

Binomial Probability Distributions - Experiments

Experiments consist of repeated independent trials, each trial having only two possible complementary outcomes.

For Example -

The two possible outcomes of a trial may be head & tail, success & failure, right & wrong, good & defective.

• If the probability of each outcome remains the same throughout the trials then such trials are called the 'Bernoulli trials' & the experiment having n Bernoulli trials is called binomial experiment. In other words, an experiment is called a binomial prob. experiment if it possesses the following four properties:

- (i) The outcomes of each trial may be classified into one of two categories, called success (S) & Failure (F). The outcome of interest is called a success & the other one is failure.
- (ii) The prob. of success, denoted by p , remains constant for all trials.
- (iii) The successive trials are all independent.
- (iv) The experiment is repeated a fixed number of times, say n .

Binomial Mass Function = (PMF)

$$f(x) = P(X=x) = \binom{n}{x} p^x q^{n-x}$$

Range:-

$$x = 0, 1, 2, \dots, n$$

Where

p = prob. of success

q = prob. of failure

$$q = 1 - p$$

$$p + q = 1$$

$$\boxed{q = 1 - p}$$

• The binomial prob. distribution has two parameters

n & p

Mean & Variance:-

$$\text{Mean} = np$$

$$\text{Variance} = npq$$