


Business Statistics:
A Decision-Making Approach
6th Edition

Chapter 13
Introduction to Linear Regression
and Correlation Analysis

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Chapter Goals

After completing this chapter, you should be able to:

- Calculate and interpret the simple correlation between two variables
- Determine whether the correlation is significant
- Calculate and interpret the simple linear regression equation for a set of data
- Understand the assumptions behind regression analysis
- Determine whether a regression model is significant

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Chapter Goals *(continued)*

After completing this chapter, you should be able to:

- Calculate and interpret confidence intervals for the regression coefficients
- Recognize regression analysis applications for purposes of prediction and description
- Recognize some potential problems if regression analysis is used incorrectly
- Recognize nonlinear relationships between two variables

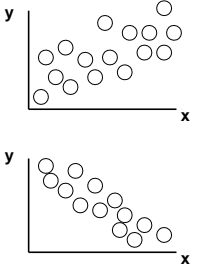
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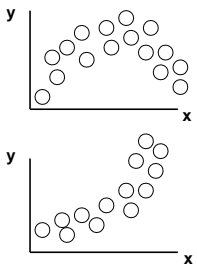
Scatter Plots and Correlation

- A scatter plot (or scatter diagram) is used to show the relationship between two variables
- Correlation analysis is used to measure strength of the association (linear relationship) between two variables
 - Only concerned with strength of the relationship
 - No causal effect is implied

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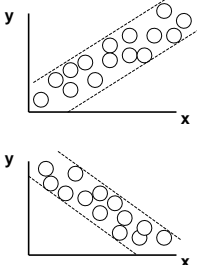
Scatter Plot Examples

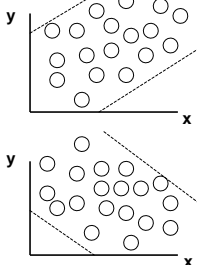
Linear relationships


Curvilinear relationships


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Scatter Plot Examples (continued)

Strong relationships


Weak relationships


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Scatter Plot Examples (continued)

No relationship

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Correlation Coefficient (continued)

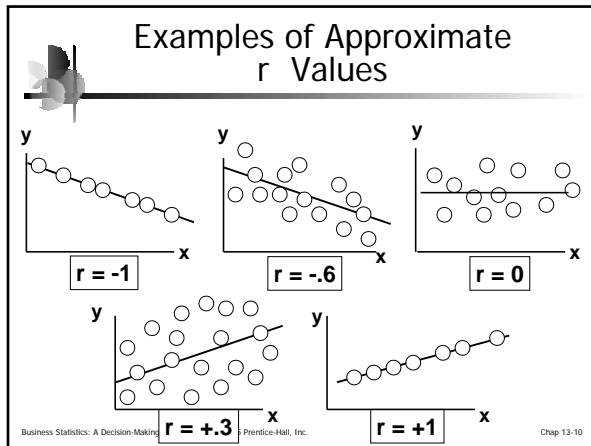
- The population correlation coefficient ρ (rho) measures the strength of the association between the variables
- The sample correlation coefficient r is an estimate of ρ and is used to measure the strength of the linear relationship in the sample observations

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Features of ρ and r

- Unit free
- Range between -1 and 1
- The closer to -1, the stronger the negative linear relationship
- The closer to 1, the stronger the positive linear relationship
- The closer to 0, the weaker the linear relationship

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Calculating the Correlation Coefficient

Sample correlation coefficient:

$$r = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sqrt{[\sum (x - \bar{x})^2][\sum (y - \bar{y})^2]}}$$

or the algebraic equivalent:

$$r = \frac{n\sum xy - \sum x \sum y}{\sqrt{[n(\sum x^2) - (\sum x)^2][n(\sum y^2) - (\sum y)^2]}}$$

where:

- r = Sample correlation coefficient
- n = Sample size
- x = Value of the independent variable
- y = Value of the dependent variable

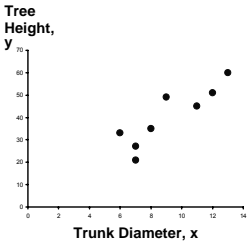
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Calculation Example

Tree Height	Trunk Diameter			
y	x	xy	y ²	x ²
35	8	280	1225	64
49	9	441	2401	81
27	7	189	729	49
33	6	198	1089	36
60	13	780	3600	169
21	7	147	441	49
45	11	495	2025	121
51	12	612	2601	144
Σ=321	Σ=73	Σ=3142	Σ=14111	Σ=713

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Calculation Example (continued)



Tree Height, y


Trunk Diameter, x

$$r = \frac{n\sum xy - \sum x \sum y}{\sqrt{[n(\sum x^2) - (\sum x)^2][n(\sum y^2) - (\sum y)^2]}}$$

$$= \frac{8(3142) - (73)(321)}{\sqrt{[8(713) - (73)^2][8(14111) - (321)^2]}}$$

$$= 0.886$$

r = 0.886 → relatively strong positive linear association between x and y



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Excel Output

Excel Correlation Output

Tools / data analysis / correlation...

	Tree Height	Trunk Diameter
Tree Height	1	
Trunk Diameter	0.886231	1

Correlation between
Tree Height and Trunk Diameter



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Significance Test for Correlation

- Hypotheses

$H_0: \rho = 0$ (no correlation)
 $H_A: \rho \neq 0$ (correlation exists)
- Test statistic

$$t = \frac{r}{\sqrt{\frac{1-r^2}{n-2}}}$$

(with n - 2 degrees of freedom)




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Example: Produce Stores

Is there evidence of a linear relationship between tree height and trunk diameter at the .05 level of significance?

$H_0: \rho = 0$ (No correlation)
 $H_1: \rho \neq 0$ (correlation exists)
 $\alpha = .05, df = 8 - 2 = 6$

$$t = \frac{r}{\frac{\sqrt{1-r^2}}{\sqrt{n-2}}} = \frac{.886}{\frac{\sqrt{1-.886^2}}{\sqrt{8-2}}} = 4.68$$


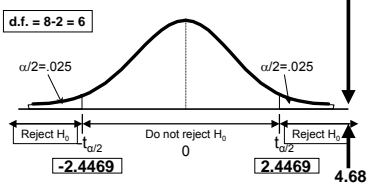
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Example: Test Solution

$t = \frac{r}{\frac{\sqrt{1-r^2}}{\sqrt{n-2}}} = \frac{.886}{\frac{\sqrt{1-.886^2}}{\sqrt{8-2}}} = 4.68$

Decision:
Reject H_0

Conclusion:
There is evidence of a linear relationship at the 5% level of significance



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Introduction to Regression Analysis

- Regression analysis is used to:
 - Predict the value of a dependent variable based on the value of at least one independent variable
 - Explain the impact of changes in an independent variable on the dependent variable

Dependent variable: the variable we wish to explain

Independent variable: the variable used to explain the dependent variable

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Simple Linear Regression Model

- Only **one** independent variable, x
- Relationship between x and y is described by a linear function
- Changes in y are assumed to be caused by changes in x

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Types of Regression Models

Positive Linear Relationship

Relationship NOT Linear

Negative Linear Relationship

No Relationship

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Population Linear Regression

The population regression model:

$$y = \beta_0 + \beta_1 x + \epsilon$$

Labels in the diagram:
 - y : Dependent Variable
 - β_0 : Population y intercept
 - β_1 : Population Slope Coefficient
 - x : Independent Variable
 - ϵ : Random Error term, or residual
 - $\beta_0 + \beta_1 x$: Linear component
 - ϵ : Random Error component

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Linear Regression Assumptions

- Error values (ϵ) are statistically independent
- Error values are normally distributed for any given value of x
- The probability distribution of the errors is normal
- The probability distribution of the errors has constant variance
- The underlying relationship between the x variable and the y variable is linear

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Population Linear Regression

(continued)

$y = \beta_0 + \beta_1x + \epsilon$

Observed Value of y for x_i

Predicted Value of y for x_i

Intercept = β_0

x_i

X

Slope = β_1

Random Error for this x value

ϵ_i

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Estimated Regression Model

The sample regression line provides an estimate of the population regression line

Estimated (or predicted) y value

Estimate of the regression intercept


Estimate of the regression slope

Independent variable

$\hat{y}_i = b_0 + b_1x$

The individual random error terms e_i have a mean of zero

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Least Squares Criterion

- b_0 and b_1 are obtained by finding the values of b_0 and b_1 that minimize the sum of the squared residuals

$$\begin{aligned} \sum e^2 &= \sum (y - \hat{y})^2 \\ &= \sum (y - (b_0 + b_1x))^2 \end{aligned}$$

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The Least Squares Equation

- The formulas for b_1 and b_0 are:

$$b_1 = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sum (x - \bar{x})^2}$$


algebraic equivalent:

$$b_1 = \frac{\sum xy - \frac{\sum x \sum y}{n}}{\sum x^2 - \frac{(\sum x)^2}{n}}$$

and

$$b_0 = \bar{y} - b_1\bar{x}$$


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Interpretation of the Slope and the Intercept

- b_0 is the estimated average value of y when the value of x is zero
- b_1 is the estimated change in the average value of y as a result of a one-unit change in x


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Finding the Least Squares Equation


- The coefficients b_0 and b_1 will usually be found using computer software, such as Excel or Minitab
- Other regression measures will also be computed as part of computer-based regression analysis

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Simple Linear Regression Example

- A real estate agent wishes to examine the relationship between the selling price of a home and its size (measured in square feet)
- A random sample of 10 houses is selected
 - Dependent variable (y) = house price in \$1000s
 - Independent variable (x) = square feet




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Sample Data for House Price Model

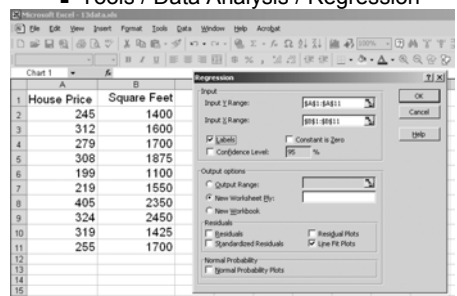
House Price in \$1000s (y)	Square Feet (x)
245	1400
312	1600
279	1700
308	1875
199	1100
219	1550
405	2350
324	2450
319	1425
255	1700



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Regression Using Excel

■ Tools / Data Analysis / Regression



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Excel Output

The regression equation is:

house price = 98.24833 + 0.10977 (square feet)

Regression Statistics	
Multiple R	0.76211
R Square	0.58082
Adjusted R Square	0.52842
Standard Error	41.33032
Observations	10

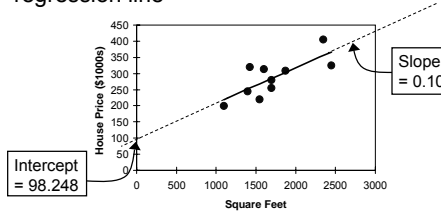
ANOVA					
	df	SS	MS	F	Significance F
Regression	1	18934.9348	18934.9348	11.0848	0.01039
Residual	8	13665.5652	1708.1957		
Total	9	32600.5000			

	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580

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Graphical Presentation

■ House price model: scatter plot and regression line




house price = 98.24833 + 0.10977 (square feet)

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Interpretation of the Intercept, b_0

$$\widehat{\text{house price}} = 98.24833 + 0.10977 (\text{square feet})$$

- b_0 is the estimated average value of Y when the value of X is zero (if $x = 0$ is in the range of observed x values)
 - Here, no houses had 0 square feet, so $b_0 = 98.24833$ just indicates that, for houses within the range of sizes observed, \$98,248.33 is the portion of the house price not explained by square feet




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Interpretation of the Slope Coefficient, b_1

$$\widehat{\text{house price}} = 98.24833 + 0.10977 (\text{square feet})$$

- b_1 measures the estimated change in the average value of Y as a result of a one-unit change in X
 - Here, $b_1 = .10977$ tells us that the average value of a house increases by $.10977(\$1000) = \109.77 , on average, for each additional one square foot of size



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Least Squares Regression Properties

- The sum of the residuals from the least squares regression line is 0 ($\sum (y - \hat{y}) = 0$)
- The sum of the squared residuals is a minimum (minimized $\sum (y - \hat{y})^2$)
- The simple regression line always passes through the mean of the y variable and the mean of the x variable
- The least squares coefficients are unbiased estimates of β_0 and β_1

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Explained and Unexplained Variation

- Total variation is made up of two parts:

$$SST = SSE + SSR$$

Total sum of Squares

Sum of Squares Error

Sum of Squares Regression

$SST = \sum (y - \bar{y})^2$

$SSE = \sum (y - \hat{y})^2$

$SSR = \sum (\hat{y} - \bar{y})^2$

where:

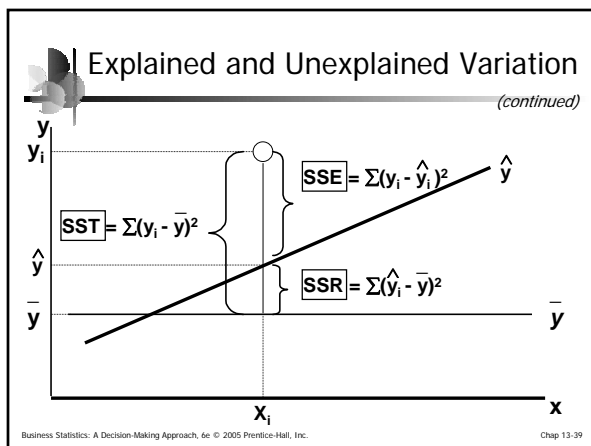
- \bar{y} = Average value of the dependent variable
- y = Observed values of the dependent variable
- \hat{y} = Estimated value of y for the given x value

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Explained and Unexplained Variation (continued)

- SST = total sum of squares**
 - Measures the variation of the y_i values around their mean \bar{y}
- SSE = error sum of squares**
 - Variation attributable to factors other than the relationship between x and y
- SSR = regression sum of squares**
 - Explained variation attributable to the relationship between x and y

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Coefficient of Determination, R^2

- The coefficient of determination is the portion of the total variation in the dependent variable that is explained by variation in the independent variable
- The coefficient of determination is also called R-squared and is denoted as R^2

$$R^2 = \frac{SSR}{SST} \quad \text{where } 0 \leq R^2 \leq 1$$

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Coefficient of Determination, R^2 (continued)

Coefficient of determination

$$R^2 = \frac{SSR}{SST} = \frac{\text{sum of squares explained by regression}}{\text{total sum of squares}}$$

Note: In the single independent variable case, the coefficient of determination is

$$R^2 = r^2$$

where:
 R^2 = Coefficient of determination
 r = Simple correlation coefficient

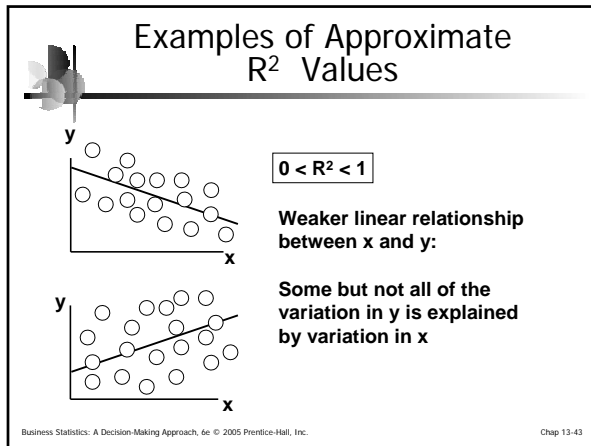
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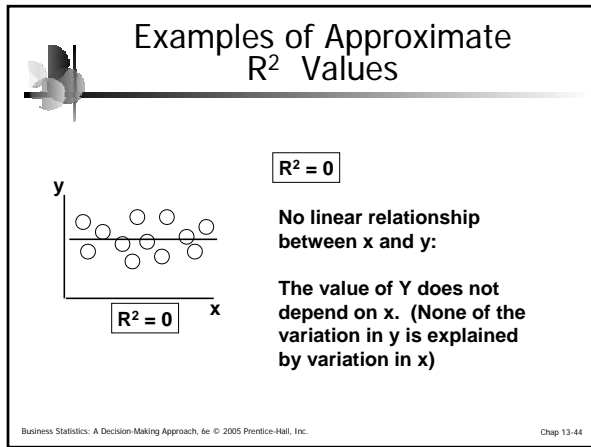
Examples of Approximate R^2 Values

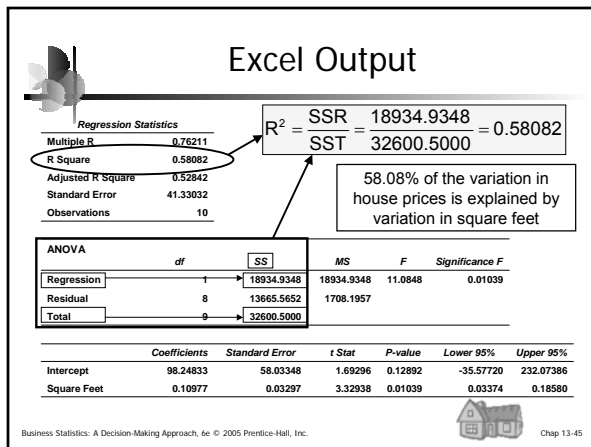
$R^2 = 1$
Perfect linear relationship between x and y:
 100% of the variation in y is explained by variation in x

$R^2 = +1$

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Standard Error of Estimate

- The standard deviation of the variation of observations around the regression line is estimated by

$$s_{\epsilon} = \sqrt{\frac{SSE}{n-k-1}}$$

Where

- SSE = Sum of squares error
- n = Sample size
- k = number of independent variables in the model

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The Standard Deviation of the Regression Slope

- The standard error of the regression slope coefficient (b_1) is estimated by

$$s_{b_1} = \frac{s_{\epsilon}}{\sqrt{\sum(x - \bar{x})^2}} = \frac{s_{\epsilon}}{\sqrt{\sum x^2 - \frac{(\sum x)^2}{n}}}$$

where:

- s_{b_1} = Estimate of the standard error of the least squares slope
- $s_{\epsilon} = \sqrt{\frac{SSE}{n-2}}$ = Sample standard error of the estimate

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Excel Output

Regression Statistics	
Multiple R	0.76211
R Square	0.58082
Adjusted R Square	0.52842
Standard Error	41.33032
Observations	10

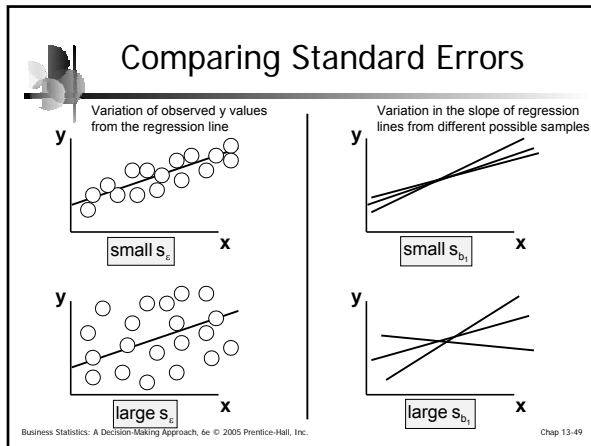
$s_{\epsilon} = 41.33032$

ANOVA		df	SS	MS	F	Significance F
Regression	1	18934.9348	18934.9348	11.0848	0.01039	
Residual	8	13665.5652	1708.1957			
Total	9	32600.5000				

$s_{b_1} = 0.03297$

	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580

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Inference about the Slope: t Test

- t test for a population slope
 - Is there a linear relationship between x and y?
- Null and alternative hypotheses
 - $H_0: \beta_1 = 0$ (no linear relationship)
 - $H_1: \beta_1 \neq 0$ (linear relationship does exist)
- Test statistic

$$t = \frac{b_1 - \beta_1}{s_{b_1}}$$

where:
 b_1 = Sample regression slope coefficient
 β_1 = Hypothesized slope
 s_{b_1} = Estimator of the standard error of the slope

 - d.f. = $n - 2$

Inference about the Slope: t Test

(continued)

House Price in \$1000s (y)	Square Feet (x)
245	1400
312	1600
279	1700
308	1875
199	1100
219	1550
405	2350
324	2450
319	1425
255	1700

Estimated Regression Equation:

$$\widehat{\text{house price}} = 98.25 + 0.1098 (\text{sq. ft.})$$

The slope of this model is 0.1098
Does square footage of the house affect its sales price?

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Inferences about the Slope: t Test Example

Test Statistic: $t = 3.329$

$H_0: \beta_1 = 0$
 $H_A: \beta_1 \neq 0$

From Excel output:

	b_1	S_{b_1}	t
Intercept	98.24833	58.03348	1.69296
Square Feet	0.10977	0.03297	3.32938

Decision: Reject H_0
Conclusion: There is sufficient evidence that square footage affects house price

d.f. = 10 - 2 = 8
 $\alpha/2 = .025$
 -2.3060 2.3060 3.329

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Regression Analysis for Description

Confidence Interval Estimate of the Slope:

$$b_1 \pm t_{\alpha/2} s_{b_1} \quad \text{d.f.} = n - 2$$

Excel Printout for House Prices:

	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580

At 95% level of confidence, the confidence interval for the slope is (0.0337, 0.1858)

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Regression Analysis for Description

	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%
Intercept	98.24833	58.03348	1.69296	0.12892	-35.57720	232.07386
Square Feet	0.10977	0.03297	3.32938	0.01039	0.03374	0.18580

Since the units of the house price variable is \$1000s, we are 95% confident that the average impact on sales price is between \$33.70 and \$185.80 per square foot of house size

This 95% confidence interval does not include 0.
 Conclusion: There is a significant relationship between house price and square feet at the .05 level of significance

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Confidence Interval for the Average y, Given x

Confidence interval estimate for the **mean of y** given a particular x_p

Size of interval varies according to distance away from mean, \bar{x}

$$\hat{y} \pm t_{\alpha/2} s_\epsilon \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum (x - \bar{x})^2}}$$

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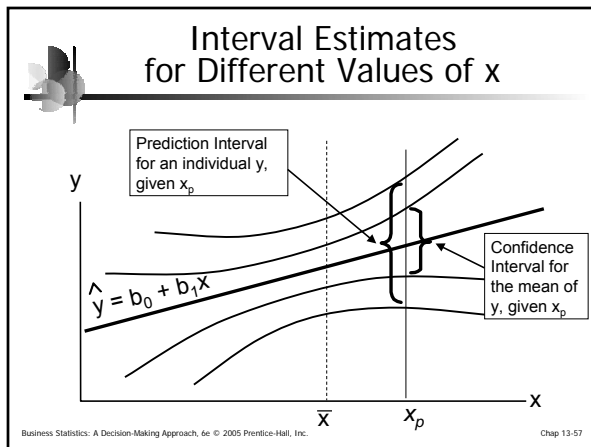
Confidence Interval for an Individual y, Given x

Confidence interval estimate for an **Individual value of y** given a particular x_p

$$\hat{y} \pm t_{\alpha/2} s_\epsilon \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum (x - \bar{x})^2}}$$

This extra term adds to the interval width to reflect the added uncertainty for an individual case

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Example: House Prices

House Price in \$1000s (y)	Square Feet (x)
245	1400
312	1600
279	1700
308	1875
199	1100
219	1550
405	2350
324	2450
319	1425
255	1700

Estimated Regression Equation:
 $\widehat{\text{house price}} = 98.25 + 0.1098 (\text{sq. ft.})$

Predict the price for a house with 2000 square feet

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Example: House Prices

(continued)

Predict the price for a house with 2000 square feet:

$$\begin{aligned} \widehat{\text{house price}} &= 98.25 + 0.1098 (\text{sq. ft.}) \\ &= 98.25 + 0.1098(2000) \\ &= 317.85 \end{aligned}$$

The predicted price for a house with 2000 square feet is 317.85(\$1,000s) = \$317,850

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Estimation of Mean Values: Example

Confidence Interval Estimate for $E(y) | x_p$

Find the 95% confidence interval for the average price of 2,000 square-foot houses

Predicted Price $\hat{Y}_1 = 317.85$ (\$1,000s)

$$\hat{y} \pm t_{\alpha/2} s_e \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum (x - \bar{x})^2}} = 317.85 \pm 37.12$$

The confidence interval endpoints are 280.66 -- 354.90, or from \$280,660 -- \$354,900

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Estimation of Individual Values: Example

Prediction Interval Estimate for $y|x_p$

Find the 95% confidence interval for an individual house with 2,000 square feet

Predicted Price $\hat{Y}_1 = 317.85$ (\$1,000s)

$$\hat{y} \pm t_{\alpha/2} s_e \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum (x - \bar{x})^2}} = 317.85 \pm 102.28$$

The prediction interval endpoints are 215.50 -- 420.07,
or from \$215,500 -- \$420,070

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Finding Confidence and Prediction Intervals PHStat

- In Excel, use
PHStat | regression | simple linear regression ...
- Check the
"confidence and prediction interval for X="
box and enter the x-value and confidence level
desired

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Finding Confidence and Prediction Intervals PHStat (continued)

	A	B
1	Confidence Interval Estimate	
2		
3	Data	
4	X Value	7000
5	Confidence Level	95%
6		
7	Intermediate Calculations	
8	Sample Size	10
9	Degrees of Freedom	9
10	t Value	2.306006
11	Sample Mean	1715
12	Sum of Squared Differences	1677600
13	Standard Error of the Estimate	41.33032
14	t Statistic	0.151886
15	Average Predicted Y (YHat)	317.7830
16		
17	For Average Predicted Y (YHat)	
18	Interval Half Width	27.11962
19	Confidence Interval Lower Limit	290.6634
20	Confidence Interval Upper Limit	354.9033
21		
22	For Individual Response Y	
23	Interval Half Width	102.2813
24	Prediction Interval Lower Limit	215.5025
25	Prediction Interval Upper Limit	420.0651

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Residual Analysis

- Purposes
 - Examine for linearity assumption
 - Examine for constant variance for all levels of x
 - Evaluate normal distribution assumption
- Graphical Analysis of Residuals
 - Can plot residuals vs. x
 - Can create histogram of residuals to check for normality

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Residual Analysis for Linearity

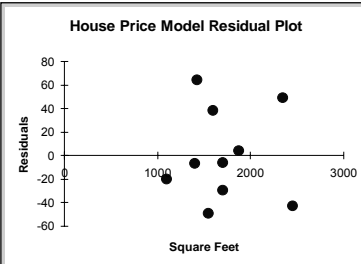
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Residual Analysis for Constant Variance

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Excel Output

RESIDUAL OUTPUT		
	Predicted House Price	Residuals
1	251.92316	-6.923162
2	273.87671	38.12329
3	284.85348	-5.853484
4	304.06284	3.937162
5	218.99284	-19.99284
6	268.38832	-49.38832
7	356.20251	48.79749
8	367.17929	-43.17929
9	254.6674	64.33264
10	284.85348	-29.85348



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Chapter Summary

- Introduced correlation analysis
- Discussed correlation to measure the strength of a linear association
- Introduced simple linear regression analysis
- Calculated the coefficients for the simple linear regression equation
- Described measures of variation (R^2 and s_e)
- Addressed assumptions of regression and correlation

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Chapter Summary

(continued)

- Described inference about the slope
- Addressed estimation of mean values and prediction of individual values
- Discussed residual analysis

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