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## Chapter Goals

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After completing this chapter, you should be able to:

- Compute and interpret the mean, median, and mode for a set of data
- Compute the range, variance, and standard deviation and know what these values mean
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- Construct and interpret a box and whiskers plot
- Compute and explain the coefficient of variation and z scores
- Use numerical measures along with graphs, charts, and tables to describe data $\qquad$

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## Chapter Topics

- Measures of Center and Location $\qquad$
- Mean, median, mode, geometric mean, midrange
- Other measures of Location
- Weighted mean, percentiles, quartiles
- Measures of Variation $\qquad$
- Range, interquartile range, variance and standard deviation, coefficient of variation $\qquad$

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- In an ordered array, the median is the "middle" number $\qquad$
- If n or N is odd, the median is the middle number
- If n or N is even, the median is the average of the $\qquad$ two middle numbers

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| Which measure of location |
| :--- |
| is the "best"? |


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## Percentiles

- The $p^{\text {th }}$ percentile in an ordered array of $n$ values is the value in $\mathrm{i}^{\text {th }}$ position, where

$$
i=\frac{p}{100}(n+1)
$$

- Example: The $60^{\text {th }}$ percentile in an ordered array of 19 values is the value in $12^{\text {th }}$ position:

$$
i=\frac{p}{100}(n+1)=\frac{60}{100}(19+1)=12
$$

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## Quartiles

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- Quartiles split the ranked data into 4 equal
- Example: Find the first quartile

| Sample Data in Ordered Array: 11 | 12 | 13 | 16 | 16 | 17 | 18 | 21 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | ( $\mathrm{n}=9$ )

 so use the value half way between the $2^{\text {nd }}$ and $3^{\text {rd }}$ values
so $\mathrm{Q} 1=12.5$

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## 2) Interquartile Range

- Can eliminate some outlier problems by using the interquartile range
- Eliminate some high-and low-valued observations and calculate the range from the remaining values.
- Interquartile range $=3^{\text {rd }}$ quartile $-1^{\text {st }}$ quartile

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the mean
- Sample variance:

$$
s^{2}=\frac{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2}}{n-1}
$$

- Population variance:

$$
\sigma^{2}=\frac{\sum_{i=1}^{N}\left(x_{i}-\mu\right)^{2}}{N}
$$

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## Standard Deviation

Most commonly used measure of variation

- Shows variation about the mean
- Has the same units as the original data
- Sample standard deviation:

- Population standard deviation:

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## Calculation Example:

## Sample Standard Deviation

## Sample

Data $\left(X_{i}\right):$| 10 | 12 | 14 | 15 | 17 | 18 | 18 | 24 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $n=8$ | Mean $=\bar{x}=16$ |  |  |  |  |  |  |

$$
s=\sqrt{\frac{(10-\bar{x})^{2}+(12-\bar{x})^{2}+(14-\bar{x})^{2}+\cdots+(24-\bar{x})^{2}}{n-1}}
$$

$$
=\sqrt{\frac{(10-16)^{2}+(12-16)^{2}+(14-16)^{2}+\cdots+(24-16)^{2}}{8-1}}
$$

$$
=\sqrt{\frac{126}{7}}=4.2426
$$

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## Coefficient of Variation

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- Measures relative variation $\qquad$
- Always in percentage (\%)
- Shows variation relative to mean
- Is used to compare two or more sets of data measured in different units

| Population | Sample |
| :---: | :---: |
| CV $=\left(\frac{\sigma}{\mu}\right) \cdot 100 \%$ | $C V=\left(\frac{s}{\bar{x}}\right) \cdot 100 \%$ |

$$
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$$

## Comparing Coefficient of Variation

- Stock A:
- Average price last year $=\$ 50$
- Standard deviation = \$5

$$
\mathrm{CV}_{\mathrm{A}}=\left(\frac{\mathrm{s}}{\overline{\mathrm{x}}}\right) \cdot 100 \%=\frac{\$ 5}{\$ 50} \cdot 100 \%=10 \%
$$

- Stock B:
- Average price last year $=\$ 100$
- Standard deviation = \$5 standard
deviation, but
stock B is less variable relative $\mathrm{CV}_{\mathrm{B}}=\left(\frac{s}{\bar{x}}\right) \cdot 100 \%=\frac{\$ 5}{\$ 100} \cdot 100 \%=5 \%$

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- If the data distribution is bell-shaped, then the interval:
- $\mu \pm 1 \sigma$ contains about $68 \%$ of the values in the population or the sample


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## The Empirical Rule

$\mu \pm 2 \sigma$ contains about $95 \%$ of the values in the population or the sample

- $\mu \pm 3 \sigma$ contains about $99.7 \%$ of the values in the population or the sample



## Tchebysheff's Theorem

- Regardless of how the data are distributed, at least ( $1-1 / k^{2}$ ) of the values will fall within k standard deviations of the mean
- Examples:

| At least | within |
| :---: | :---: |
| $\left(1-1 / 1^{2}\right)=0 \% \ldots \ldots \ldots .$. | $\mathrm{k}=1 \quad(\mu \pm 1 \sigma)$ |
| $\left(1-1 / 2^{2}\right)=75 \% \ldots \ldots \ldots . \mathrm{k}=2(\mu \pm 2 \sigma)$ |  |
| $\left(1-1 / 3^{2}\right)=89 \% \ldots \ldots \ldots . \mathrm{k}=3 \quad(\mu \pm 3 \sigma)$ |  |

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+2-2 y+2
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Standardized Population Values

$$
z=\frac{x-\mu}{\sigma}
$$

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- $\mathrm{x}=$ original data value
$\qquad$
- $\sigma=$ population standard deviation
- z = standard score (number of standard deviations x is from $\mu$ )
$\qquad$

$$
z=\frac{x-\bar{x}}{s}
$$

$\qquad$
$\qquad$
where:

- $\mathrm{x}=$ original data value $\qquad$
- $\overline{\mathrm{x}}=$ sample mean
- $\mathrm{s}=$ sample standard deviation $\qquad$
- z = standard score
(number of standard deviations x is from $\mu$ )

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