

point  $E$  is reached. The gradual increase in the strain (or length) of the specimen is followed with the uniform reduction of its cross-sectional area. The work done, during stretching the specimen, is transformed largely into heat and the specimen becomes hot. At  $E$ , the stress, which attains its maximum value is known as **ultimate stress**. It is defined as the largest stress obtained by dividing the largest value of the load reached in a test to the original cross-sectional area of the test piece.

**5. Breaking stress.** After the specimen has reached the ultimate stress, a neck is formed, which decreases the cross-sectional area of the specimen, as shown in Fig. 4.12 (b). A little consideration will show that the stress (or load) necessary to break away the specimen, is less than the maximum stress. The stress is, therefore, reduced until the specimen breaks away at point  $F$ . The stress corresponding to point  $F$  is known as **breaking stress**.

**Note :** The breaking stress (*i.e.* stress at  $F$  which is less than at  $E$ ) appears to be somewhat misleading. As the formation of a neck takes place at  $E$  which reduces the cross-sectional area, it causes the specimen suddenly to fail at  $F$ . If for each value of the strain between  $E$  and  $F$ , the tensile load is divided by the reduced cross-sectional area at the narrowest part of the neck, then the true stress-strain curve will follow the dotted line  $EG$ . However, it is an established practice, to calculate strains on the basis of original cross-sectional area of the specimen.

**6. Percentage reduction in area.** It is the difference between the original cross-sectional area and cross-sectional area at the neck (*i.e.* where the fracture takes place). This difference is expressed as percentage of the original cross-sectional area.

Let  $A$  = Original cross-sectional area, and  
 $a$  = Cross-sectional area at the neck.

Then reduction in area =  $A - a$

and percentage reduction in area =  $\frac{A - a}{A} \times 100$

**7. Percentage elongation.** It is the percentage increase in the standard gauge length (*i.e.* original length) obtained by measuring the fractured specimen after bringing the broken parts together.

Let  $l$  = Gauge length or original length, and  
 $L$  = Length of specimen after fracture or final length.

$\therefore$  Elongation =  $L - l$

and percentage elongation =  $\frac{L - l}{l} \times 100$

**Note :** The percentage elongation gives a measure of ductility of the metal under test. The amount of local extensions depends upon the material and also on the transverse dimensions of the test piece. Since the specimens are to be made from bars, strips, sheets, wires, forgings, castings, etc., therefore it is not possible to make all specimens of one standard size. Since the dimensions of the specimen influence the result, therefore some standard means of comparison of results are necessary.



A recovery truck with crane.

**Note :** This picture is given as additional information and is not a direct example of the current chapter.

## 100 ■ A Textbook of Machine Design

As a result of series of experiments, Barba established a law that in tension, similar test pieces deform similarly and two test pieces are said to be similar if they have the same value of  $\frac{l}{\sqrt{A}}$ , where  $l$  is the gauge length and  $A$  is the cross-sectional area. A little consideration will show that the same material will give the same percentage elongation and percentage reduction in area.

It has been found experimentally by Unwin that the general extension (up to the maximum load) is proportional to the gauge length of the test piece and that the local extension (from maximum load to the breaking load) is proportional to the square root of the cross-sectional area. According to Unwin's formula, the increase in length,

$$\delta l = b.l + C\sqrt{A}$$

and percentage elongation  $= \frac{\delta l}{l} \times 100$

where

$$l = \text{Gauge length,}$$

$$A = \text{Cross-sectional area, and}$$

$$b \text{ and } C = \text{Constants depending upon the quality of the material.}$$

The values of  $b$  and  $C$  are determined by finding the values of  $\delta l$  for two test pieces of known length ( $l$ ) and area ( $A$ ).

**Example 4.10.** A mild steel rod of 12 mm diameter was tested for tensile strength with the gauge length of 60 mm. Following observations were recorded :

Final length = 80 mm; Final diameter = 7 mm; Yield load = 3.4 kN and Ultimate load = 6.1 kN.

Calculate : 1. yield stress, 2. ultimate tensile stress, 3. percentage reduction in area, and 4. percentage elongation.

**Solution.** Given :  $D = 12$  mm ;  $l = 60$  mm ;  $L = 80$  mm ;  $d = 7$  mm ;  $W_y = 3.4$  kN = 3400 N;  $W_u = 6.1$  kN = 6100 N

We know that original area of the rod,

$$A = \frac{\pi}{4} \times D^2 = \frac{\pi}{4} (12)^2 = 113 \text{ mm}^2$$

and final area of the rod,

$$a = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} (7)^2 = 38.5 \text{ mm}^2$$

### 1. Yield stress

We know that yield stress

$$= \frac{W_y}{A} = \frac{3400}{113} = 30.1 \text{ N/mm}^2 = 30.1 \text{ MPa} \quad \text{Ans.}$$

### 2. Ultimate tensile stress

We know the ultimate tensile stress

$$= \frac{W_u}{A} = \frac{6100}{113} = 54 \text{ N/mm}^2 = 54 \text{ MPa} \quad \text{Ans.}$$

### 3. Percentage reduction in area

We know that percentage reduction in area

$$= \frac{A - a}{A} = \frac{113 - 38.5}{113} = 0.66 \text{ or } 66\% \quad \text{Ans.}$$