-term stresses, but they exhibit plastic strain if stronger or longer stress is applied. Finally, when the stress exceeds the strength of the material, rupture occurs. By pulling very hard, we can stretch a rubber band or the lump of clay.

Explorations by seismologists are principally with elastic strain. To be sure, plastic deformation and rupture are common in explosions or movements along faults that generate seismic waves. But this strain is confined to a small zone around the point of energy release. As the seismic waves travel away from this small source, they produce only elastic strain. Therefore, it is important for us to examine the forces involved in describing elastic strain.

Bulk Modulus

Suppose we placed a specimen of a substance in a fluid-filled container. The hydrostatic pressure could

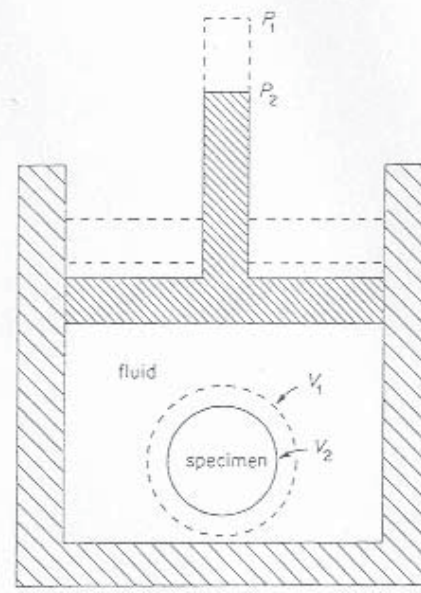


Figure 2-1

Testing the bulk modulus in a pressure cell. An increase in pressure from P_1 to P_2 causes the volume of the specimen to decrease from V_1 to V_2 .

(Figure 2-1). If the pressure is maintained at a value of P_1 , the volume of the specimen is observed to be V_1 . Now, if the pressure is increased by a small amount to P_2 , the specimen becomes compressed into a slightly smaller volume V_2 . This indicates the strain produced

by the change in stress. The mass of the specimen remain unchanged. Therefore, if the density of the specimen under pressure of P_1 , an increase to P_2 causes an increase in density. Experiments on elastic substances show that the volume and density are proportional to change in pressure. The constant of proportionality (k) is called the *bulk modulus* and is defined as

$$k = \frac{-\Delta P}{\Delta V/V_1} = \frac{\Delta P}{\Delta \rho/\rho_1}$$

where $\Delta P = P_1 - P_2$, $\Delta V = V_1 - V_2$, and $\rho_1 = \rho_2$. The bulk modulus is a measure of the capacity of a substance to be compressed. Different values of this physical property are used to distinguish one substance from another (Table 2-1). From Equation 2-1, it is expressed in the same units as pressure. The value of bulk modulus can be determined for any kind of solid, liquid, or gas.

Shear Modulus

Let us next consider a test of shear modulus, in which the shape of a specimen

TABLE 2-1 Elastic Properties of Selected Rock Specimens

SPECIMEN	BULK MODULUS (N/m ²)	SHEAR MODULUS (N/m ²)	YOUNG'S MODULUS (N/m ²)
Sandstone, quartzitic	4.17×10^{10}	4.28×10^{10}	9.6×10^{10}
Limestone, Solenhofen, Bavaria, West Germany	4.67×10^{10}	2.47×10^{10}	6.3×10^{10}
Granite, Quincy, Mass.	5.21×10^{10}	3.45×10^{10}	8.49×10^{10}
Gabbro, French Creek, Penn.	8.85×10^{10}	4.80×10^{10}	10.43×10^{10}
Marble, Vermont	7.19×10^{10}	3.33×10^{10}	8.7×10^{10}

From Francis Birch, J. F. Schairer, and H. Cecil Spicer (editors), *Handbook of Physical Constants*, Geological Society of America, Special Papers, No. 36, Table 5-8, p. 80, January 31, 1942, reprinted 1961.

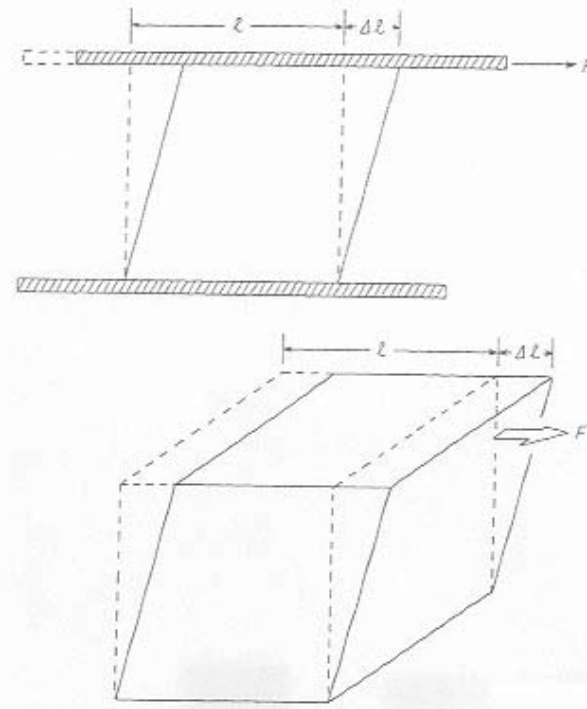


Figure 2-2

Testing shear modulus by distortion of a cube. One face of the cube is fixed, and the opposite parallel face is displaced by the small distance $\Delta\ell$ in response to the force of traction acting on that face.

We begin by attaching a cube of some substance between two parallel plates. Then force (F) is applied to displace one plate in a direction parallel to the other. Because one surface of the cube is attached to the plate, the force is applied over the entire area (A) of that surface. This creates a directed stress, $\tau = F/A$, which we call a *traction* or a *shear stress*. The cube becomes distorted as one side is shifted by the small distance $\Delta\ell$ relative to the opposite side (Figure 2-2). This distortion is an indication of shear strain. In an elastic cube of length ℓ , the small displacement will be proportional to the strength of the shear stress. The constant of proportionality (μ), called the *shear modulus*, is defined as

$$\mu = \frac{\tau}{\Delta\ell/\ell}$$

Shear stress cannot be applied to liquids and gases. For these substances, shear stress is zero. Solids possess the physical property of shear stress, which is measured by the shear modulus. This property is used to distinguish different substances (Table 2-1).

Young's Modulus and Poisson's Ratio

What happens to a specimen that is stretched or compressed by a directed stress? It can be tested by placing a cylindrical specimen in a press (Figure 2-3). Here, force is applied against the area (A) of the specimen in the direction of the stress. This force produces a directed stress: $\eta = F/A$. Suppose that when the stress has a value η_1 , the length of the specimen is ℓ_1 , and its diameter is d_1 . Now, the stress is increased to a slightly higher value η_2 , and the length of the specimen increases to ℓ_2 and its diameter increases to d_2 . The change in length is proportional to the change in stress for an elastic substance. The constant of proportionality is called the *Young's modulus* (E). It is defined as

$$E = \frac{-\Delta\eta}{\Delta\ell/\ell_1}$$

where $\Delta\eta = \eta_2 - \eta_1$ and $\Delta\ell = \ell_2 - \ell_1$. Another constant, which we call *Poisson's ratio* (σ), is used to show that the change in diameter $\Delta d = d_1 - d_2$ is proportional to the change in length:

$$\sigma = \frac{\Delta d/d_1}{\Delta\ell/\ell_1}$$

Young's modulus and Poisson's ratio, along with the shear modulus, are constants for a given material.

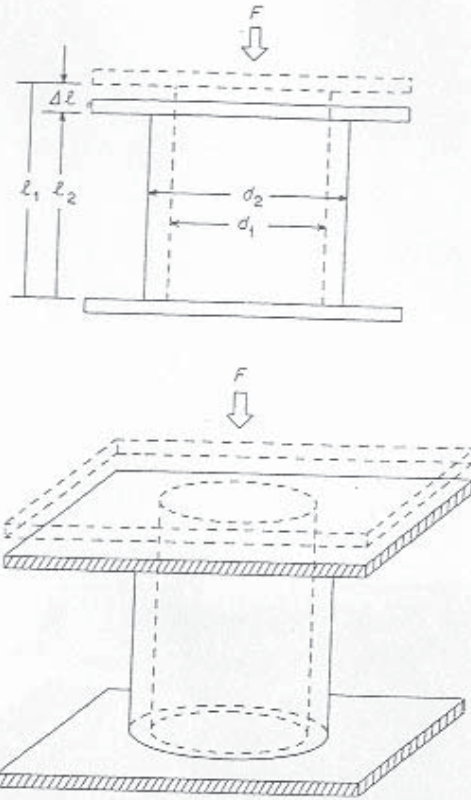


Figure 2-3
Testing Young's modulus and Poisson's ratio in a press. Young's modulus is determined from the change in length Δl , and Poisson's ratio is determined from the change in diameter $d_2 - d_1$.

ful for describing the elastic properties of solids (Table 2-1). These constants cannot be used to describe liquids and gases for which elasticity is expressed solely by the bulk modulus.

SEISMIC BODY WAVES

We are more familiar with waves on ponds, lakes, and the ocean than with seismic waves. Tossing a pebble into a quiet pond produces ripples with certain features that are common to all waves. We will look at these features first

and then describe the particular seismic waves. The ripples that spread on a pond are illustrated by the photograph in Figure 2-4, which extends outward from the point of impact of the pebble. The shape of the surface changes from time t_1 to time t_2 because the ripples are advancing. The distance between two successive crests at some particular time is called the wavelength (λ). Observe the advance of one crest from position r_1 at time t_1 to position r_2 at time t_2 . This shows that the speed of the wave is

$$V = \frac{r_2 - r_1}{t_2 - t_1}$$

The wave amplitude (H) is the maximum displacement of a water particle above or below the undisturbed surface of the pond. The graph in Figure 2-5 shows how the amplitude r_1 changes with time. The length of time required for one cycle of oscillation is called the wave period (T). This is the time for a wave crest to advance a distance equal to one wavelength (λ). Therefore, we can determine wavelength, period, and speed:

$$V = \lambda/T$$

The frequency (f) of the waves is the number of oscillations that occur during a stated interval of time. It is the reciprocal of the period:

$$f = 1/T$$

Waves on lakes and oceans come with periods of several seconds or tens of seconds and wavelengths of several meters. Some earthquake waves have similar periods and wavelengths. But exploration geophysicists usually work with wave periods of fractions of a second. These waves have frequencies of tens or hundreds of cycles per second. The unit of frequency commonly used is the hertz, which is one cycle of oscillation per second.

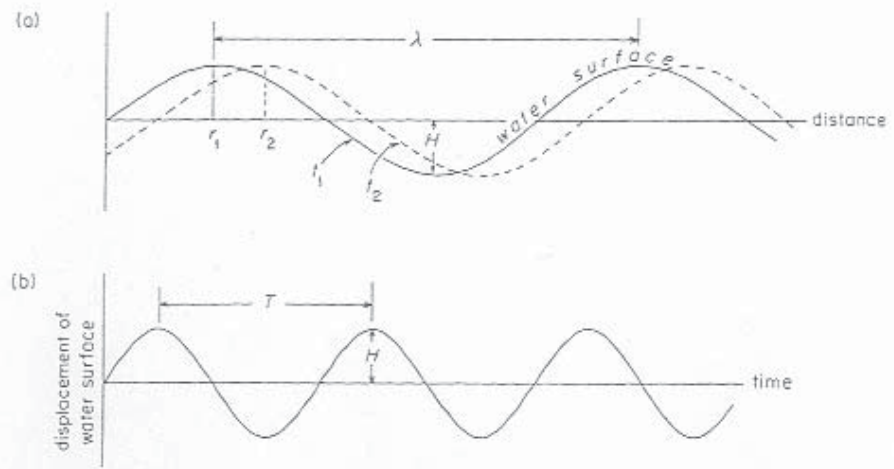


Figure 2-4

Waves produced by a pebble into a pond. The water surface extends outward from the point of impact (solid line), then at time t_2 (dashed line). Wavelength λ and H describe the shape of the surface. (b) Displacement of a point on the water surface or below the undisturbed surface changes with time as passing waves. The period T and wave height H describe the movement of this

second. The particular kinds of waves of most interest to exploration seismologists can now be described.

Compressional Waves

There are different ways to make vibrations in a specimen of rock. Let us consider what vibrations will be produced by directly striking one side with a hammer. Suppose that we have some way to detect the movement of rock particles inside the specimen. Actually, tiny pressure-sensitive devices called transducers can be used for this purpose. At the instant of impact, the particles on that side will be displaced in the direction that the hammer was moving. For a brief moment, these particles will move back and forth in this direction. A little later they will cease moving, but other particles farther inside will move back and forth in the same direction. In this way, a pulse of vibration moves through the specimen, causing particles farther and farther from the point of impact to vibrate momentarily. This pulse of vibration is the seismic wave. It moves through the specimen first

compressing, and then stretching, from place to place, as we can see in Figure 2-5. Observe that the vibrating particles move back and forth in the same direction as the path of the pulse through the specimen, causing this kind of vibration to be called a *compressional wave*, a *longitudinal wave*, all of which mean the same thing.

By placing transducers on both sides of a specimen to measure the instant when the pulse strikes and the instant when the pulse strikes the far side, we can find the time (t_p) for the P -wave to travel the distance (x) through the specimen. From this information, the P -wave speed (V_p) can be calculated.

$$V_p = x/t_p$$

Next, suppose that experimenters can measure the density and elastic properties of the specimen. We could then calculate the P -wave speed depends on these properties in the following way,

$$V_p = \sqrt{\frac{k + \frac{4}{3}\mu}{\rho}}$$

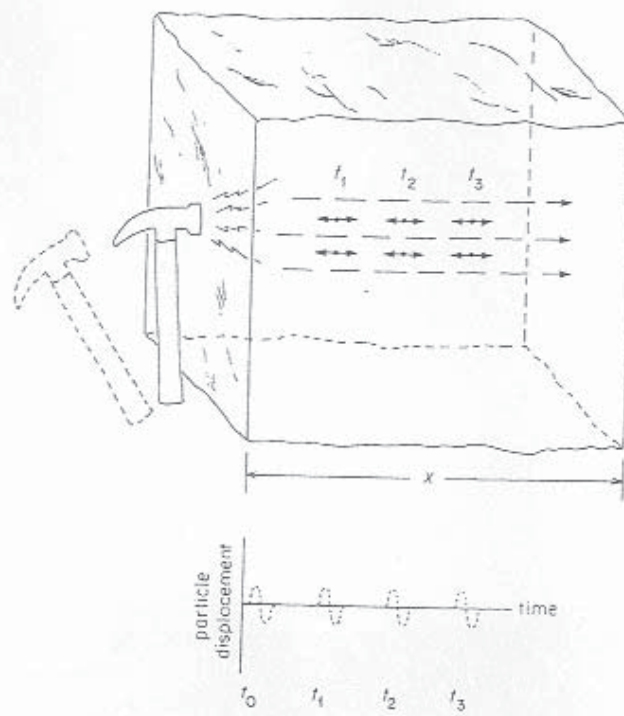


Figure 2-5

P-wave (also called a compressional wave) pulse of vibration traveling through the specimen. A simple pulse of vibration is applied on one side at time t_0 by the hammer. At later times, this wave pulse travels farther through the specimen, causing particles to vibrate back and forth in line with the direction of the wave.

or

$$V_p = \sqrt{\frac{E}{\rho} \left[\frac{1 - \sigma}{(1 - 2\sigma)(1 + \sigma)} \right]} \quad (2-9b)$$

We can tell from these equations that *P*-waves will travel through any kind of substance: solid, liquid, or gas. They can do so because values of density and bulk modulus exist for all substances, even fluids for which the shear modulus is zero. Sound waves traveling through the air are *P*-waves.

Shear Waves

Can another kind of vibration be produced in a rock specimen? Rather than hammering directly on one side, suppose that we strike a glancing blow (Figure 2-6). At the instant of impact, the rock particles hit by the hammer will vibrate back and forth briefly in a direc-

tion parallel to this side. This vibration will then move through the specimen, causing interior particles to vibrate in the same direction. After a length of time, the wave pulse will have traveled the distance x to the other side of the specimen. In Figure 2-6, the particles vibrate in a direction that is perpendicular, or transverse, to the path of the wave. We call this kind of vibration a *transverse wave*, a *shear wave*, or an *S-wave*. These terms are interchangeable. The speed V_s of the wave through the specimen would be

$$V_s = x/t_s$$

If we had already measured the elastic properties of the specimen, we could use the following relationships between elasticity, density, and *S*-wave speed,

$$V_s = \sqrt{\frac{\mu}{\rho}}$$

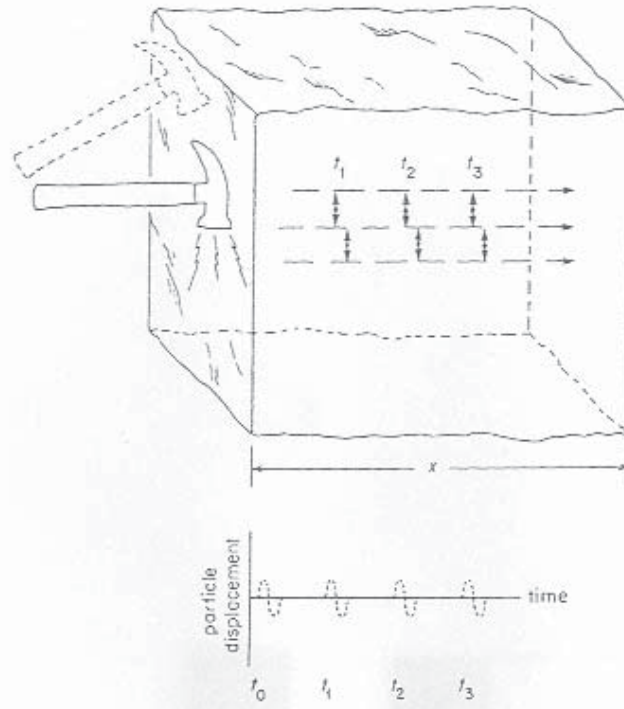


Figure 2-6

S-wave (also called a shear wave or wave) pulse of vibration traveling through the specimen. This wave pulse causes particles to vibrate back and forth in a line perpendicular to the direction of the advancing wave.

or

$$V_s = \sqrt{\frac{E}{2\rho(1 + \sigma)}} \quad (2-11b)$$

We know that $\mu = 0$ for ideal liquids and gases. Therefore, Equation 2-11 clearly shows that S-waves do not travel in fluids. These transverse vibrations travel only in solids.

Body Waves

Both P- and S-waves are called *body waves* because they can travel directly through a mass of some substance in any direction. Other kinds of seismic waves called *surface waves* can travel only near the surface of such a mass, or close to the border between two different substances. The P- and S-waves are the most basic kinds of seismic waves. Surface waves can be explained in terms of combinations of these

body waves that interfere with each other in distinctive ways when traveling along the surface of a mass. Surface waves will be discussed more fully later in this chapter.

We can learn some things about the relationship between P- and body wave speeds by combining Equations 2-9 and 2-11 to get the ratio

$$\frac{V_p}{V_s} = \sqrt{\frac{k}{\mu} + \frac{4}{3}}$$

or

$$\frac{V_p}{V_s} = \sqrt{\frac{1 - \sigma}{\frac{1}{2} - \sigma}}$$

The fact that both k and μ are positive numbers indicates that $V_p/V_s > 1$. If this is true, the P-wave must always travel faster than the S-wave through the same material.

is to say that $V_p > V_s$. It also restricts the positive range of values for Poisson's ratio: $0 < \sigma < 1/2$.

REFRACTION AND REFLECTION OF SEISMIC BODY WAVES

Rays and Wave Fronts

Think again about the ripples made by tossing a pebble into a quiet pond. Each wave moves away from the point of impact in an ever-expanding circle. The circle at the outer edge of an advancing wave marks the *wave front*. Lines drawn outward are *rays* that show directions along which the wave is advancing. Now,

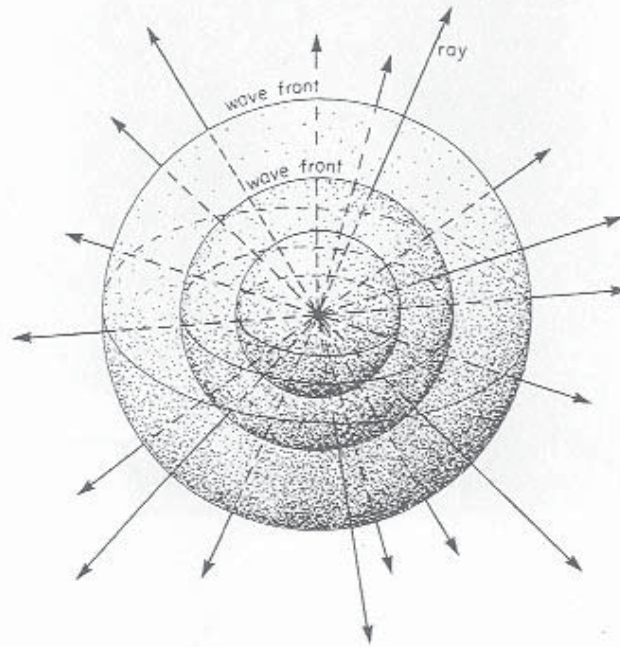


Figure 2-7

Spherical wave fronts and radiating rays illustrate the advance of waves outward in all directions from a source. The wave fronts show the position of a wave at successively later times t_1 , t_2 , t_3 , and t_4 .

rather than the surface of a pond, waves produced at a point inside a rock (Figure 2-7), perhaps by an explosion. The movement of these waves is illustrated by spherical wave fronts that radiate outward in all directions from a source. Observe that the rays are perpendicular to the wave fronts.

Wave Conversions

What happens when a wave reaches a boundary between two substances in which the wave speeds are different? It may be reflected, or *reflect*, from the boundary, or other waves that pass, or *refract*, through the boundary. The rays in Figure 2-8 show the movement of these different waves. The original wave that travels to the boundary is called the *incident wave*. At the boundary, it is converted into *reflected* and *refracted* waves, and *S*-waves that travel away from the boundary in different directions.

Observe that an incident *P*-wave is converted into *S*-waves as well as *P*-waves (Figure 2-8b). An important feature of these *S*-waves is that the transverse particle motion occurs in a plane that is perpendicular to the direction of wave travel. If the boundary is a horizontal boundary, this will be a vertical plane, and the shear waves causing vibrations in this plane are called *SV*-waves. An *SV*-wave incident on a boundary converts into reflected and refracted *SV*-waves and *P*-waves (Figure 2-8b).

A shear wave that produces transverse particle motion is called a *shear wave*. If this kind of horizontal shear wave is incident on a boundary, it converts into reflected and refracted waves (Figure 2-8c) with no associated *P*-waves.

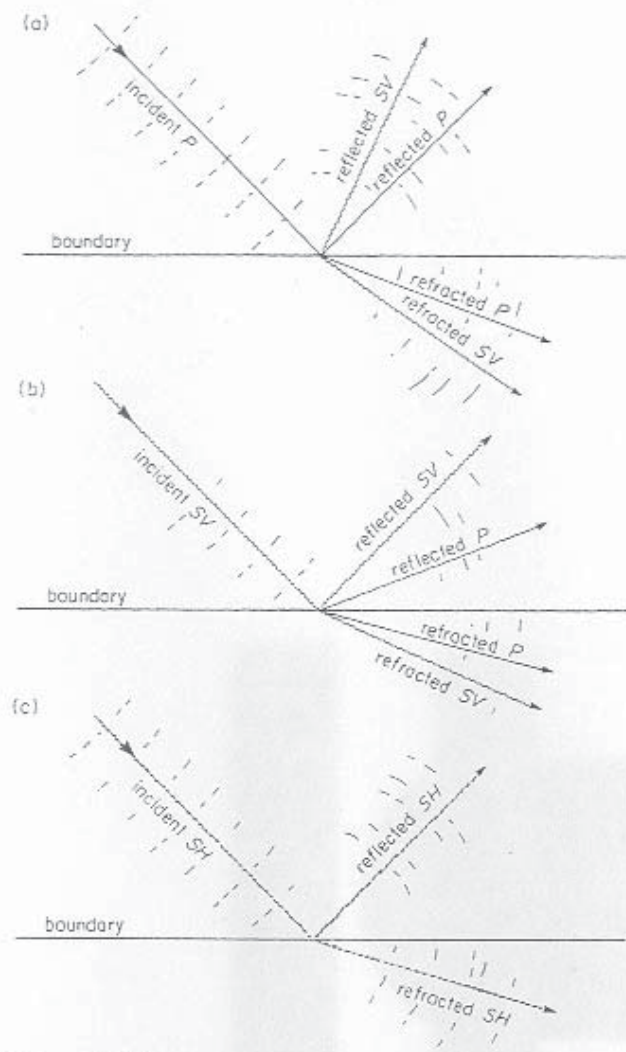


Figure 2-8
Wave conversions at the boundary between two rock layers. Each incident *P*-wave ray or *SV*-wave ray divides into four reflected and refracted *P*- and *SV*-wave rays. An incident *SH*-wave ray produces only reflected and refracted *SH*-wave rays.

speeds of the waves. To explain this phenomenon, let us suppose that the source of the incident *P*-waves is situated far from the boundary. One implication is that two rays that originate together are almost parallel at the boundary. Another implication is that the portion of a wave front between these two rays is so small that it is nearly a straight line. In the following things further, we will look only at reflected and refracted *P*-waves, ignoring other reflected and refracted waves.

Now examine in Figure 2-9 the incident wave rays and straight wave fronts close to the boundary. The incident wave moves at speed V_1 . It takes the same time for one point on the wave front to move from *A* to *C* as it takes for another point to move from *B* to *D*.

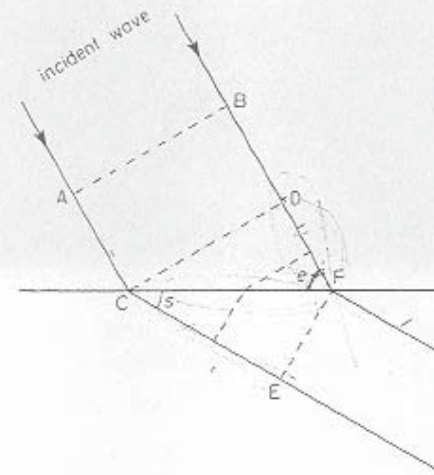


Figure 2-9
Wave refraction at the boundary between two layers. Notice that one point on the wave front advances from *D* to *F* at speed V_1 during the same time that another point on the same wave front advances from *C* to *E* at speed V_2 . The wave front bends at the boundary as it moves along.

Snell's Law

The directions of refracted and reflected waves traveling away from a boundary depend on the direction of the incident wave and the

both parts of the wave front are moving at speed V_1 . After C is reached, that point on the wave front refracts into a new direction and travels at speed V_2 toward E. Let t be the interval of time needed for the wave at that point to travel from C to E. Then, by rearranging Equation 2-8, we can show that the distance $\underline{CE} = V_2t$. During the same interval of time, the other point continues from D to F at speed V_1 . This requires that the distance $\underline{DF} = V_1t$. Observe that the wave front bends where it crosses the boundary.

The incident rays are inclined from the boundary at the angle e . Because rays are perpendicular to wave fronts, the figure CDF is a right triangle. Therefore, from trigonometry we recognize that $\underline{\cos e} = \underline{DF/CF} = \underline{V_1t/CF}$. This expression can be rearranged so that

$$CF = V_1t/\cos e \quad (2-13a)$$

The refracted rays are inclined at the angle s from the boundary. Since the figure CEF is a right triangle, we see that $\underline{\cos s} = \underline{CE/CF} = \underline{V_2t/CF}$. We can rearrange this expression to get

$$CF = V_2t/\cos s \quad (2-13b)$$

Combining and rearranging Equations 2-13a and 2-13b shows how wave speeds and directions are related:

$$\frac{\cos e}{\cos s} = \frac{V_1}{V_2} \quad (2-14)$$

Next, let us consider the relationship between a reflected wave and the incident wave that produced it. The case of an incident P -wave and the reflected SV -wave is illustrated in Figure 2-10, where the same letters that appear in Figure 2-9 are used. Now reread the previous two paragraphs, making the following changes. Replace the word "refract" with the word "reflect" and change V_1 and V_2

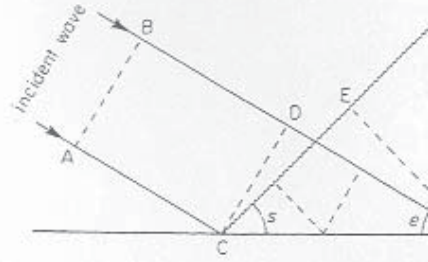


Figure 2-10

Example of wave reflection at the boundary between two rock layers in which a reflected P -wave is produced by an incident P -wave (not shown). Notice that a point on the wave front travels from D to F during the same time that a point on the reflecting surface travels from C to E.

to V_p and V_s . We will see that Equation 2-14 also shows how incident and reflected wave speeds and directions are related. To understand that an incident P -wave produces a reflected P -wave (Figure 2-11) travels at the same speed. For this case, Equation 2-11 shows that the incident and reflected rays are inclined from the boundary at the same angle.

It is a more common practice among geophysicists to draw a line perpendicular to the boundary and to measure the angle i of the incident ray and the angle r of the reflected ray from this line (Figure 2-12). We will follow this practice and rewrite Equation 2-14 in the form

$$\frac{\sin i}{\sin r} = \frac{V_i}{V_r}$$

where V_i is the speed of the incident wave, V_r is the speed of the reflected wave. This equation is called Snell's law and governs the directions of all refracted

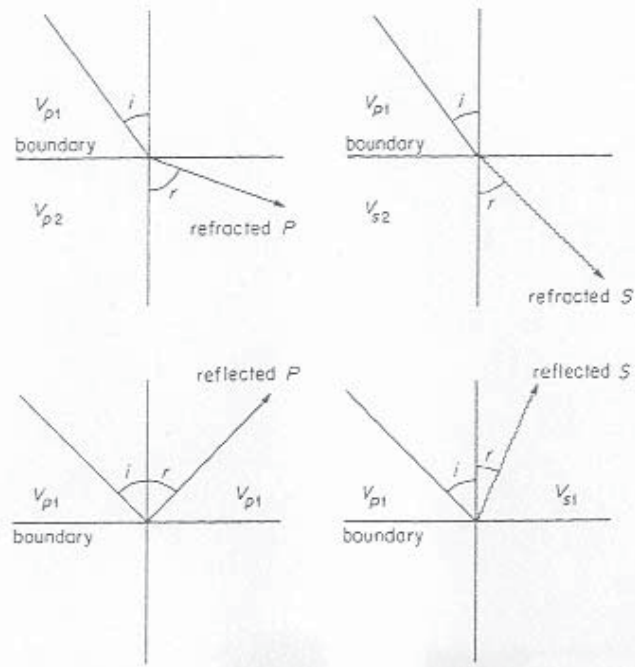


Figure 2-11
Angles of incidence (i) and reflection and refraction (r) measured from a line perpendicular to the boundary between two rock layers are shown separately for the four P - and SV -waves that are produced by an incident P -wave.

reflected P - and S -waves produced by an incident P -wave or an incident S -wave.

Critical Refraction

Let us look further at how seismic waves cross a boundary between two different kinds of rock. To keep things as simple as possible, we will first consider only incident and refracted P -waves. In Figure 2-12a, rays from a source in the upper layer reach the boundary at different angles of incidence and then continue in the lower layer at different angles of refraction in accordance with Snell's law. Observe that the angle refraction is 90 degrees for one

particular ray. It is the *critically refracted* ray that shows how the wave travels right along the top of the lower layer.

The critically refracted wave is an incident wave traveling along the boundary at the *critical angle of incidence* i_c . For this case of critical refraction, note that $\sin r = \sin 90^\circ = 1$, so according to Snell's law we can write

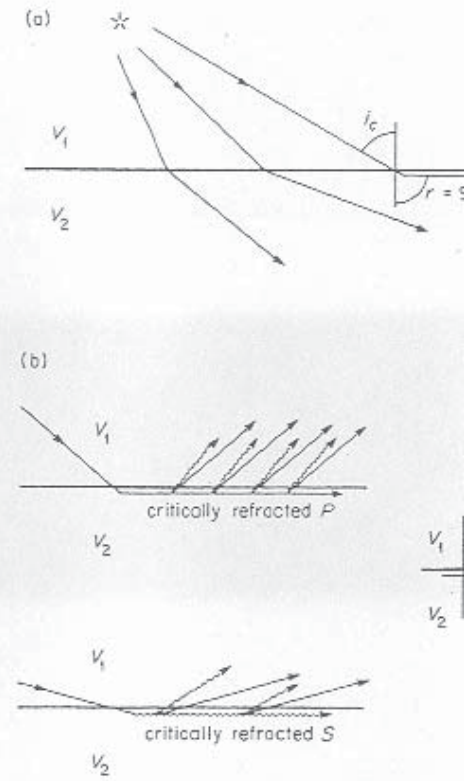


Figure 2-12
Refraction of rays at the boundary between two layers includes (a) a critically refracted ray which the angle of refraction $r = 90^\circ$. This ray is produced from an incident ray that reaches the boundary at the critical angle of incidence. Critically refracted P - and SV -waves along the ray produce P - and SV -waves that refract across the boundary at angles

$$\sin i_c = V_1/V_2 \quad (2-16)$$

which shows how the critical angle depends on the wave speeds. It is obvious that the angle of refraction ($r = 90$ degrees) is larger than the critical angle of incidence. We can tell from Snell's law that this condition is possible only if the refracted wave travels faster than the incident wave. Recall from Figure 2-8 that refracted P - and SV -waves are both produced by either an incident P -wave or an incident SV -wave. Critical refraction can result from any of these combinations if the refracted wave travels faster than the incident wave.

The critically refracted wave does an interesting thing as it travels close to a boundary between two layers. Figure 2-12b shows how a critically refracted P -wave traveling at speed V_{p2} along the top of the lower layer continually produces P - and SV -waves that refract across the boundary. They travel at speeds V_{p1} and V_{s1} in the upper layer. Let i_p and i_s be the angles of the upward directed rays. They are related to the wave speeds according to Snell's law in the same way as Equation 2-16 relates angles of incident and critically refracted rays: $\sin i_p = V_{p1}/V_{p2}$ and $\sin i_s = V_{s1}/V_{p2}$.

A critically refracted SV -wave traveling along the top of the lower layer at speed V_{s2} can also produce P - and SV -waves that refract into the upper layer (Fig. 2-12b). For this case, the angles are related to wave speeds in the following way: $\sin i_p = V_{p1}/V_{s2}$ and $\sin i_s = V_{s1}/V_{s2}$. The P -wave is generated only if $V_{p1} < V_{s2}$.

How does a critically refracted wave continually produce the upward traveling waves illustrated in Figure 2-12? A complete answer would be very complicated. We can glean some understanding from *Huygen's principle*, a statement which asserts that every point on a wave front is a source of new waves that travel

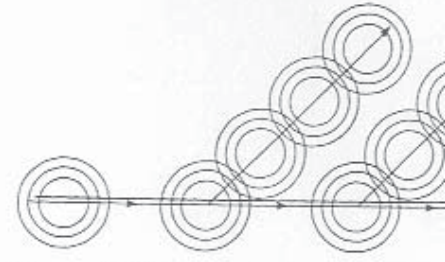


Figure 2-13

Huygen's principle asserts that each wave front is a source of spherically spreading waves. This is shown by spherical waves spreading from different points along an advancing wave front.

away from it in all directions. This is illustrated in Figure 2-13, which shows wave fronts spreading out from an old wave front situated close to the boundary between two layers.

Paths of Seismic Body Waves

The purpose of exploration seismology is to discover what lies underground by measurements made on the earth's surface. Geologists detect seismic waves produced by a source close to the surface that travel along different paths into the earth, and then return to the surface. Rays from the source travel in different directions and refract and reflect at a boundary between different subsurface layers in accordance with Snell's law. Which ray will reach a detector located some distance away from the source?

First, consider a very simple structure consisting of two horizontal layers (Fig. 2-14) in which the wave speeds are V_{s2} and V_{s1} , with $V_{s2} > V_{s1}$. Suppose that only P -waves are produced at the source. We can see that the wave front extends along the land surface and

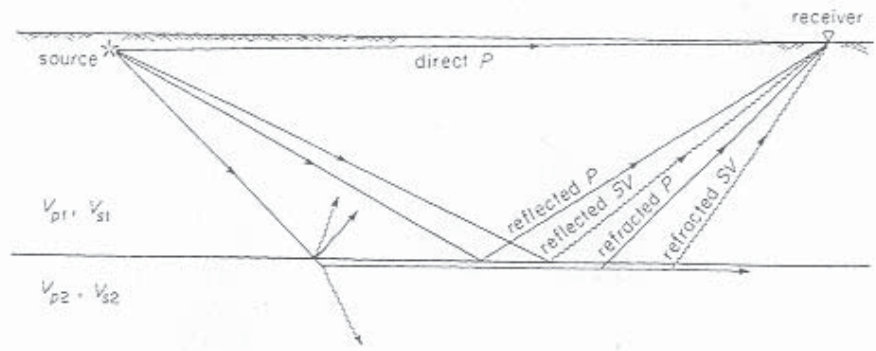


Figure 2-14
 Paths followed by seismic waves from a source to a receiver in an idealized structure of only two rock layers. The wave speeds V_{p1} , V_{s1} , V_{p2} , and V_{s2} are such that $V_{p1} > V_{s2} > V_{s1}$. Each path is consistent with Snell's law.

path of the *direct wave*. Other rays mark paths of the reflected *P*- and *SV*-waves produced by different incident *P*-waves. Still another incident *P*-wave produces the critically refracted ray from which *P*- and *SV*-waves refract to the surface. Altogether, there are five different paths leading to the detector.

Next, look at a structure with several horizontal layers (Figure 2-15). We know that each ray divides into four refracted and reflected *P*- and *SV*-wave rays when it reaches a boundary. Clearly, there will be a large number of paths leading to a detector. By omitting all *SV*-wave rays from the diagram and showing only refracted and reflected *P*-waves, we

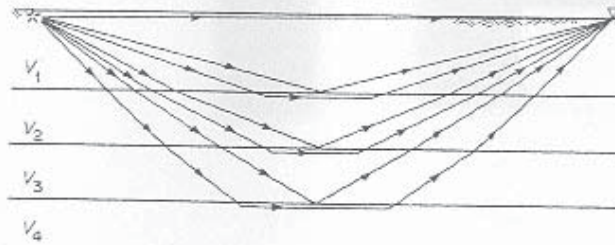


Figure 2-15
 Paths followed by *P*-waves from a source to a receiver in a structure consisting of four parallel layers in which the wave speeds $V_{p1} < V_{p2} < V_{p3} < V_{p4}$. The paths of *SV*-waves that also would be produced are not shown in this example.

still have many rays converging at the detector.

How much time is required for a wave to follow one of these paths? The travel time interval can be calculated from Snell's law if we know the length of the path in each layer. For example, the travel time t needed for a wave to travel along the path ABCD in Figure 2-16 would be

$$t = t_{AB} + t_{BC} + t_{CD} = \frac{AB}{V_{p1}} + \frac{BC}{V_{p2}} + \dots$$

Suppose for the moment that seismic waves were not constrained by Snell's law. They could follow other paths as well. What is the shortest path to be refracted along various paths?

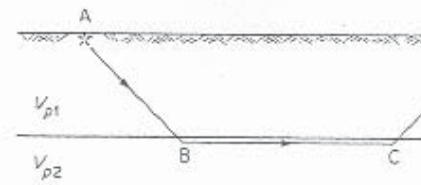


Figure 2-16
 Segments of the path of the refracted wave traveling from a source at A to a receiver at C. Wave speed is V_{p1} along segments AB and CD. Along the segment BC, the wave travels with wave speed V_{p2} .

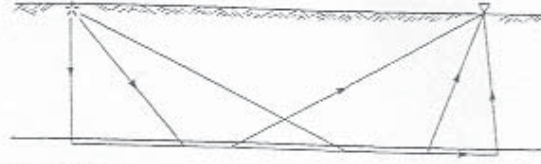


Figure 2-17

Alternate wave paths for testing Fermat's principle. By comparing the travel times along these different paths, we can find the smallest value for the path that is consistent with Snell's law.

ones illustrated in Figure 2-17? Calculating the travel times for these different routes reveals that the particular path requiring the least time is the path predicted from Snell's law. But we know that seismic waves are governed by Snell's law, which means that they do follow paths of minimum travel time. A statement of this fact is called *Fermat's principle*, which asserts that elastic waves travel between two points along paths requiring the least time.

SEISMIC SURFACE WAVES

Recall our discussion of the nature of vibrations produced by passing seismic body waves. As a *P*-wave pulse moves through a rock layer, particles vibrate back and forth in the direction of the ray that marks the path of the wave. The vibrations produced by an *S*-wave are perpendicular to the ray pointing out its path. Material close to the earth's surface experiences these kinds of *P*- and *S*-wave vibrations and other more complicated patterns of vibration as well. These additional kinds of vibration can be measured only at locations close to the surface. Instruments placed away

from the surface in boreholes measure them. Such vibrations must result from waves that follow paths close to the earth's surface. We call them seismic surface waves.

Rayleigh Waves

Vibrations produced by seismic surface waves are separated into two types. One type is ground movement in a vertical plane with the path of the wave (Figure 2-18). This type of vibration is produced by a surface wave bearing the name of the physicist J. W. S. Rayleigh (1842-1919), who made important contributions to our understanding of elasticity. Unlike body waves that move in simple movements back and forth along a straight line, passing Rayleigh waves cause a point on the ground to move in a path shaped like an ellipse.

Another important difference

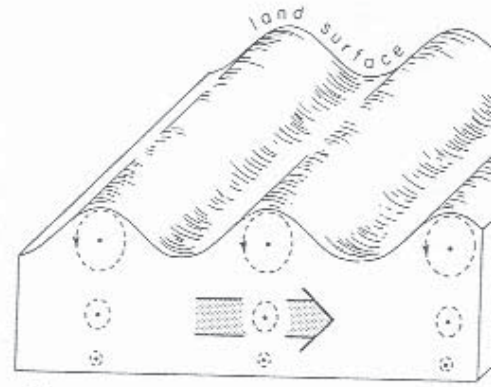


Figure 2-18

Ground vibration produced by Rayleigh waves. Notice that the amplitude of vibration decreases with depth. As the waves pass, a point on the surface moves through an elliptical orbit in a vertical plane.

tion of the Rayleigh wave vibration. Ordinarily, a passing body wave pulse will cause a point on the ground to move back and forth a few times before coming to rest. But the Rayleigh wave vibration tends to persist much longer. The point on the ground will cycle around its elliptical path many times.

Rayleigh wave vibrations change with time in an interesting way. As the wave travels past, the ground vibrates slowly at first and then more and more rapidly. The wave frequency increases with time. As we have noted previously, this kind of vibration can be detected close to the earth's surface but becomes weaker with depth below the surface, rapidly diminishing to a level that cannot be measured.

The Rayleigh wave travels at a speed that is slower than the direct *S*-wave. It follows a path along the earth's surface.

Love Waves

The other type of seismic surface wave named after A. E. H. Love (1864-1926), a pioneer geophysicist. Like the Rayleigh wave, the Love wave travels at a slower speed than the direct *S*-wave. But the direct *S*-wave vibration is different. A passing *S*-wave causes horizontal ground movement perpendicular to the path of the wave. And, unlike an *S*-wave, which causes ground movement in the same direction as the wave passes, the Love wave vibration persists much longer. Following many cycles of oscillation of this persistent Love wave vibration, similar to Rayleigh wave ground motion, beginning slowly, the oscillation grows faster as the wave passes. In other words, frequency increases with time.

Wave Guides

In this discussion, we will not give a theoretical explanation of seismic wave guides. But we can gain some understanding by looking at *P*- and *S*-waves trapped in layers close to the earth's surface.

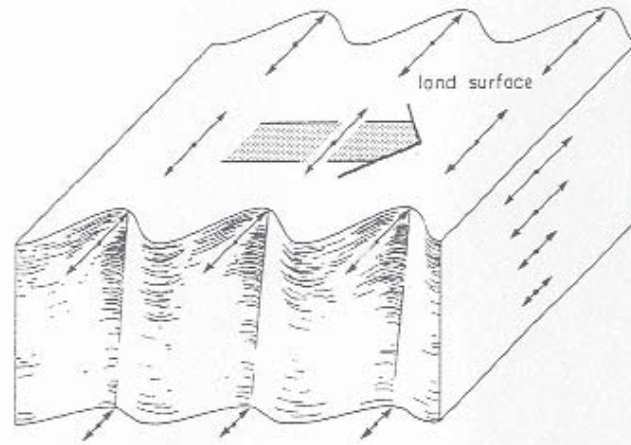


Figure 2-19

Ground vibration produced by Love waves. A point on the land surface cycles back and forth on a horizontal line perpendicular to the direction in which the wave is moving. Amplitude of this horizontal ground movement diminishes with depth.

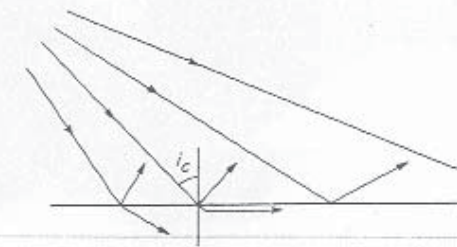


Figure 2-20

Rays reaching a boundary at angles greater than the critical angle of incidence are totally reflected. No refracted waves are produced.

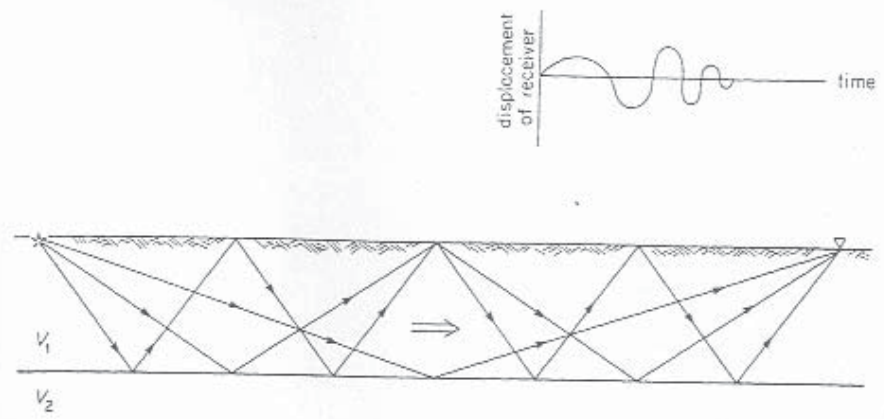


Figure 2-21
Body waves that are reflected at the upper boundaries of a "low-speed" layer can interact to produce surface waves.

We have already seen what happens to body wave rays that are incident on a boundary at angles less than or equal to the critical angle i_c (Figure 2-11). These divide into refracted and reflected P - and SV -waves. But what about a ray with an angle of incidence larger than i_c ? It produces only a reflected wave! No wave will refract across the boundary (Figure 2-20). What does this have to do with surface waves?

Typically, layers very close to the earth's surface are "low-speed" layers. Body waves travel more slowly in these layers of soil and weathered rock than in the underlying harder rock. Figure 2-21 shows what happens to P - and S -waves that are incident on the base of a single "low-speed" layer at angles larger than the critical angle i_c . These waves remain trapped in the low-speed layer, repeatedly reflecting from its base and its upper surface. Because the waves are guided along paths completely within the layer and cannot escape from it, the low-speed layer is called a *waveguide*.

Look at the individual paths in Figure 2-21 of waves traveling in the waveguide from a source to a seismometer. The length of a path depends on the number of times it is reflected. Shorter paths have fewer reflections. Because

more time is needed to travel a longer path, a succession of waves will reach the receiver. Each successively later wave has followed a path with one more reflection at the base of the waveguide.

Now suppose that each wave has a different phase of oscillation to the ground motion recorded by a seismometer. The succession of reflected waves will then produce a complex sequence of oscillations. P -waves and SV -waves in this fashion contribute to the oscillation we recognize as Rayleigh waves. Reflected SH -waves produce the transverse sequence of vibrations that we recognize as Love waves.

SEISMOGRAMS

Seismic waves follow many different paths between a source and a receiver located some distance away. At the receiver, the vibrations are recorded on a chart that produces a *seismogram*. The pattern of vibrations played on a seismogram depends on the nature of the waves produced at the source and on how the size of a wave changes along its path.

The Source Wavelet

Suppose that an explosive is detonated at some point in the earth. This is a particularly effective way to produce *P*-waves. Severe deformation occurs in the zone very close to the charge. Rock is shattered and partly melted in this small *source zone*. Outside the source zone, however, there is only momentary elastic deformation indicated by vibrations.

Let us examine the vibration just outside the source zone. In Figure 2-22, *P*-wave rays extend outward in all directions. An individual particle vibrates back and forth in the direction of a ray. This motion is described on the

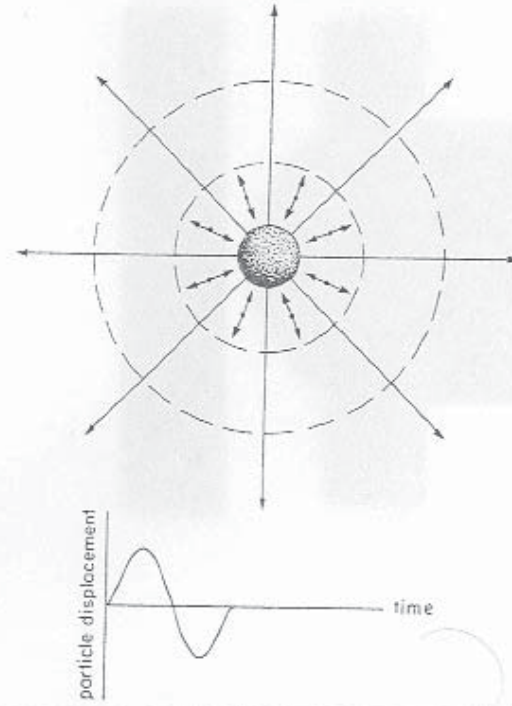


Figure 2-22

Wavelet produced in the source zone is the pulse of vibration that travels outward in all directions. In this idealized example, the source wavelet consists of a single cycle of oscillation.

accompanying graph, which shows the displacement of the particle from its position changes with time. The shape of this brief pulse of vibration is called the *wavelet*. It advances outward from the source zone in all directions.

We can think of the graph in Figure 2-22 as the seismogram that would be recorded at a location very close to the source zone. In this example, it has a simple shape consisting of only one cycle of oscillation. Some wavelets of more complicated shape are discussed in Chapter 5.

Geometrical Spreading and Amplitude

As a source wavelet travels farther from the source, its amplitude decreases. The ground vibration is proportional to the energy of the wave, which is constant after the wavelet leaves the source zone. After the wavelet leaves the source zone, it receives no more energy. The advancing wavelet has a continually expanding spherical wave front (Figure 2-7). As the wave front expands, the same quantity of energy must be distributed over a larger surface. This means that less energy is available for each particle on that surface than was available to other particles closer to the source where the wave front was smaller. Particles farther from the source receive smaller amplitudes than particles closer to the source. This is the result of the effect called *geometrical spreading*.

How much change in wave amplitude do we expect from geometrical spreading? The surface area of a sphere with radius r is $4\pi r^2$. The energy available to a particle is proportional to the total energy Ω divided by the surface area $4\pi r^2$. It is possible to prove that the amplitude of the particle vibration is proportional to $1/r$.

$\sqrt{\Omega}$. This means that amplitude decreases directly with distance from the source,

$$H = H_0/x \quad (2-18)$$

where H_0 is the amplitude of the wavelet leaving the source zone.

When something begins to vibrate, it usually begins to grow warmer at the same time. Heat is produced by the internal friction of particles rubbing together during the process of vibration. In this way, some of the energy of a seismic wave is converted into heat. We say that this wave energy has been absorbed by the material through which the wavelet is traveling. Energy used in this way is not available to cause vibration. So the effect we call *absorption* causes the amplitude of vibration to decrease with distance from the source.

Although we do not understand the process of absorption very well, we have learned from experiments that its effect on wave amplitude can be predicted from the formula

$$H = H_0 e^{-\alpha x} \quad (2-19)$$

where α is called the *absorption coefficient*, and $e = 2.71828$ is the Napierian constant. The value of α is different for different materials.

We can combine the equations for geometrical spreading and absorption to predict how the amplitude of a seismic wave should change as it travels away from the source:

$$H = H_0 e^{-\alpha x}/x \quad (2-20)$$

Transmission and Reflection Coefficients

The amplitude of a seismic wave is changed by reflection and refraction. Recall from Figure 2-8 that a wave incident on a boundary divides into reflected and refracted *P*- and *SV*-waves. Because the energy must be shared be-

tween these reflected and refracted waves, they will have smaller amplitudes than the incident wave.

Ratios that compare the amplitudes of reflected and refracted waves to the amplitude of the incident wave can be called *reflection* and *transmission coefficients*. Suppose that an incident *P*-wave of amplitude H_0 produces reflected *P*- and *SV*-waves with amplitudes H_{1p} and H_{1s} . The ratios

$$R_{1p} = H_{1p}/H_0 \quad \text{and} \quad R_{1s} = H_{1s}/H_0$$

are called the *reflection coefficients*. An incident wave also produces refracted *P*- and *SV*-waves with amplitudes H_{2p} and H_{2s} . The ratios

$$T_{2p} = H_{2p}/H_0 \quad \text{and} \quad T_{2s} = H_{2s}/H_0$$

are called either *transmission coefficients* or *fraction coefficients*.

Values of transmission and reflection coefficients depend on the angle of incidence, the densities of the two layers, and the speeds in these layers. For most materials, R_{1p} and T_{2p} are larger than R_{1s} and T_{2s} for an incident *P*-wave. The opposite is true for an incident *SV*-wave, where R_{1s} and T_{2s} tend to be larger than R_{1p} and T_{2p} . If the angle of incidence is zero for a *P*-wave, then $R_{1s} = R_{1p}$ and $T_{2s} = T_{2p}$.

$$R_{1p} = \frac{\rho_2 V_{2p} - \rho_1 V_{1p}}{\rho_2 V_{2p} + \rho_1 V_{1p}}, \quad T_{2p} = \frac{2 \rho_1 V_{1p}}{\rho_2 V_{2p} + \rho_1 V_{1p}}$$

More complicated formulas are needed to compute the transmission and reflection coefficients when the angle of incidence is not zero.

Vibrations at a Receiver

What pattern of vibration do we expect from a source some distance away from a receiver? Suppose that a wavelet

form (Figure 2-22) is produced at the source. Look again at Figures 2-14 and 2-21, which show that many different paths lead this simple pulse of vibration from the source to a receiver. Because of the different distances and wave speeds along these various paths, pulses of vibration reach the receiver at different times. The effects of geometrical spreading, absorption, refraction, and reflection are different along each of these paths. Therefore, the pulses of vibration will have different amplitudes when they reach the receiver.

Now suppose that we plot a graph of the ground vibration at the receiver that would be produced by waves following the paths in Figures 2-14 and 2-21. The result is the *seismogram* seen in Figure 2-23. It consists of several discrete pulses followed by a continuous series of oscillations. Each pulse has the same shape as the source wavelet, but a different amplitude. These pulses indicate waves that followed the paths shown in Figure 2-14. The continuous oscillations that follow are surface waves related to paths seen in Figure 2-21.

The example in Figure 2-23 shows several

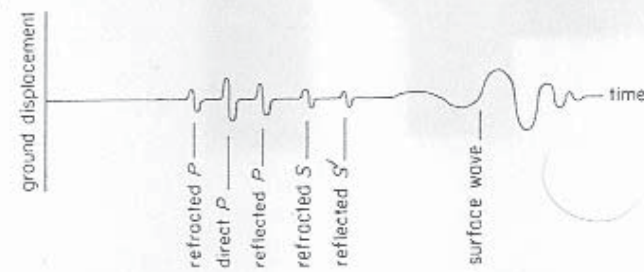


Figure 2-23

Seismogram consisting of body wave pulses, each having the same shape as the source wavelet, and surface wave oscillations with frequency that increases with time. The pulses represent the ground vibration produced by body waves that followed the paths in Figure 2-14.

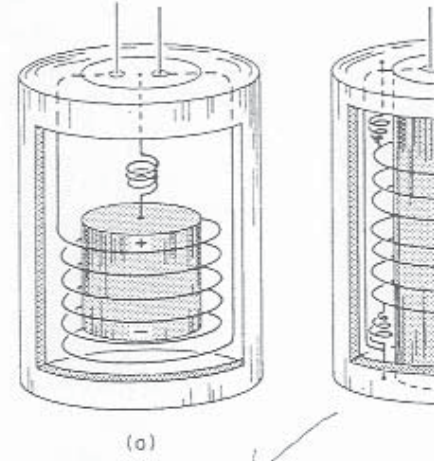


Figure 2-24

A typical geophone (a) has a magnet and coil assembly that can move inside a cylindrical container. Movement of the magnet causes an electric current to flow in the coil. An alternate design consists of a coil of wire and springs that encloses a magnet fixed to the container.

pulses that are clearly separated from one another. The exploration seismologist is presented with a somewhat more complex pattern of vibrations. In nature, these vibrations are more irregular, and they pass through many more layers. Like the simple pulses, however, these more complex seismograms consist of discrete pulses, one for each different path through the earth, together with surface wave oscillations.

Recording Seismic Waves

The exploration seismologist records ground vibrations with a device that is called a *seismometer* or a *geophone*, an instrument usually about the size of a fist. Two types of signs are illustrated in Figure 2-24. The typical sign consists of a coil of wire

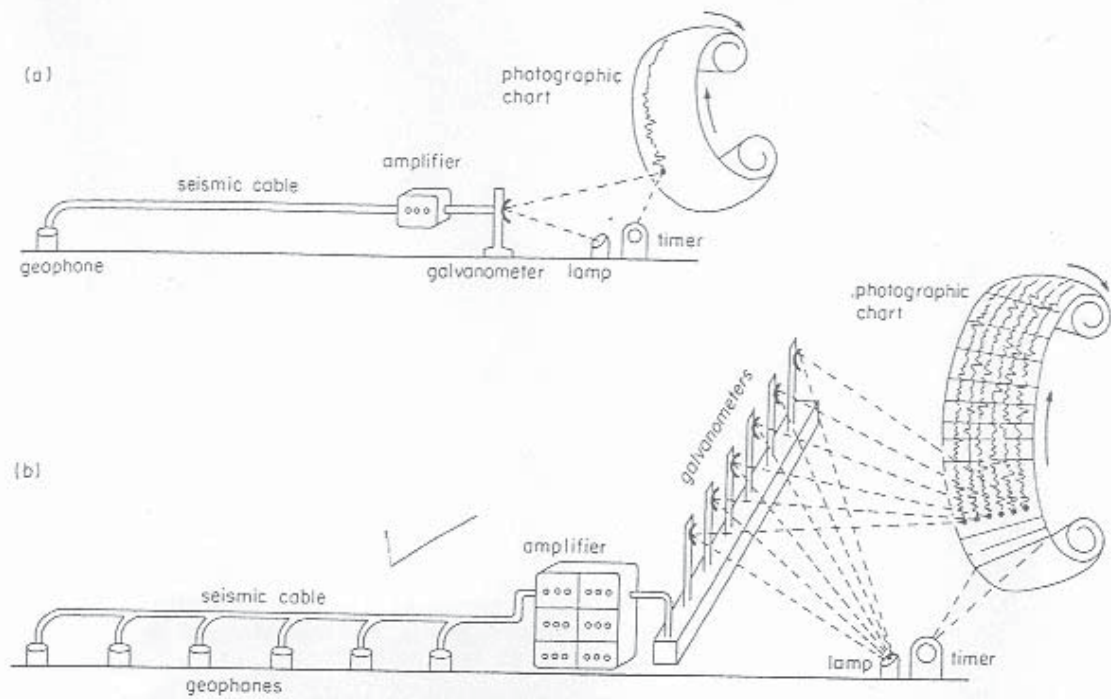


Figure 2-25

Optical-electronic recording of seismic waves. (a) Electric current from the geophone is transmitted through the seismic cable to an amplifier. Then the amplified current activates the galvanometer mirror, which reflects a beam of light onto an advancing photographic chart. (b) A six-channel exploration seismic system with a separate amplifier and galvanometer circuit for recording the electric signal from each geophone.

cylindrical container. A magnetized mass attached to a spring is suspended inside the coil. Ground vibration causes movement of the mass within the coil. Because the mass is a magnet, an electric current that is related to the amplitude of ground vibration is generated in the coil. In the second basic design, the magnet can be fixed to the container and the coil mounted on the spring.

The electric current from a geophone is carried through a line called the *seismic cable* to a recorder. In older seismic recorders, this current was first amplified electronically and then transmitted to a galvanometer (Figure 2-25). This device contains a coil that rotates on

a suspension in response to an current. A concave mirror attached to the coil focuses a point of light from a nearby lamp onto a chart of photographic paper. As the mirror rotates back and forth and the chart advances, usually at a speed of 10 centimeters per second, an irregular line is traced on the chart. This irregular line represents all the pulses of ground vibration recorded in a seismicogram. Marks are also placed on the chart by a timing device.

The most common practice in seismicology is to record simultaneously on the same chart the vibrations detected by 24, 48, or 96 separate geophones

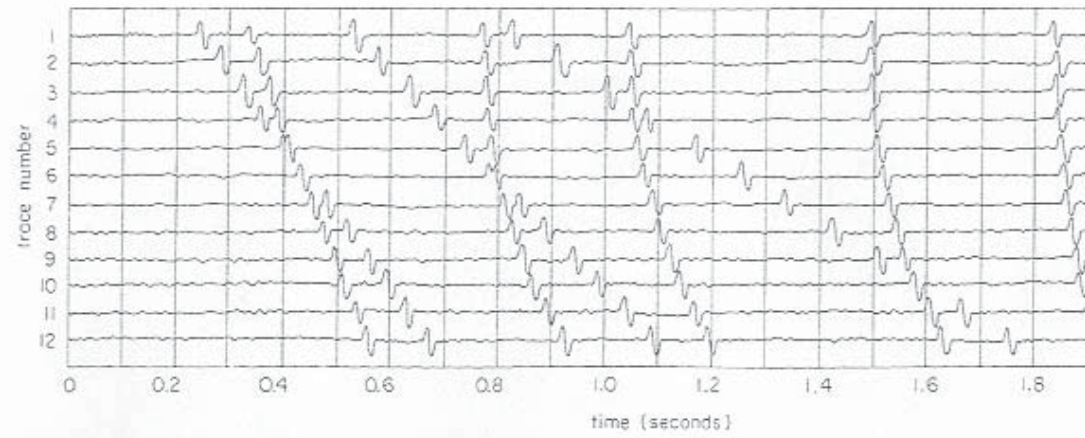


Figure 2-26

A 12-trace exploration seismogram showing pulses of seismic waves refracted and reflected from several rock layers. Vertical time lines on the chart

provide the reference for determining which these various pulses arrive at the geophones.

25). The galvanometers in the recording system are mounted in a row. Lines crossing the chart are exposed every 0.01 second by the timing device. The result is an exploration seismogram (Figure 2-26).

Each geophone-amplifier-galvanometer unit of the system functions independently of the others. Such a unit is one *channel* of an exploration seismic system. The ground vibrations detected by this channel are displayed by one of the irregular lines on the exploration seismogram. Each irregular line is called a *trace*. A 12-channel seismic system, which is larger but otherwise similar to the 6-channel system in Figure 2-25, would produce the 12-trace seismogram shown in Figure 2-26. Modern seismic systems with 6, 12, 24, 48, and 96 channels are described more fully in Chapter 5. These systems are equipped with digital

magnetic tape recorders as well as magnetic tape recorders we have described. Digital magnetic tape are more common. Data processing by computer is discussed in Chapter 6.

How does a geophysicist recognize different pulses of ground vibration that appear on an exploration seismogram? By observing the pulses from a line of geophones on a seismic record we can recognize different pulses. Observe in Figure 2-26 that the pulses lie along straight lines of different angles. The pulses that originate from refracted waves. Methods for analyzing them are presented in Chapter 4. Analysis of reflected waves is discussed in Chapter 4. In Figure 2-26, the pulses that are reflected are indicated by the pulses that lie along the lines.

STUDY EXERCISES

1. Suppose that a P -wave ray produced by an explosion detonated 5 m beneath the ocean surface travels down through the water and reaches solid rock on the ocean bottom at an angle of incidence $i = 30$ degrees. P -wave speed is 1500 m/s in the water and 5000 m/s in the rock.
 - a. How many reflected and refracted rays are generated by this incident ray?
 - b. What is the angle of refraction of the refracted P -wave ray?
2. An SH -wave originating in a solid layer where the shear modulus is μ_1 and the density is ρ_1 refracts across a boundary into another solid layer where the shear modulus μ_2 is equal to μ_1 , but where the density ρ_2 is greater than ρ_1 . This implies that the angle of incidence is (a) larger than or (b) smaller than the angle of incidence. Explain!
3. Consider two solid layers, one resting on the other. In the top layer, the P -wave speed $V_{p1} = 4000$ m/s and the S -wave speed $V_{s1} = 2200$ m/s, and in the deeper layer the P -wave speed $V_{p2} = 4000$ m/s and Poisson's ratio $\sigma = 0.25$. Suppose that an SH -wave originating in the top layer refracts into the deeper layer.
 - a. Is the angle of refraction larger or smaller than the angle of incidence? Explain!
 - b. If the density in the deeper layer is 2.5 g/cm³, what are the values of shear modulus and bulk modulus in that layer?
4. A P -wave traveling at a speed of 3000 m/s in the upper layer refracts across a boundary into a lower layer where its speed increases to 4000 m/s. The frequency of vibration is 30 Hz. What is the length of the refracted P -wave compared to the wavelength of the incident wave? Explain!
5. An incident P -wave traveling at a speed of 3000 m/s is critically refracted at a boundary. The critical angle is 30 degrees, what is the speed of the refracted P -wave?
6. At a distance of 100 m from a source, the amplitude of a P -wave is 0.1000 mm. At a distance of 150 m the amplitude is 0.0665 mm. What is the absorption coefficient of the rock through which the wave travels?

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