

Del: (Nabla)

$$\nabla = \frac{d}{dx} \hat{i} + \frac{d}{dy} \hat{j} + \frac{d}{dz} \hat{k} + \dots$$

$\nabla = \frac{d}{dx} \hat{i} + \frac{d}{dy} \hat{j} + \frac{d}{dz} \hat{k}$ Can be used as an operator.

→ → itni dimensions hon utni terms,
Can be treated quadratic bridge!

as vector

Treated as vectors But sends signals and
remained flying!

Measures distance!

In communication

frequency plays an imp
role.

Del Operator:

Del operators are not vector quantities ~~but~~ ^{iden} ~~can~~ ^{be} treated as operator.

For a differentiable fn

U ,

$$\text{Del } U = \left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) U$$

Now >

(i)

$$\left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) U$$

$$\Rightarrow \text{Del } U = \frac{\partial U}{\partial x} \hat{i} + \frac{\partial U}{\partial y} \hat{j} + \frac{\partial U}{\partial z} \hat{k}$$

This is taken as gradient of the given diff fn U .

(ii)

$$\nabla \cdot U = \left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) \cdot (U_1 \hat{i} + U_2 \hat{j} + U_3 \hat{k})$$

$$\Rightarrow \nabla \cdot U = \frac{\partial U_1}{\partial x} + \frac{\partial U_2}{\partial y} + \frac{\partial U_3}{\partial z}$$

This is taken as the divergence of any diff fn U .

iii) Similarly,

$$\nabla \times U = \left[\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right] \times [U_1 \hat{i} + U_2 \hat{j} + U_3 \hat{k}]$$

$$\nabla \times U = \left(\frac{\partial U_3}{\partial y} - \frac{\partial U_2}{\partial z} \right) \hat{i} + \left(\frac{\partial U_1}{\partial z} - \frac{\partial U_3}{\partial x} \right) \hat{j} + \left(\frac{\partial U_2}{\partial x} - \frac{\partial U_1}{\partial y} \right) \hat{k}$$

is taken as the curl of the given fn. Taken as the rotating measure of the bodies.

eg hot air rising (Tornado)
water circulation in sea, stress river etc -

iv) Also we can extend the concept of Gauss's of Del for the collection of vectors for

$$\nabla (V_1 + V_2) = \nabla V_1 + \nabla V_2 \text{ etc}$$

$$v) \operatorname{div}(\nabla \cdot \nabla)U = \left(\frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \cdot \frac{\partial}{\partial x} \hat{i} + \frac{\partial}{\partial y} \hat{j} + \frac{\partial}{\partial z} \hat{k} \right) U$$

$$\Rightarrow \nabla^2 U = \frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} + \frac{\partial^2 U}{\partial z^2} = \text{Laplacian of the fn.}$$

vii) Del is independent of the coord's system.

eg heart pump, gas is earth for combustion or later for or latter ka.
 $\nabla \rightarrow \Delta$
 cylindrical

if we have one object then $\nabla \rightarrow \Delta$